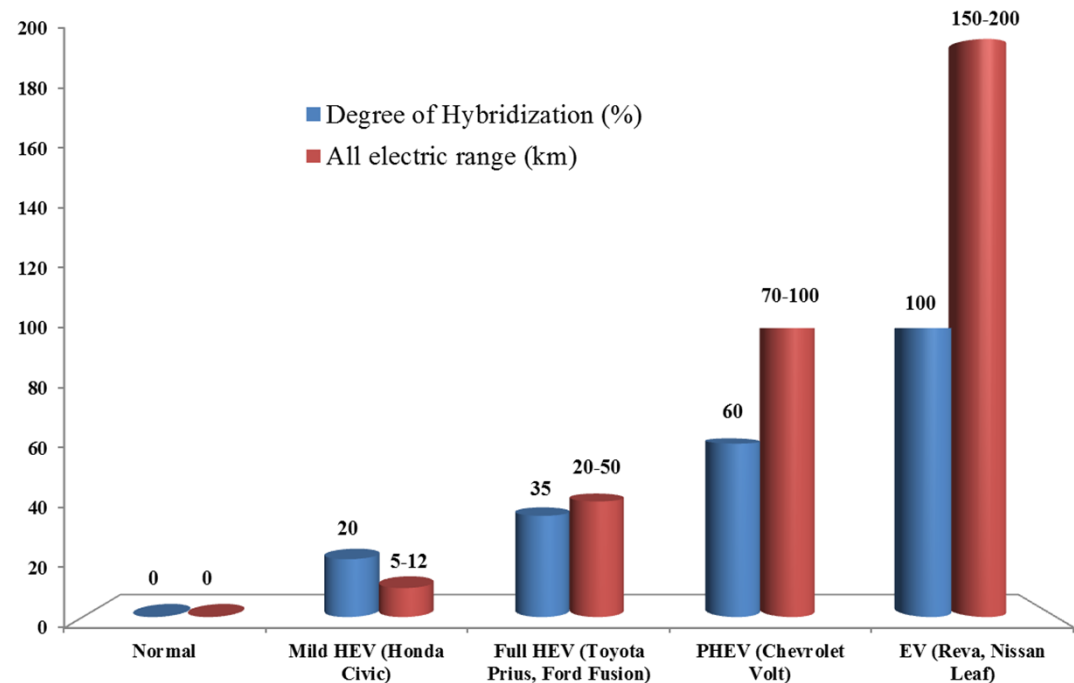
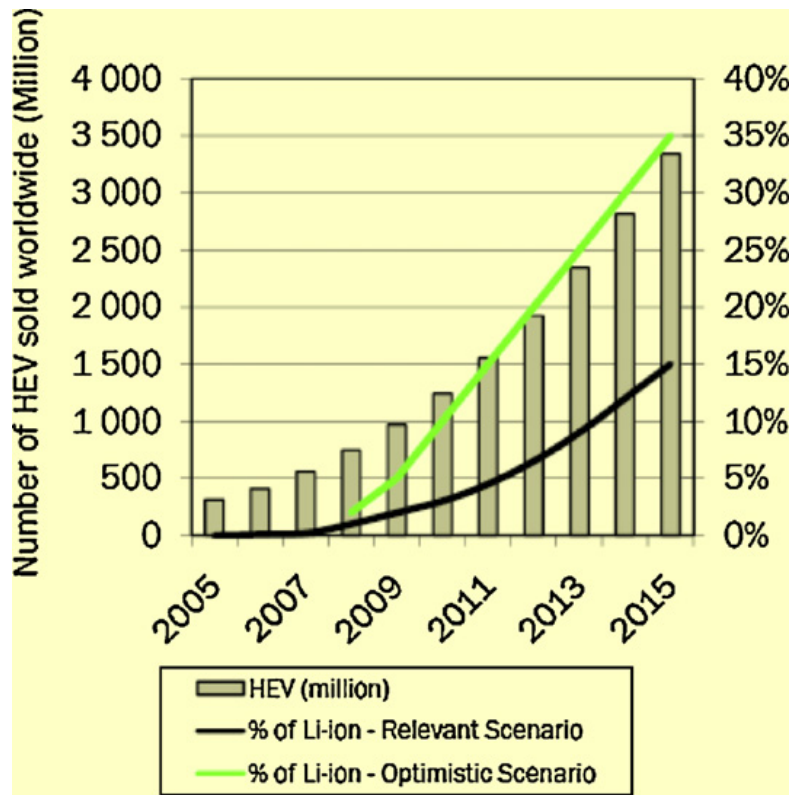




