

Introduction to AC/DC Module





VERSION 4.3

Introduction to the AC/DC Module

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Introduction

The AC/DC Module is used by engineers and scientists to understand, predict, and design electric and magnetic fields in statics and low-frequency applications. Simulations of this kind result in more powerful and efficient products and engineering methods. It allows its users to quickly and accurately predict electromagnetic field distributions, electromagnetic forces, and power dissipation in a proposed design. Compared to traditional prototyping, COMSOL helps to lower costs and can evaluate and predict entities that are not directly measurable in experiments. It also allows the exploration of operating conditions that would destroy a real prototype or be hazardous.

The AC/DC Module includes stationary and dynamic electric and magnetic fields in two-dimensional and three-dimensional spaces along with traditional circuit-based modeling of passive and active devices. All modeling formulations are based on Maxwell's equations or subsets and special cases of these together with material laws like Ohm's law for charge transport. The modeling capabilities are accessed via a number of predefined user interfaces, referred to as AC/DC interfaces, which allow you to set up and solve electromagnetic models. The AC/DC interfaces cover electrostatics, DC current flow, magnetostatics, AC and transient current flow, AC and transient magnetodynamics, and AC electromagnetic (full Maxwell) formulations.

Under the hood, the AC/DC interfaces formulate and solve the differential form of Maxwell's equations together with initial and boundary conditions. The equations are solved using the finite element method with numerically stable edge element discretization in combination with state-of-the-art algorithms for preconditioning and solution of the resulting sparse equation systems. The results are presented in the graphics window through predefined plots of electric and magnetic fields, currents and voltages or as expressions of the physical quantities that you can define freely, and derived tabulated quantities (for example resistance, capacitance, inductance, electromagnetic force, and torque) obtained from a simulation.

The work flow in the module is straightforward and is described by the following steps: define the geometry, select materials, select a suitable AC/DC interface, define boundary and initial conditions, define the finite element mesh, select a solver, and visualize the results. All these steps are accessed from the COMSOL Desktop. The solver step is usually carried out automatically using the default settings, which are already tuned for each specific interface.

The AC/DC Module Model Library describes the AC/DC interfaces and the available features using tutorial and benchmark examples for the different formulations. The library contains models for industrial equipment and devices, tutorial models, and benchmark models for verification and validation of the AC/DC interfaces. See "Opening the Model Library" on page 16 to start exploring now.

This guide is intended to give you a jump start to your modeling work. It contains examples of the typical use of the module, a list of all the AC/DC interfaces including a short description for each interface, and a tutorial example that introduces the modeling workflow.

The Use of the AC/DC Module

The AC/DC Module can model electric, magnetic, and electromagnetic fields in statics and low-frequency applications. The latter means that it covers the modeling of devices that are up to about 0.1 electromagnetic wavelengths in size. Thus, it can be used to model nanodevices up to optical frequencies or for human size devices operated at frequencies up to 10 MHz.

AC/DC simulations are frequently used to extract circuit parameters. Figure 1 shows the electric potential and the magnetic flux lines for a micro-scale square inductor, used for LC bandpass filters in microelectromechanical systems (MEMS). A DC voltage is applied across the electrically conducting square shaped spiral, resulting in

an electric current flow that in turn generates a magnetic field through and around the device.

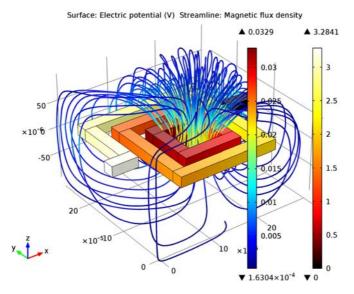


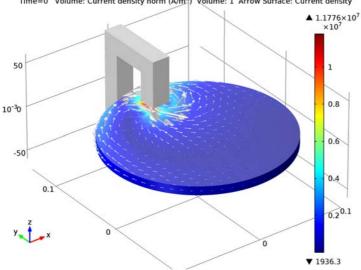
Figure 1: Electric potential distribution and magnetic flux lines for a MEMS inductor.

The distribution and strength of electric and magnetic fields arising from applied current and voltage can be translated into resistance, capacitance, and inductance values for an equivalent circuit model that is easy to understand and analyze from both qualitative and quantitative perspectives. This kind of understanding in terms of a simplified model is usually the first step when creating or improving a design.

Another common use of this module is to predict forces and motion in electric motors and actuators of a wide range of scales.

In the next three figures (Figure 2, Figure 3, and Figure 4), the dynamics of a magnetic brake is shown. The brake consists of a disc of conductive material and a permanent magnet. The magnet generates a constant magnetic field, in which the disc is rotating.

When a conductor moves in a magnetic field it induces currents, and the Lorentz forces from the currents counteracts the spinning of the disc.



Time=0 Volume: Current density norm (A/m²) Volume: 1 Arrow Surface: Current density

Figure 2: The eddy current magnitude and direction in the spinning disc of a magnetic brake.

The braking torque is computed from the magnetic flux and eddy current distributions. It is then fed into a rigid body model for the dynamics of the spinning disc that is solved simultaneously with the electromagnetic model.

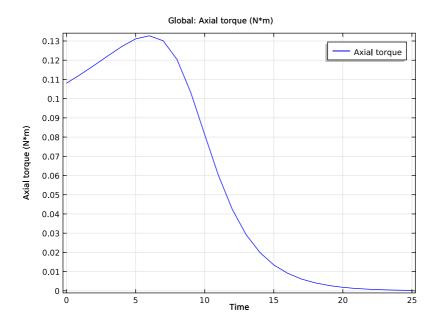


Figure 3: The time evolution of the braking torque.

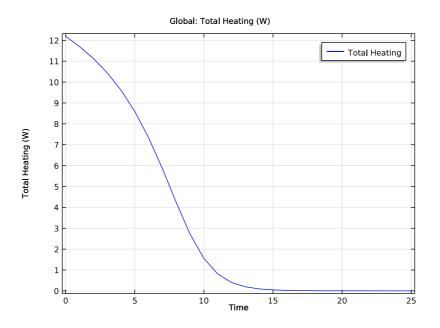


Figure 4: The time evolution of the angular velocity.

The AC/DC Module includes a vast range of tools to evaluate and export results, for example, the evaluation of force, torque, and lumped circuit parameters like resistance, capacitance, inductance, impedance, and scattering matrices (S-parameters). Lumped parameters can also be exported in the Touchstone file format.

The combination of fully distributed electromagnetic field modeling and simplified circuit based modeling is an ideal basis for design, exploration, and optimization. More complex system models can be exploited using circuit-based modeling while maintaining links to full field models for key devices in the circuit allowing for design innovation and optimization on both levels.

The AC/DC Module Interfaces

The AC/DC physics interfaces are based upon Maxwell's equations or subsets and special cases of these together with material laws. Different subsets of Maxwell's equations in combination with special material laws result in different electric, magnetic, or electromagnetic formulations. In the module, these laws of physics are

translated by the AC/DC interfaces to sets of partial differential equations with corresponding initial and boundary conditions.

An AC/DC interface defines a number of features. Each feature represents an operation that describes a term or condition in the underlying Maxwell-based formulation. Such a term or condition may be defined in a geometric entity of the model, such as a domain, boundary, edge (for 3D models), or point.

Figure 5 on the next page uses the Capacitor Tunable model (found in the AC/DC Module Model Library) to show the Model Builder window and the settings window for the selected Charge Conservation I feature node. The Charge Conservation I node also adds the terms to the model equations to a selected geometrical domain representing the electrostatics domain in the model.

Furthermore, and shown in Figure 5, the Charge Conservation I node may link to the Materials node to obtain physical properties such as relative permittivity, in this case the relative permittivity of a user-defined dielectric. The properties, defined by the Dielectric material node, may be functions of the modeled physical quantities, such as temperature. In the same fashion, the Zero Charge I boundary condition feature adds the natural boundary conditions that limit the Electrostatics domain.

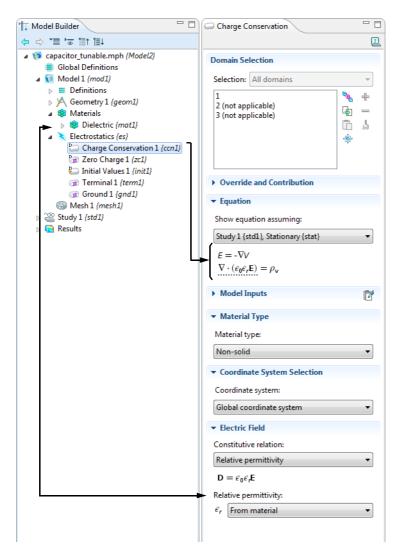


Figure 5: The Model Builder window (to the left), and the Charge Conservation I settings window for the selected feature node (to the right). The Equation section in the settings window shows the model equations and the terms added to the model equations by the Charge Conservation I node. The added terms are underlined with a dotted line. The text also explains the link between the Dialectric node and the values for the Relative permittivity.

The AC/DC Module includes a number of AC/DC interfaces () for different types of electric and/or magnetic modeling. Figure 6 includes the AC/DC interfaces as well

as those under the Heat Transfer folder, which contains the Induction Heating interface. Also see "Physics List by Space Dimension and Preset Study Type" on page 15. A brief overview of the AC/DC interfaces follows.

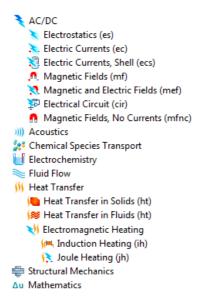


Figure 6: The AC/DC Module physics as displayed in the Model Wizard. Note that this is for 3D models. The Rotating Machinery, Magnetic interface is also available in 2D.

ELECTROSTATICS

The Electrostatics interface () solves a charge conservation equation for the electric potential given the spatial distribution of the electric charge. It is used primarily to model charge conservation in dielectrics under static conditions. The interface applies also under transient conditions but then it is usually combined with a separate transport model for single species or multispecies charge transport. Such transport models can be found in the Chemical Reaction Engineering Module and in the Plasma Module. Some typical applications that are simulated in the interface are capacitors, dielectric sensors, and bushings for high voltage DC insulation.

ELECTRIC CURRENTS

The Electric Currents interface () is used to model DC, AC, and transient electric current flow in conductive and capacitive media. The interface solves a current conservation equation for the electric potential. Some examples of its use are

designing busbars for DC current distribution, computing current distributions in impressed current cathodic corrosion protection, and designing AC capacitors.

ELECTRIC CURRENTS, SHELL

The Electric Currents, Shell interface () is available in 2D, 2D axisymmetric, and 3D geometries. It is used to model DC, AC, and transient electric current flow confined to conductive and capacitive thin current-conducting shells of fixed or varying thickness. The interface solves a boundary current conservation equation for the electric potential. Modeling ground return current flow in the hull of a ship or in the body of a car are two examples of simulations that can be performed using this interface.

MAGNETIC FIELDS

The Magnetic Fields interface (,) solves Ampère's law for the magnetic vector potential. It is used to model magnetostatics, AC, and transient magnetodynamics. Magnets, magnetic actuators, electric motors, transformers, induction based nondestructive testing, and eddy current generation are typical applications for this interface. It supports both linear media and media with magnetic saturation.

MAGNETIC AND ELECTRIC FIELDS

MAGNETIC FIELDS, NO CURRENTS

The Magnetic Fields, No Currents interface (\bigcap) is used to efficiently model magnetostatics in current free regions, for example, when designing permanent magnet-based devices. It solves a magnetic flux conservation equation for the magnetic scalar potential. The interface supports both linear media and media with magnetic saturation.

ELECTRICAL CIRCUIT

The Electrical Circuit interface () has the equations to model electrical circuits with or without connections to a distributed fields model, solving for the voltages,

currents, and charges associated with the circuit elements. Circuit models can contain passive elements like resistors, capacitors, and inductors as well as active elements such as diodes and transistors.

ROTATING MACHINERY, MAGNETIC

The Rotating Machinery, Magnetic interface (()) combines the magnetic fields (magnetic vector potential) and magnetic fields, no currents (scalar magnetic potential) formulations with a selection of predefined frames for prescribed rotation or rotation velocity—it shares most of its features with the Magnetic Fields interface. This interface requires that the geometry is created as an assembly from individual parts for the rotor and stator.

INDUCTION HEATING

The Induction Heating multiphysics interface ((m) combines all features from the Magnetic Fields interface in the time-harmonic formulation with the Heat Transfer interface to model induction and eddy current heating. The predefined interaction adds the electromagnetic losses from the magnetic field as a heat source. This interface is based on the assumption that the magnetic cycle time is short compared to the thermal time scale (adiabatic assumption).

Physics List by Space Dimension and Preset Study Type

The table below list the interfaces available specifically with this module in addition to the COMSOL Multiphysics basic license.