# State-of-Charge (SOC) governed fast charging method for lithium based batteries

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**CONFERENCE**  
BANGALORE2013



### References:

1. Battery Market Development: Materials Requirements and Trends 2012-2025; Christophe Pillot, Director, Avicenne Energy; Advanced Automotive Battery Technology, Application and Market Symposium 2013
2. Plug-in Hybrid and Battery-Electric Vehicles: State of the research & development and comparative analysis of energy & cost efficiency; Nemry F. et.al.; JRC ITPS technical notes



### Comparison of energy sources: Gasoline powered vs. battery powered

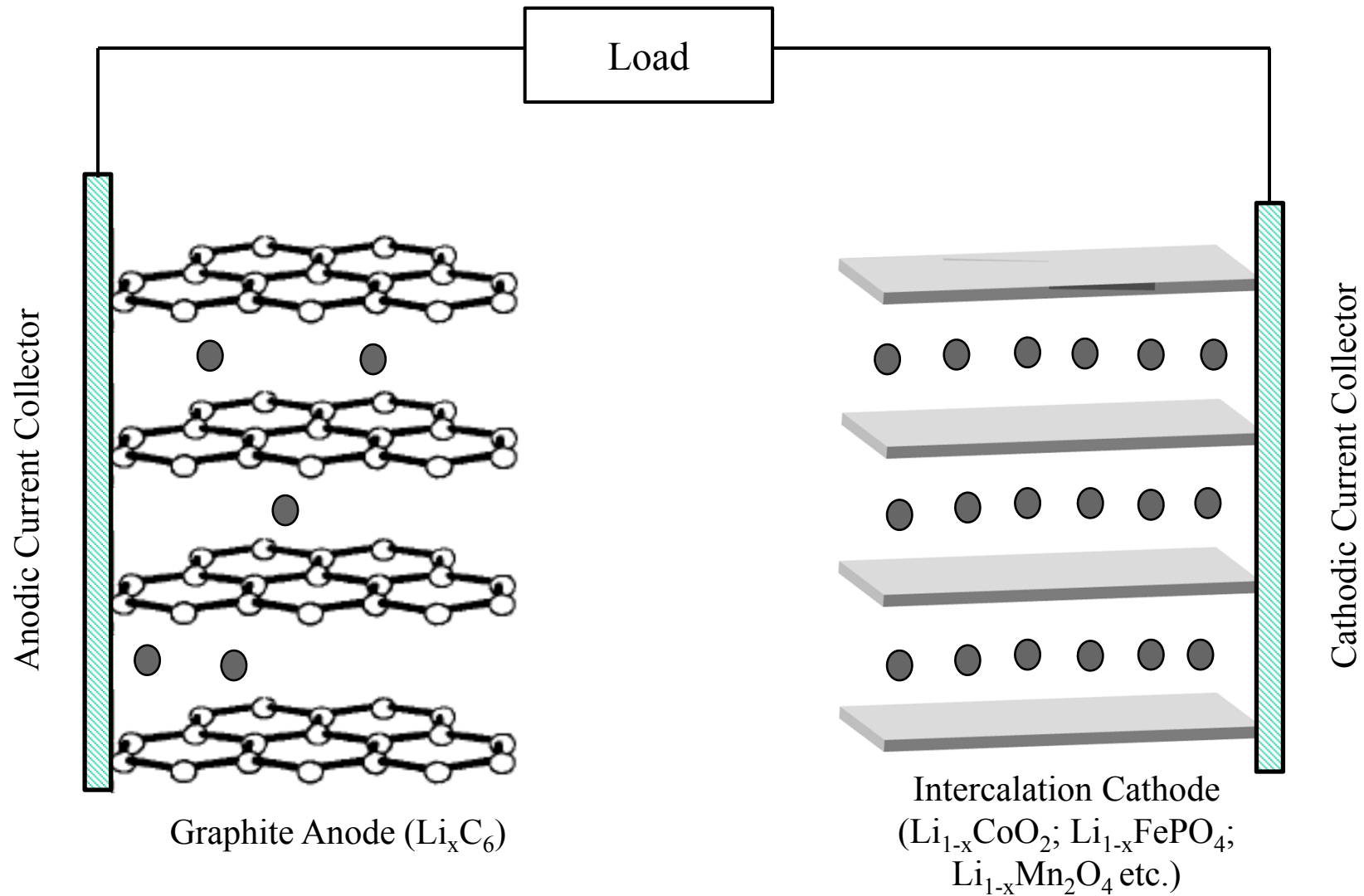
Energy Source	Energy Density <sup>1</sup> (Wh/kg)	Charging Time <sup>2</sup>	No. of Cycles
Gasoline	~ 4,000	~ 5-10 min <sup>3</sup>	N/A
Lead Acid Battery	80 - 100	4 – 6 hrs.	800-1000
Lithium Battery	400 - 500	2 – 3 hrs.	~ 2000
Fuel-cell	~ 19,000	~ 15-30 min <sup>3</sup>	N/A
Ultra-capacitor	5 - 10	0.3 – 30 s	~ 500,000