PHYSICS	ICON	TAG	SPACE DIMENSION	PRESET STUDIES
🔪 AC/DC				
Electrostatics*	×	es	all dimensions	stationary; time dependent
Electric Currents*	*	ec	all dimensions	stationary; frequency domain; time dependent; small signal analysis, frequency domain
Electric Currents - Shell	1	ecs	3D, 2D, 2D axisymmetric	stationary; frequency domain; time dependent; small signal analysis, frequency domain
Magnetic Fields*	<u>, n</u>	mf	3D, 2D, 2D axisymmetric	stationary; frequency domain; time dependent; small signal analysis, frequency domain; coil current calculation

PHYSICS	ICON	TAG	SPACE DIMENSION	PRESET STUDIES
Magnetic and Electric Fields	×.	mef	3D, 2D, 2D axisymmetric	stationary; frequency domain; small signal analysis, frequency domain
Magnetic Fields, No Currents	Ω	mfnc	all dimensions	stationary; time dependent
Rotating Machinery, Magnetic	Ì	rmm	3D, 2D	stationary; time dependent
Electrical Circuit	1	cir	Not space dependent	stationary; frequency domain; time dependent
🔰 Electromagnetic Heating				
Induction Heating	<mark>∫n=</mark> i,	ih	3D, 2D, 2D axisymmetric	stationary; frequency domain; time dependent; frequency stationary; frequency transient

functionality for this module.

Opening the Model Library

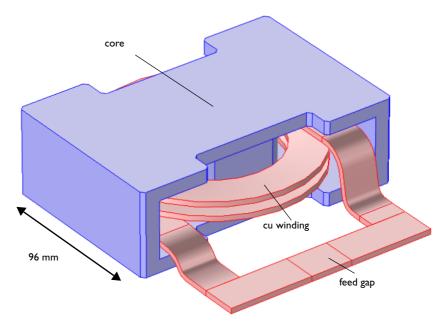
To open an AC/DC Module Model Library model, select **View > Model Library []]** from the main menu in COMSOL Multiphysics. In the Model Library window that opens, expand the AC/DC Module folder and browse or search the contents. Click **Open Model and PDF** to open the model in COMSOL Multiphysics and a PDF to read background theory about the model including the step-by-step instructions to build it. The MPH-files in the COMSOL model libraries can have two formats—Full MPH-files or Compact MPH-files.

- Full MPH-files, including all meshes and solutions. In the Model Library these models appear with the 🕥 icon. If the MPH-file's size exceeds 25MB, a tip with the text "Large file" and the file size appears when you position the cursor at the model's node in the Model Library tree.
- Compact MPH-files with all settings for the model but without built meshes and solution data to save space on the DVD (a few MPH-files have no solutions for other reasons). You can open these models to study the settings and to mesh and re-solve the models. It is also possible to download the full versions—with meshes and solutions—of most of these models through Model Library Update. In the Model Library these models appear with the **(**) icon.

The next section uses a model from the Model Library. Go to "Tutorial Example: Modeling a 3D Inductor" to get started.

Tutorial Example: Modeling a 3D Inductor

Inductors are used in many applications for low-pass filtering or for impedance matching of predominantly capacitive loads. They are used in a wide frequency range from near static up to several MHz. An inductor usually has a magnetic core to increase the inductance, while keeping its size small. The magnetic core also reduces the electromagnetic interference with other devices as the magnetic flux tends to stay within it. Because there are only crude analytical or empirical formulas available to calculate impedances, computer simulations or measurements are necessary during the design stage. In general, inductor modeling is more complex than modeling resistors and capacitors but similar principles apply. Using an external CAD software program to design and draw the model, the geometry is imported into the AC/DC Module for static and frequency domain analysis. The inductor geometry is shown in Figure 7.





First a magnetostatic simulation is performed to get the DC inductance. At low frequencies capacitive effects are negligible. A relevant equivalent circuit model is an ideal inductor in a series with an ideal resistor. The inductance and the resistance are both computed in the magnetostatic simulation. At a high frequency, capacitive

effects become significant. The equivalent circuit model involves connecting an ideal capacitor in parallel with the DC circuit. The circuit parameters are obtained by analyzing the frequency dependent impedance obtained from a frequency domain simulation. In this tutorial, the AC analysis is done up to the point when the frequency dependent impedance is computed.

These step-by-step instructions guide you through the detailed modeling of an inductor in 3D. The module also has a physics interface to model electrical circuits, which is detailed in the magnetostatic part of this model. The first step is to perform a DC simulation.

MODEL WIZARD

- I Double-click the COMSOL Multiphysics icon on the desktop.
- 2 In the Model Wizard, click the 3D button and click Next \Rightarrow .
- 3 In the Add Physics tree under AC/DC, select Magnetic Fields (mf) 💸.
- 4 Click Add Selected ♣ then click Next ♣.
- 5 In the Studies tree, select Preset Studies>Stationary 🗁.
- 6 Click Finish 🚮.

GEOMETRY I

The main geometry is imported from a file. Air domains are typically not part of a CAD geometry, so these are added to the model. For convenience, three additional domains are defined in the CAD file and then used to define a narrow feed gap where an excitation is applied.

Import I

- Under Model I, right-click Geometry I 🕺 and select Import 🗔.
- 2 In the settings window under **Import**, click **Browse**. Then navigate to your COMSOL Multiphysics installation folder, locate the subfolder

ACDC_Module\Inductive_Devices_and_Coils, select the file inductor_3d.mphbin and click Open.

Note: The location of the files used in this exercise varies based on the installation. For example, if the installation is on your hard drive, the file path might be similar to C:\Program Files\COMSOL43\models\.

3 Click Import.

Sphere I

- In the Model Builder, right-click Geometry I and choose Sphere O.
- 2 Go to the **Sphere** settings window. Under **Size** and **Shape** in the **Radius** field, enter **0**.2.

- 3 Click to expand the Layers section. In the associated table, under Thickness enter 0.05.
- 4 Click the **Build All** 📗 button.

Form Union

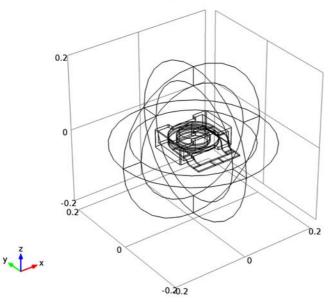
- I In the Model Builder under Geometry I, click Form Union ⊮.
- 2 In the Finalize settings window, click Build All
- 3 On the **Graphics** window toolbar, click the **Zoom Extents** button and then the **Wireframe Rendering** button.