<sup>1</sup>: practical energy density based on system efficiency

<sup>2</sup>: based on widely used conventional methods

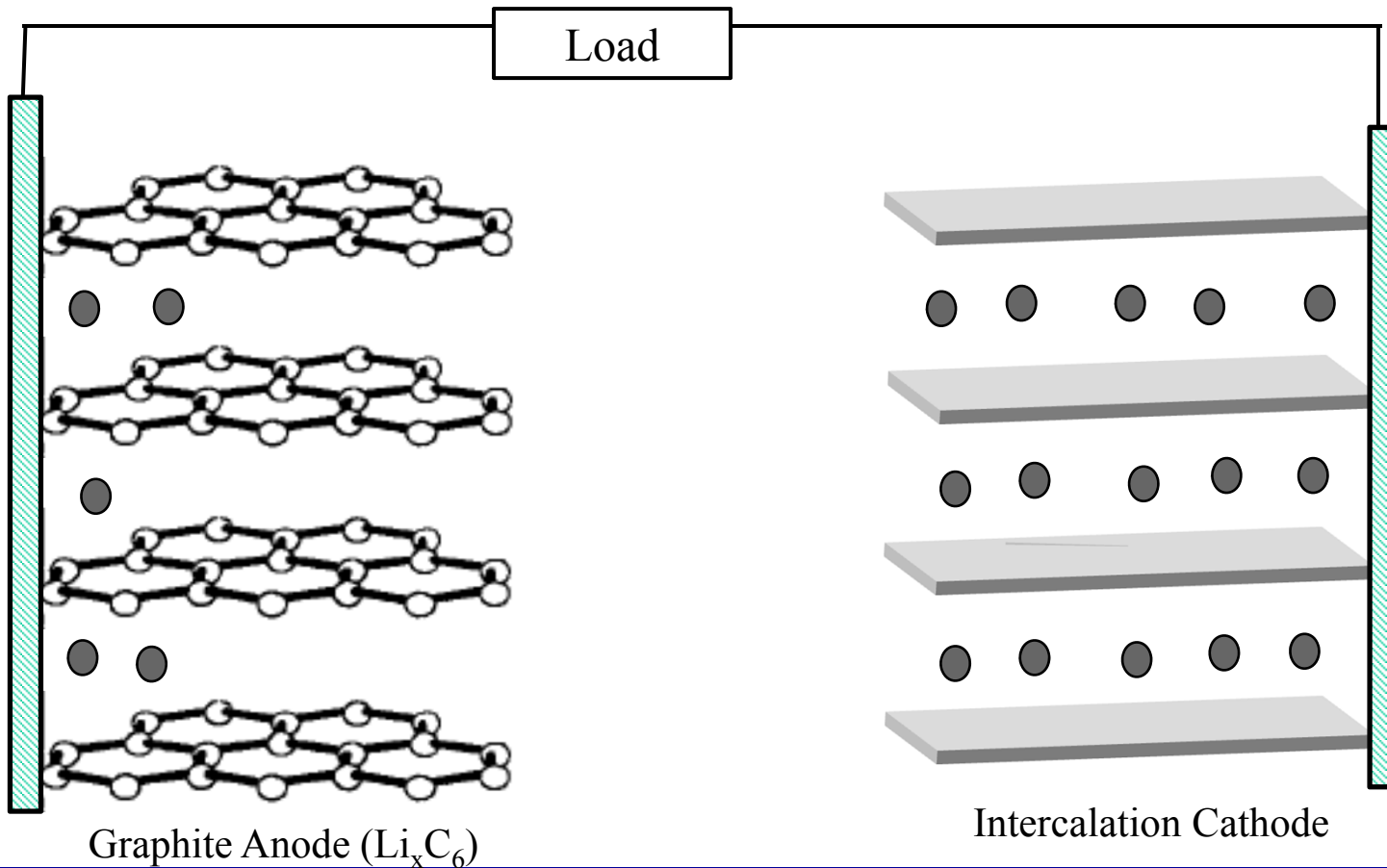
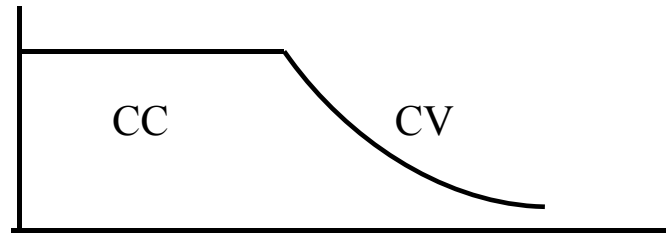
<sup>3</sup>: re-fueling time

- Conventional CC-CV algorithm takes ~2-3 hrs. to completely charge a battery

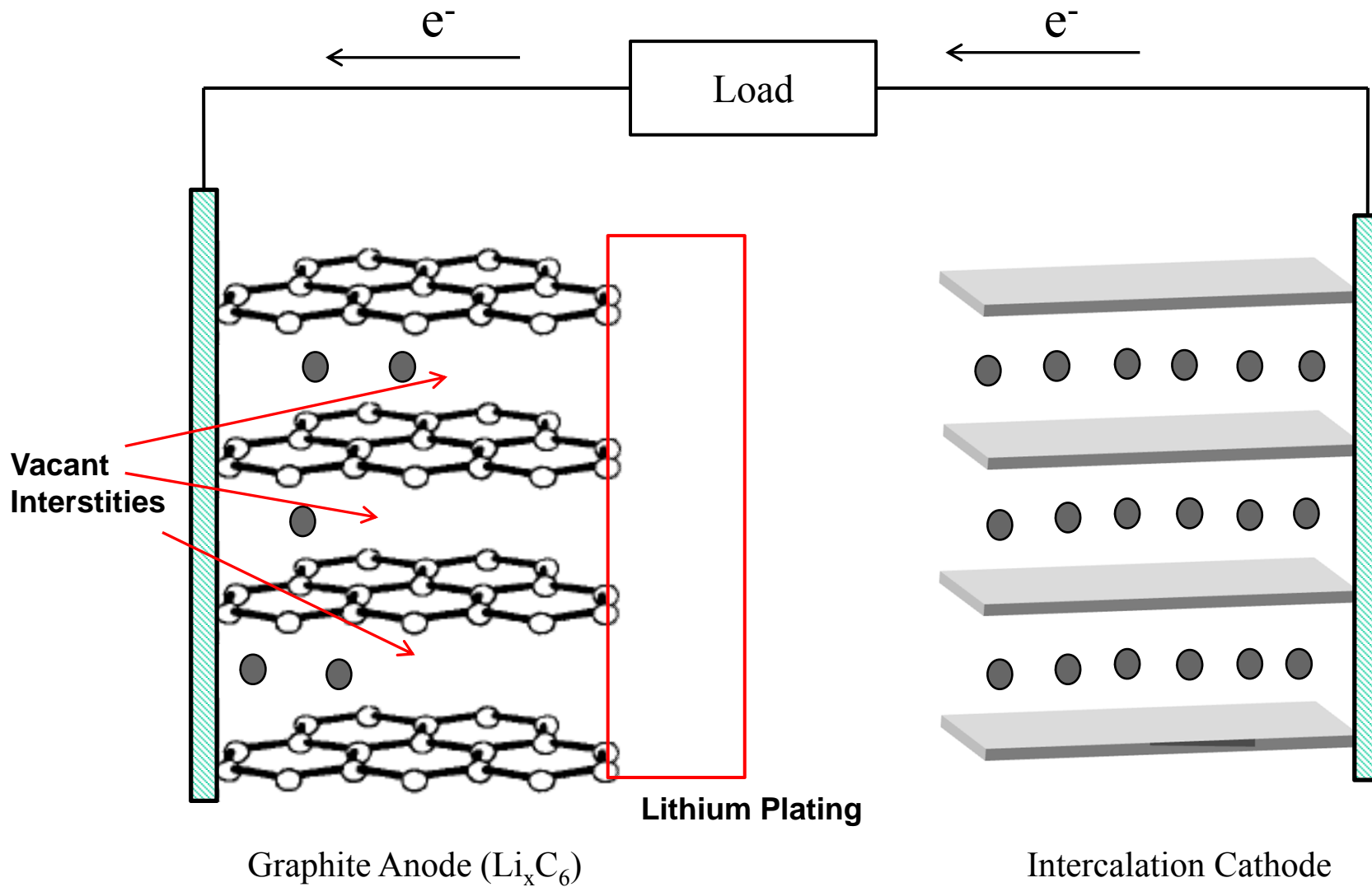




## Charging using conventional CC-CV algorithm



Fast Charging