Import		
Build Selected	Build All	2
▼ Import		
Geometry import:		
COMSOL Multipl	nysics file	-
Filename:		
inductor_3d.mpł	ıbin	
Browse	Import	
 Selections of R 	esulting Entities	
Create selectio	ns	
Sphere		- 8
Build Selected	Build All	2
▼ Object Type		
Type: Solid		•
 Size and Shape 		
Radius: 0.2		m
▼ Position		
- Laures		
 Layers 		
Layer name	Thickness (m)	
Layer 1	0.05	
Layer 2		
ት 🕂 🐱		
Finalize		

ł

Finalize	- 8
📙 Build Selected 📲 Build All	2
▼ Finalize	
Finalization method:	
Form a union	•
Relative repair tolerance:	
1.0E-6	

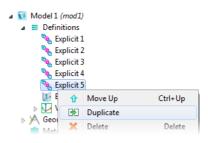
The geometry should match this figure.



DEFINITIONS - SELECTIONS

Use the Selection feature available under the Definitions node to make the set up of materials and physics easier. Start by defining the domain group for the inductor winding and continue by adding other useful selections. These steps illustrate how to set up the Explicit nodes and rename the geometric selections accordingly.

- I In the Model Builder under Model I, right-click Definitions ≡ and choose Selections>Explicit %.
- Repeat Step I and add a total of six (6)
 Explicit nodes . Or right-click the first
 Explicit node and select Duplicate .



The following steps are done one at a time for each node using the table below.

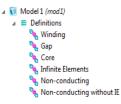
- 3 In the Model Builder click an Explicit node 👒 to open its settings window.
- 4 In the settings window under **Geometric Scope**, select **Domain** from the **Geometric entity Ievel** list. Use the table as a guide, and in the **Graphics** window, select the domains as indicated. Then press F2 and rename the node.

DEFAULT NODE NAME	SELECT THESE DOMAINS	NEW NAME FOR THE NODE
Explicit I	7, 8, and 14	Winding
Explicit 2	9	Gap
Explicit 3	6	Core
Explicit 4	1-4 and 10-13	Infinite Elements
Explicit 5	1–6 and 9–13	Non-conducting
Explicit 6	5,6, and 9	Non-conducting without IE

Note: There are many ways to select geometric entities. When you know the domain to add, such as in this exercise, you can click the **Paste Selection** button and enter the information in the **Selection** field. In this example for the **Explicit I** node, enter **7**,**8**,**14** in the **Paste Selection** window. For more information about selecting geometric entities in the **Graphics** window, see the *COMSOL Multiphysics User's Guide*.

🔞 Paste Se	lection		×
Selection:	7,8,14		
		ОК	Cancel

5 After renaming all the nodes under Definitions, the sequence of nodes should match this figure.



DEFINITIONS - INFINITE ELEMENTS

Use the Infinite Element feature available under the Definitions node to emulate an infinite open space surrounding the inductor. The infinite element coordinate scaling is recognized by any physics interface supporting it - other physics interfaces are automatically disabled in the infinite element domains.

- In the Model Builder under Model I, right-click Definitions \equiv and choose Infinite Element Domain \underline{i}_{∞} .
- **2** Go to the **Infinite Elements** settings window. Under **Domain Selection** select **Infinite Elements** from the **Selection** list.
- 3 Under Geometry from the Type list, select Spherical.

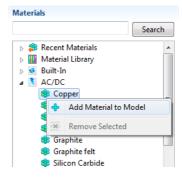
Geometry			
ype:			
Spherical			
14	nato		
Center coordi	nate		
Center coordi	y (m)	z (m)	

MATERIALS

Now define the material settings for the different parts of the inductor. Use the Selections defined in the previous section.

Copper

- From the main menu, select View>Material Browser :
- 2 Go to the Material Browser. In the Materials tree under AC/DC, right-click Copper and choose + Add Material to Model from the menu.



3 In the Model Builder, click Copper.

Air

4 Go to the Material settings window. Under Geometric Entity Selection select Winding from the Selection list.

 Go to the Material Browser. In the Materials tree under Built-In right-click Air and choose
 Add Material to Model from the menu.

3 Go to the Material settings window. Under

Geometric Entity Selection	
Geometric entity level: Domain	•
Selection: Winding	•
7 8 14	🍬 + La 🗕 Ĉ
 Material Material Browser Material Browser 	
Materials	
	Search
Recent Materials	*
 Material Library Built-In Air 	ш
🗯 🕂 🛛 Add Material to Model	
🗱 💌 Remove Selected	
Aluminum 6063-T83	
Aluminum American red oak	
American red oak	

2 In the Model Builder, click Air.

Geometric Entity Selection select Non-conducting from the Selection list.

USER-DEFINED MATERIAL 3

The core material is not included in the material library so it is entered as a user-defined material.

- In the Model Builder, right-click Materials (*) and choose Material (*).
- 2 Go to the Material settings window. Under Geometric Entity Selection select Core from the Selection list.

Geometric Entity Selec	tion		
Geometric entity level:	Domain		•
Selection:	Core		•
6		می آ ث	+

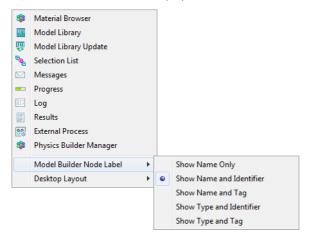
- 3 Under Material Contents in the table, enter these settings in the Value column:
 - 0 for the Electrical conductivity
 - 1 for the Relative permittivity
 - 1e3 for the Relative permeability

Mat	terial Contents				
	Property	Name	Value	Unit	Property group
~	Electrical conductivity	sigma	0	S/m	Basic
~	Relative permittivity	epsilonr	1	1	Basic
~	Relative permeability	mur	1e3	1	Basic

- 4 Press F2 and choose **Rename** <a>a. Go to the **Rename Material** dialog box and enter **Core** in the **New name** field.
- 5 Click **OK**. The node sequence under Materials should match the figure to the right.



To view the **Identifier** (mat1, mat2, mat3) next to the material node name, select **View>Model Builder Node Label** and select one of the options. This changes what combinations of labels are displayed in the Model Builder next to each node.



MAGNETIC FIELDS (MF)

The model is solved everywhere except in the feed gap region. By keeping this void, its default boundary conditions support surface currents closing the current loop. In inductor modeling it is crucial to respect current conservation as this is a law of nature (Ampère's law).