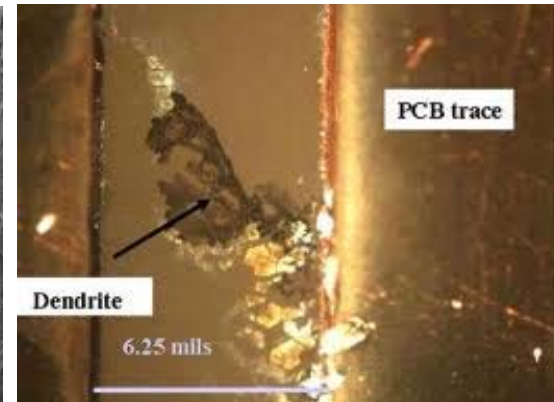




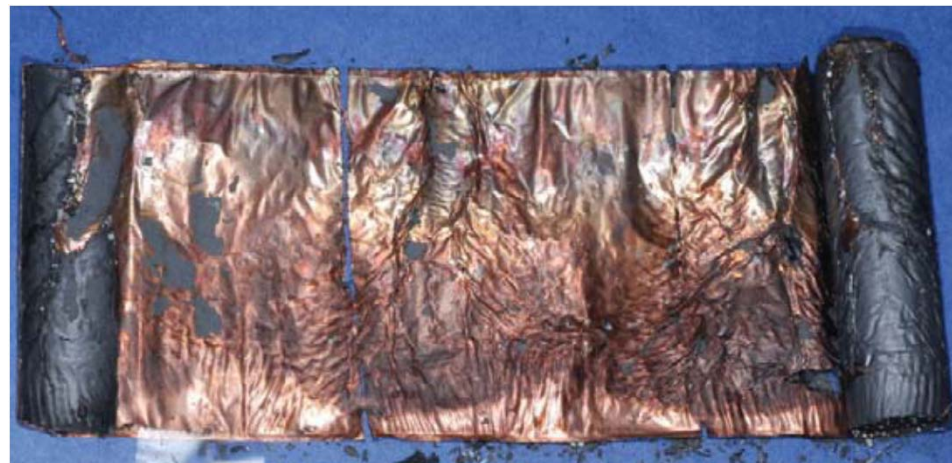
- Most fast charging methods have detrimental effect on battery life



Lithium plating on graphite  
Anode



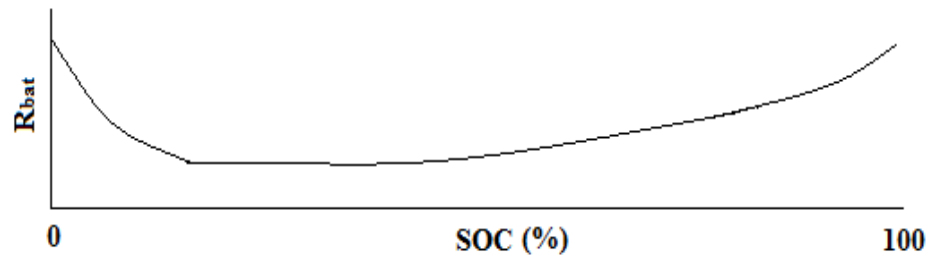
Dendrite growth



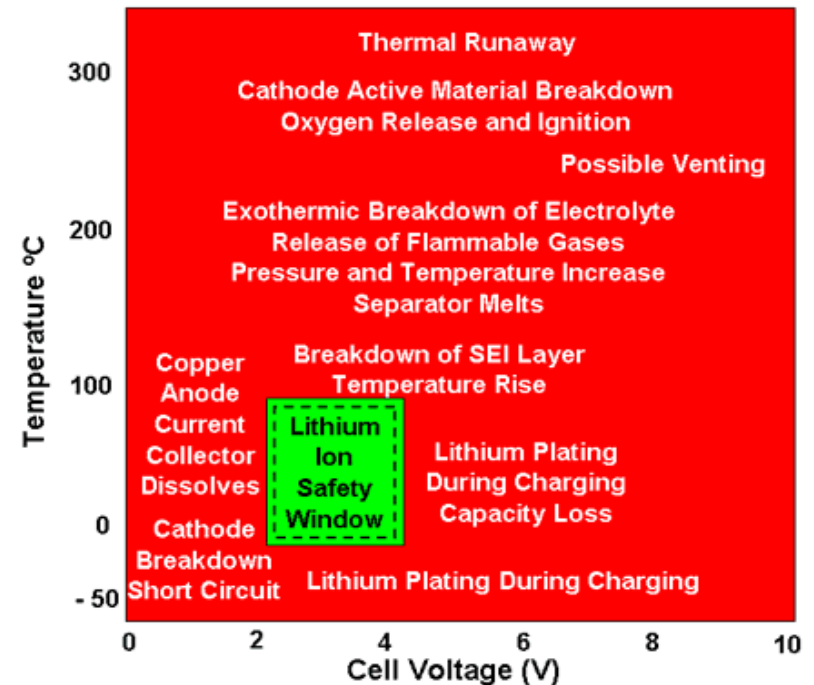
Separator puncture & Internal short-circuit due to  
dendrite growth



- ✓ SOC governed fast charging algorithm
- ✓ Different charging stages to account for the varying internal impedance
- ✓ More setting time to smoothen out conc. gradients on anode surface
- ✓ Controlled charging for better safety