- In the Model Builder under Model I, click Magnetic Fields 👧.
- 2 In the Magnetic Fields settings window, select domains 1–8 and 10–14 only (all domains except 9). Or click the Paste Selection button n and enter 1–8, 10–14 in the Selection field.



Single-Turn Coil Domain 1 and Boundary Feed 1

A dedicated feature is added for the solid copper winding of the inductor. This feature makes it easier to excite the model in various ways.

- Right-click Magnetic Fields and choose the domain setting Single-Turn Coil Domain .
- 2 In the Single-Turn Coil Domain settings window, under Domain Selection, choose Winding from the Selection list.
- 3 Right-click Single-Turn Coil Domain I and at the boundary level choose Boundary Feed a.
- 4 In the Boundary Feed settings window, to the right of the Boundary Selection list, click the Clear Selection button ▲.
- 5 Click the Paste Selection button 💼 and enter 58 in the Selection field. Click OK.

Ground I

- I In the Model Builder, right-click Single-Turn Coil Domain I and choose the boundary condition Ground @.
- 2 In the Ground settings window, to the right of the Boundary Selection list, click the Clear Selection button
- 3 Click the Paste Selection button 👘 and enter 79 in the Selection field. Click OK.

The node sequence under Magnetic Fields should at this point match the figure to the right.



MESH I

The steep radial scaling of the infinite elements region requires a swept mesh to maintain a reasonably effective element quality.

Free Triangular I and Size

- In the Model Builder under Model I, right-click Mesh I (a) and choose More Operations>Free Triangular (%).
- 2 Select Boundaries 9–12, 68, 69, 73, and 76 only. Or click the Paste Selection button n and enter 9–12, 68, 69, 73, 76 in the Paste Selection field.
- 3 In the Model Builder under Mesh I, click Size A. In the Size settings window under Element Size, click the Predefined button. From the list select Coarser.

Free Triangular				
Build Selected 📙 Build All 📃				
Boundary Selection				
Geometric entity level: Boundary 🔻				
Selection:	Manual		-	
9		6	+	
10		L.	_	
11			-	
12			<u>, (</u>	
68				
69		- <u>(</u>		
73				
76				

- 4 Click to expand the **Element Size Parameters** section. In the **Minimum element size** field, enter **0.005**.
- 5 In the Model Builder, right-click Free Triangular I 🛝 and select Build Selected 攌



Swept I and Distribution I

- Right-click Mesh I 💿 and choose Swept 🐞.
- 2 Go to the Swept settings window. Under Domain Selection:
 - From the Geometric entity level list, select Domain.
 - From the Selection list, select Infinite Elements.

- 3 Right-click Swept I i and choose Distribution III.
- 4 Go to the **Distribution** settings window. Under **Distribution** in the **Number of elements** field, enter 4.
- 5 Click Build Selected 🔚.

Free Tetrahedral I

- 2 In the Model Builder, right-click Free Tetrahedral I and choose Build Selected .

The final node sequence under **Mesh** should match the figure.

Distribution	
Build Selected 👖 Build All	2
Domain Selection	
Selection: Manual	•
1 2 3 4 10 11 12 13 ▼ Distribution	+ %
Distribution properties:	
Fixed number of elements	•
Number of elements:	
4	
 ▲ Mesh 1 ▲ Size № Free Tri ▲ ௵ Swept 1 Ⅲ Dist ▲ Free Tei 	ribution 1

STUDY I

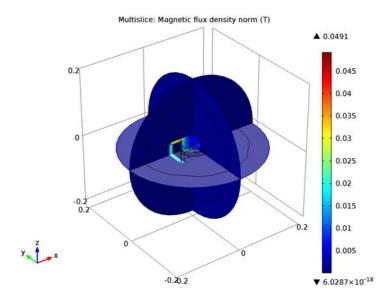
The magnetostatic model is now ready to solve.

I in the Model Builder, right-click Study I 💥 and choose Compute = .

RESULTS

Magnetic Flux Density

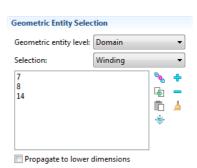
The default plot group shows the magnetic flux density norm. At this point it is important to consider whether the results make sense and to try and detect any modeling errors.



DATA SETS AND SELECTIONS

By adding Selections and adjusting the Data Sets under the **Results** node you can create more interesting plots.

- I In the Model Builder, expand the Results>Data Sets node. Right-click Solution I i and choose Duplicate in.
- Right-click Solution 2 in and choose Add Selection .
- **3** Go to the **Selection** settings window. Under **Geometric entity selection**:
 - From the Geometric entity level list, select Domain.



- From the Selection list, select Winding.
- 4 Right-click Solution I 💼 and choose Duplicate 🖃.

- 5 Right-click Solution 3 i and choose Add Selection A Selection node is added to the Model Builder.
- 6 Go to the Selection settings window. Under Geometric Entity Selection:
 - From the Geometric entity level list, select Domain.
 - From the Selection list, select Core.

3D Plot Group 2

- I In the Model Builder, right-click Results 🝙 and choose 3D Plot Group 🛅.
- 2 Right-click 3D Plot Group 2 🛅 and choose Volume 🛅.
- 3 Go to the Volume settings window. Under Data from the Data set list, select Solution 2.
- 4 Click Replace Expression **a** in the upper-right corner of the Expression section. From the menu, choose Magnetic Fields>Coil parameters>Coil voltage (mf.VCoil).
- **5** Under Coloring and Style from the Color table list, select Thermal.
- 6 In the Model Builder, right-click 3D Plot Group 2 and choose Volume . A Volume 2 node is added to the Model Builder.
 - ▲ Results
 ▷ IIII Data Sets
 ▷ 8.85 ▷ 9.800 Derived Values
 ▷ IIII Tables
 - Magnetic flux density, norm
 - a 🛅 3D Plot Group 2
 - Colume 1
- 7 Go to the **Volume** settings window. Under
 - Data from the Data set list, select Solution 3.
- 8 Click the Plot ✓ button. On the Graphics window toolbar, click the Zoom In ⓐ button twice.