### Lithium Ion Cell Operating Window



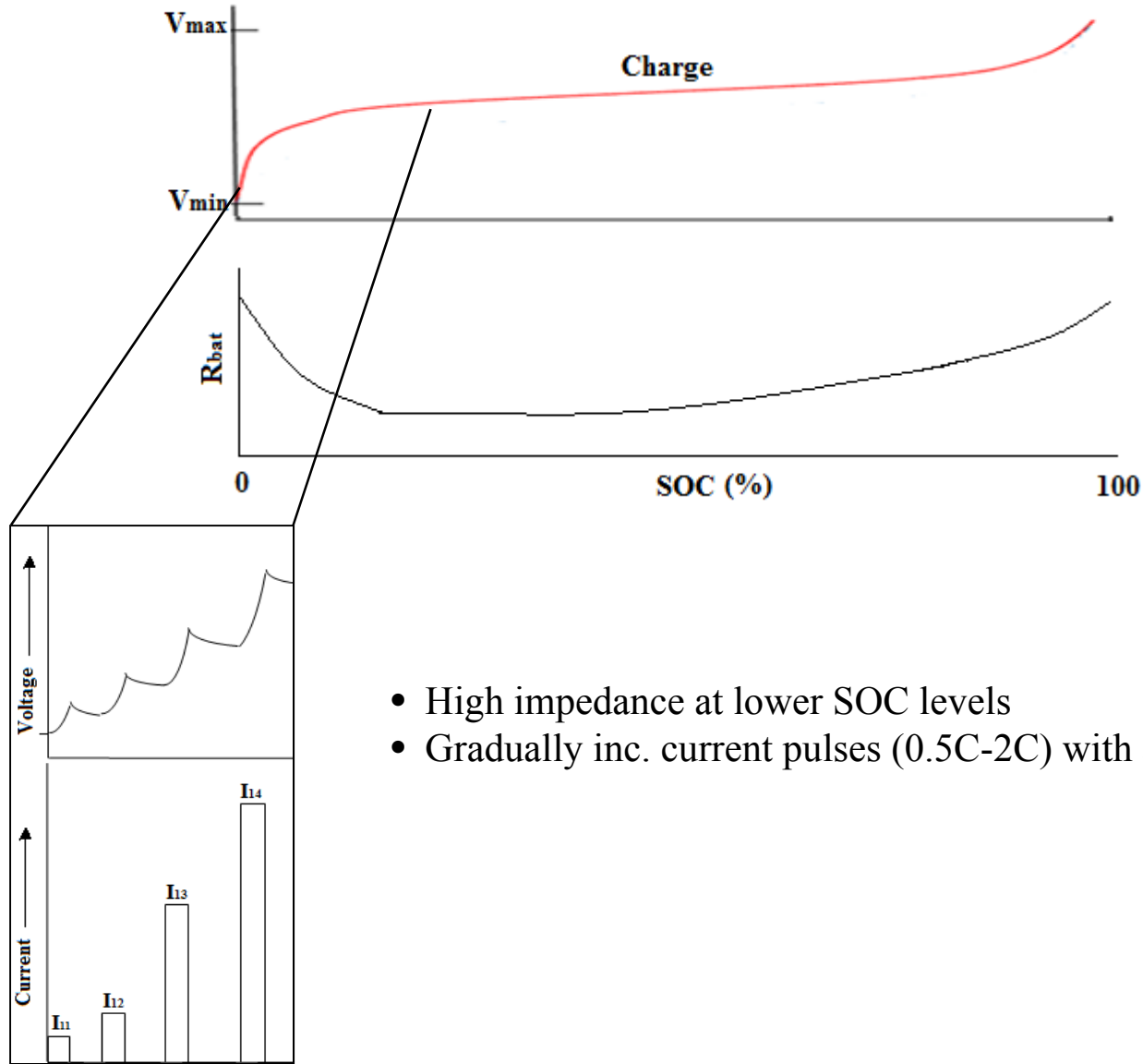
#### References:

1. Paryani et.al.; Fast charging of battery using adjustable voltage control; *US 2011/0012563 A1*; Tesla Motors Inc. (US), 2011
2. [www.electropaedia.com](http://www.electropaedia.com)