🔁 Volume		- 0
🖌 Plot		2
▼ Data		
Data set:	Solution 3	-
▼ Expression		
Expression:		
mf.normB		
Unit:		
Т		•
Description	1:	
Magnetic flux	density norm	
▶ Title		

Coloring and Style

Color table

Thermal

•

-

Coloring:

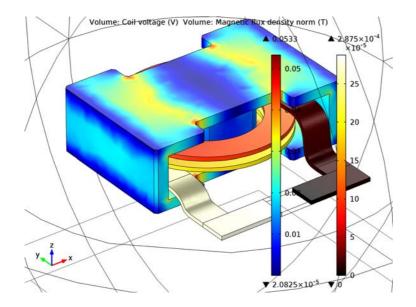
Color table:

Color legend

Wireframe

Symmetrize color range

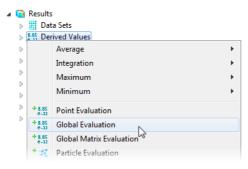




DERIVED VALUES

The coil inductance and resistance are available as predefined variables, which are displayed as follows.

I In the Model Builder under Results, right-click Derived Values and choose Global Evaluation



2 In the Global Evaluation settings window, locate the Expression section.

- 3 In the Expression edit field, enter mf.VCoil_1/mf.ICoil_1.
- 4 Click the **Evaluate** = button. The results are available in the **Results** window table located in the lower right side of the COMSOL Desktop. Or select **View>Results** if from the main menu to open the **Results** window.
- 5 In the Model Builder, right-click Derived Values 🟭 and choose Global Evaluation 🟭.
- 6 In the Global Evaluation settings window, in the Expression field, enter 2*mf.intWm/ mf.ICoil_1^2.
- 7 Click the **Evaluate** = button and compare the results in the **Results** window.

🕶 Data	
Data set:	Solution 1 🔹
 Expression 	+ - ∖
Expression: 2*mf.intWm/mf.	ICoil 142
Unit:	
Н	•
Description:	

You can also click the down arrow next to the **Evaluate** button = on the settings window to view each table. You should get about 0.29 m Ω and 0.11 mH, respectively.

🖂 Messages 📼 Progress	💷 Log 📳 Results 😫	- 8		
🔛 👯 🝐 🗙 📐 📕 🕞 🖙 🌐 🗸				
mf.VCoil_1/mf.ICoil_1 (Ω)	2*mf.intWm/mf.ICoil_1^2 (H)			
2.8747e-4	1.1469e-4			

MAGNETIC FIELDS (MF)

As can be seen in the Magnetic Flux Density plot, this is effectively contained within the core. Thus, there should be little need to use infinite elements in this model. Solve the model without the infinite elements to test this hypothesis.

- In the Model Builder under Model I, click Magnetic Fields 👧.
- 2 In the Magnetic Fields settings window, select domains 5–8 and 14 only.



STUDY I

In the Model Builder, right-click Study I 💥 and choose Compute = .

DERIVED VALUES

- In the Model Builder under Results>Derived Values, click Global Evaluation I 🟭.
 - Results
 Data Sets
 8.55 Derived Values
 8.55 Global Evaluation 1
 8.65 Global Evaluation 2
- 2 In the Global Evaluation settings window, click the Evaluate = button. The Inductance value displays in the Results window table.
- 3 In the Model Builder, click Global Evaluation 2
- 4 In the Global Evaluation settings window, click the Evaluate = button. The Resistance value displays in the Results window table. The results change very little.

MODEL WIZARD

Next, add a simple circuit to the model.

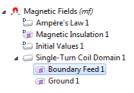
- In the Model Builder, right-click Model I 👿 and choose Add Physics 🏨.
- 2 In the Add physics tree under AC/DC, double-click Electrical Circuit (cir) 🐲 to add it to the Selected physics list. You do not need to add any studies. Click Finish 🚀.

MAGNETIC FIELDS (MF)

Change the field excitation so that it can connect to the circuit part of the model.

- 2 In the Boundary Feed settings window under Single-Turn Coil Domain, choose Circuit (current) from the Coil excitation list.

 Single-Turn Coil Domain 			
Coil name:			
1			
Coil excitation:			
Circuit (current)	-		



ELECTRICAL CIRCUIT (CIR)

Add a resistor in series with the inductor and drive. This is done for both by applying a voltage source.

Voltage Source I

In the Model Builder under Model I, right-click Electrical Circuit 🔊 and choose Voltage Source 👌.

The default settings correspond to a DC source of I V between nodes I and 0 in the circuit net. Keep these settings.

Resistor	l
----------	---

- In the Model Builder, right-click Electrical Circuit 🜮 and choose Resistor 👄.
- 2 Go to the Resistor settings window. Under Node Connections enter 1 and 2 in the Node names table as in the figure to the right.
- **3** Under **Device Parameters** in the *R* field, enter **100**[mohm].

Voltage	e Source	- 8				
		2				
▼ Node	Connections					
Label	Node names					
р	1					
n	0					
▼ Figure	•					
P + - n)					
▼ Devic	e Parameters					
Source t	ype:					
DC-sou	irce	•				
Voltage						
V _{src}	L	V				
▼ Node	Connections					
Label	Node names					
p	1					
n	2					
▼ Figure	•					
₽	<u> </u>					
	e Parameters					
Resistan						
	R 100[mohm]					

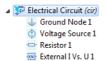
External I Vs. U I

There is a special feature for connecting the circuit to the finite elements model.

- I In the Model Builder, right-click Electrical Circuit 🜮 and choose External I Vs. U 👜.
- 2 In the External I Vs. U settings window under Node Connections, enter Node names as in to the figure to the right.
- **3** Under External Device, from the Electric potential *V* list choose Coil voltage (mf/stcdpl).

The sequence of nodes under **Electrical Circuit** should match this figure.

-10	Externa	I I Vs. U	
			2
	Node	Connections	
	Label	Node names	
	р	2	
	n	0	
	_		
	Exter	nal Device	
	Electric	potential:	
	V Coil	voltage (mf/stcdp1)	•

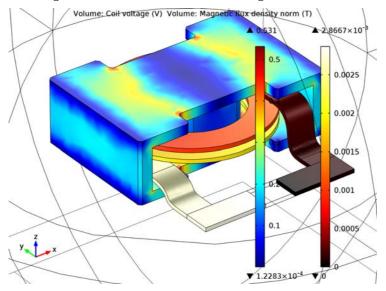


STUDY I

I In the Model Builder, right-click Study I 💥 and choose Compute = .

RESULTS

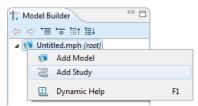
The current is now limited to approximately 10 A by the external resistor which has a much larger resistance than that of the winding.



MODEL WIZARD - ADD A SECOND STUDY

Now, set up the model for computing the frequency-dependent impedance.

In the Model Builder, right-click the top node Untitled.mph (root) and choose Add Study.



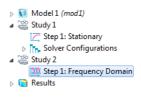
- 2 In the Select Study Type window that opens, under Studies>Preset Studies for Selected Physics click Frequency Domain [10] .
- **3** Find the **Selected physics** subsection.

4 In the Selected physics table under Solve for, click to change the check mark to an X and remove the **Selectrical Circuit (cir)** interface.

Selected p	hysics	
	Physics	Solve for
.0.	Magnetic Fields (mf)	×
20	Electrical Circuit (cir)	×

5 Click Finish 🚮.

A **Study 2** node with a **Frequency Domain** study step is added to the **Model Builder**.



DEFINITIONS

At high frequencies, the skin depth of the copper conductor in the winding becomes difficult to resolve. The solution is to exclude the interior of the copper domain from the simulation and instead represent the winding by a boundary condition, which introduces surface losses via an equivalent surface impedance. For this purpose add a boundary selection and an associated surface material.

Conductor Boundaries

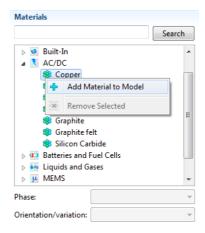
- I In the Model Builder under Model I, right-click Definitions ≡ and choose Selections>Explicit _%.
- 2 Select Domains 7, 8, and 14 only.
- 3 Go to the Explicit settings window. Under Output Entities from the Output entities list, select Adjacent boundaries.
- 4 Press F2 and choose Rename <a>.
- 5 In the Rename Explicit window enter Conductor Boundaries in the New name field. Click OK.

 Input Entities 	
Geometric entity level: Doma	ain 🔻
7 8 14	ias + in − i⊛ ⊿
 All domains Output Entities 	
Adjacent boundaries	•
Exterior boundaries	
Interior boundaries	

MATERIALS

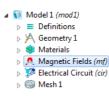
Copper (2)

- From the main menu, select View>Material Browser . In the Materials tree under AC/DC, right-click Copper and choose + Add Material to Model.
- 2 In the Model Builder, click Copper (2).
 - ▲ Materials
 ▷ Copper (mat1)
 ▷ Air (mat2)
 ▷ Core (mat3)
 ▷ Copper (2) (mat4)
- 3 Go to the Material settings window. Under Geometric Entity Selection:
 - From the Geometric entity level list, select Boundary.
 - From the Selection list, select Conductor Boundaries.



MAGNETIC FIELDS (MF)

- In the Model Builder under Model I, click Magnetic Fields 👧
- 2 Go to the Magnetic Fields settings window. Under Domain Selection from the Selection list, select Non-conducting without IE.



Ampère's Law 2

Apart from the surface loss in the copper conductor, there are also AC losses in the core. The loss in the core is introduced as an effective loss tangent. For this purpose an extra equation/constitutive relation is required.

- In the Model Builder, right-click Magnetic Fields <u>n</u> and choose Ampère's Law <u>.</u> A second Ampère's Law node is added to the Model Builder.
- 2 Go to the Ampère's Law settings window. Under Domain Selection from the Selection list, select Core.

3 Under Electric Field from the ϵ_r list, select User defined and enter 1 - 5e - 4* j in the field.

✓ Electric Field	
$\mathbf{D} = \epsilon_0 \epsilon_r \mathbf{E}$	
Relative permittivity:	
$\epsilon_{ m r}$ User defined	-
1-5e-4*j	1
Isotropic	+

Impedance Boundary Condition 1

- I In the Model Builder, right-click Magnetic Fields <u>n</u> and at the boundary level, choose Impedance Boundary Condition @.
- **2** Go to the **Impedance Boundary Condition** settings window. Under **Boundary Selection** from the **Selection** list, select **Conductor Boundaries**.

Boundary Selection					
Selection:	Conductor Boundaries			•	
23			0	÷	
24 25		=	L.	_	
25			1 2	_	
26			ĥ		
27			din.		
29					
30					
31		Ŧ			

Disable the Single-Turn Coil Domain I

The Single Turn Coil Domain does not apply to an active domain anymore so it needs to be disabled.

• In the Model Builder, under Magnetic Fields right-click Single-Turn Coil Domain I i and choose Disable @. The node is greyed out.

Lumped Port I

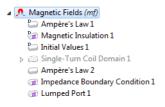
The electric potential is not available in this physics interface, so to excite the model a different boundary feature, which is more appropriate for high frequency modeling, must be used.

- In the Model Builder, right-click Magnetic Fields and at the boundary level choose Lumped Port (a). A Lumped Port node is added to the sequence in the Model Builder.
 - ▲ Magnetic Fields (mf)
 ▷ Ampère's Law 1
 ▷ Magnetic Insulation 1
 ▷ Initial Values 1
 ▷ Single-Turn Coil Domain 1
 Ampère's Law 2
 ⊘ Impedance Boundary Condition 1
 Lumped Port 1
- 2 Go to the Lumped Port settings window. Select boundaries 59–62 only.

The geometrical parameters of the boundary set need to be entered manually.

- **3** Under **Port Properties** from the **Type of port** list, select **User defined**.
 - In the h_{port} field, enter 0.024.
 - In the w_{port} field, enter **0.046**.
- 4 Specify the $\mathbf{a}_{\mathbf{h}}$ vector as in the figure to the right.
- 5 From the Terminal type list, select Current.

The Model Builder node sequence under Magnetic Fields should match this:



Boundary Selection			
Selection: Manual 👻			
59 60 61 62			• + ≥ - 〕 ↓ ©
Over	ride and Contribution		
► Equa	tion		
▼ Port	Properties		
Port na	me:		
1			
Type of	f port:		
User d	efined		•
Height	of lumped port:		
h_{port}	0.024		
Width of lumped port:			
Wport 0.046			m
Direction between lumped port terminals:			
	1	x	
\mathbf{a}_{h}	0	У	1
	0	z	
Terminal type:			
Current			

STUDY 2

Set up a frequency sweep from I-I0 MHz in steps of I MHz.

I In the Model Builder, expand the Study 2 node and click Step 1: Frequency Domain j

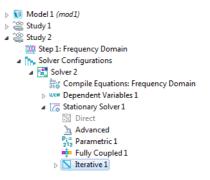
- 2 Under Study Settings, click the Range 🛄 button.
- 3 In the Range window, enter these settings:
 - In the Start field, enter 1e6.
 - In the Step field, enter 1e6.
 - In the Stop field, enter 1e7.
- 4 Click Replace.

🔯 Range	×	
Entry method:	Step 🔹	
Start:	1e6	
Step:	1e6	
Stop:	1e7	
Function to apply to all values: None 🔹		
Replace Add Cancel		

Near the resonance frequency, the problem becomes ill-conditioned. If there were no loss, it would even become singular as the field solution then would approach infinity. Thus for a high Q factor, the iterative solver may fail to converge and then a direct solver must be used. Here it is sufficient to tweak the iterative solver to use a more robust preconditioner.

Solver 2

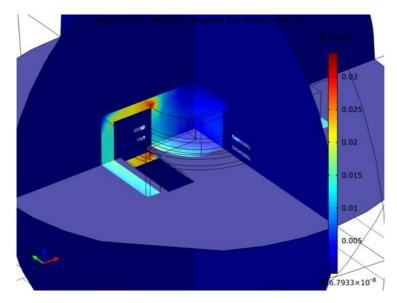
- I In the Model Builder, right-click Study 2 🎬 and choose Show Default Solver 👘.
- In the Model Builder, expand the Study 2 Solver Configurations in nodes as in the figure to the right and then click the lterative I N node.
- 3 Go to the Iterative settings window. Under General select Right from the Preconditioning list.
- 4 In the Model Builder, right-click Study 2 and choose Compute =.



RESULTS

Magnetic Flux Density

Again check the default plot for any modeling errors. Note that the magnetic flux density inside the copper winding is not computed as this domain was excluded.



Plot the surface current distribution at the lowest frequency solved for. This frequency is below resonance and the device is still of an inductive nature.

Data Sets

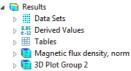
- I In the Model Builder under Results>Data Sets, right-click Solution 4 in and choose Duplicate in.
- 2 Right-click Solution 5 💼 and choose Add Selection 👒.
- **3** Go to the Selection settings window. Under Geometric Entity Selection from the Geometric entity level list, choose Boundary.
- 4 From the Selection list, choose Conductor Boundaries.

3D Plot Group 4

- I In the Model Builder, right-click Results 🝙 and choose 3D Plot Group 📬. A 3D Plot Group 4 node is added to the sequence.
- 2 Go to the 3D Plot Group settings window. Under Data from the Data set list, choose Solution 5.

▼ Data	
Data set:	Solution 5 🔹
Parameter value (freq):	10e5 🔹





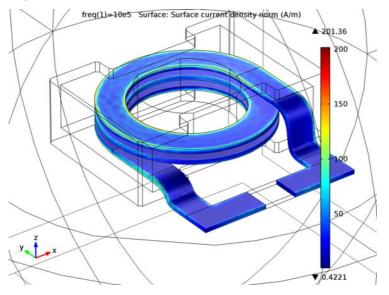
- Magnetic flux density, norm 1
- b 🛅 3D Plot Group 4

- **3** From the **Parameter value (freq)** list, choose **10e5**.
- 4 Right-click 3D Plot Group 4 🛅 and choose Surface 🛅.
- 5 Go to the Surface settings window. In the upper-right corner of the Expression section, click Replace Expression ≥.
- 6 From the menu, choose Magnetic Fields>Currents and charge>Surface current norm (mf.normJs) (when you know the variable name, as in this exercise, you can also enter mf.normJs in the Expression field).

 Expression 	÷.	
Expression:		
mf.normJs		
Unit:		
A/m		•
Description:		
Surface current norm		

7 Click the **Plot** 🗾 button.

The plot shows the surface current distribution and should match this figure.



Change to the highest frequency solved for and compare the results. Finish the modeling session by plotting the real and imaginary parts of the coil impedance.

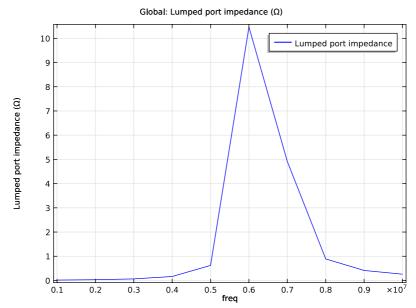
ID Plot Group 5

- I In the Model Builder, right-click Results 🕤 and choose ID Plot Group 📐.
- 2 In the ID Plot Group settings window under Data, select Solution 4 from the Data set list.
- 3 Under Results right-click ID Plot Group 5 📐 and choose Global 📐.

4 Go to the Global settings window. Under y-Axis Data in the Expression column, enter real(mf.Zport_1). In the Description column, enter Lumped port impedance.

▼ y-Axis Data		∳ ∗ \ *
Expression	Unit	Description
real(mf.Zport_1)	Ω	Lumped port impedance

Note: In general, you can click the **Replace Expression** > to see what variables are available in the predefined lists. In this case, you can enter the information directly into the table.



5 Click the **Plot** \checkmark button.

The resistive part of the coil impedance peaks at the resonance frequency.

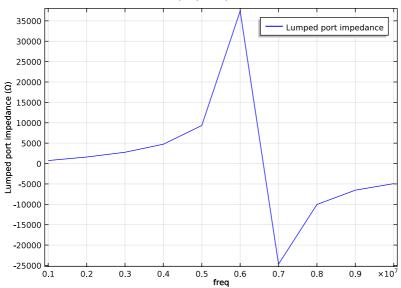
ID Plot Group 6

- I In the Model Builder, right-click Results 🕤 and choose ID Plot Group 📐.
- 2 Go to the ID Plot Group settings window. Under Data from the Data set list, select Solution 4.
- 3 Under Results right-click ID Plot Group 6 📐 and choose Global 📐.

4 Go to the Global settings window. Under y-Axis Data in the Expression column, enter imag(mf.Zport_I). In the Description column, enter Lumped port impedance.

•	y-Axis Data		
[Expression	Unit	Description
	imag(mf.Zport_1)	Ω	Lumped port impedance

5 Click the **Plot** 🗾 button.



Global: Lumped port impedance (Ω)

The reactive part of the coil impedance changes sign when passing through the resonance frequency, going from inductive to capacitive.

As a final step, pick one of the plots to use as a model thumbnail.

- I In the Model Builder under Results click 3D Plot Group 2 🛅.
- 2 From the File menu, choose Save Model Thumbnail.

To view the thumbnail image, click the **Root** node and look under the **Model Thumbnail** section. Make adjustments to the image in the **Graphics** window using the toolbar buttons until the image is one that is suitable to your purposes.

This concludes this introduction.