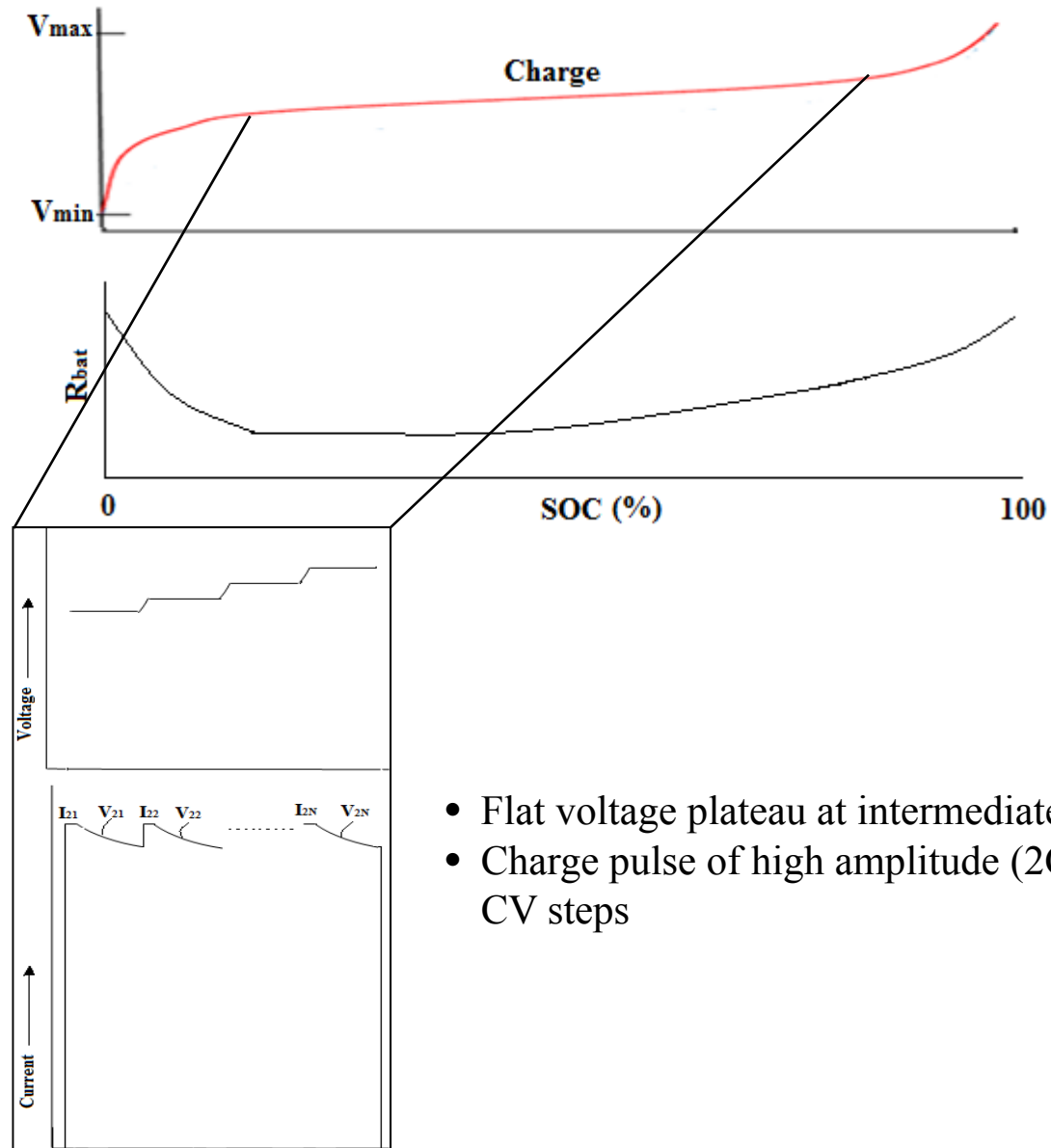
### Stage 1: Multiple CC charging ( $0 = \text{SOC} \leq 50$ )



- High impedance at lower SOC levels
- Gradually inc. current pulses (0.5C-2C) with alternate rest periods



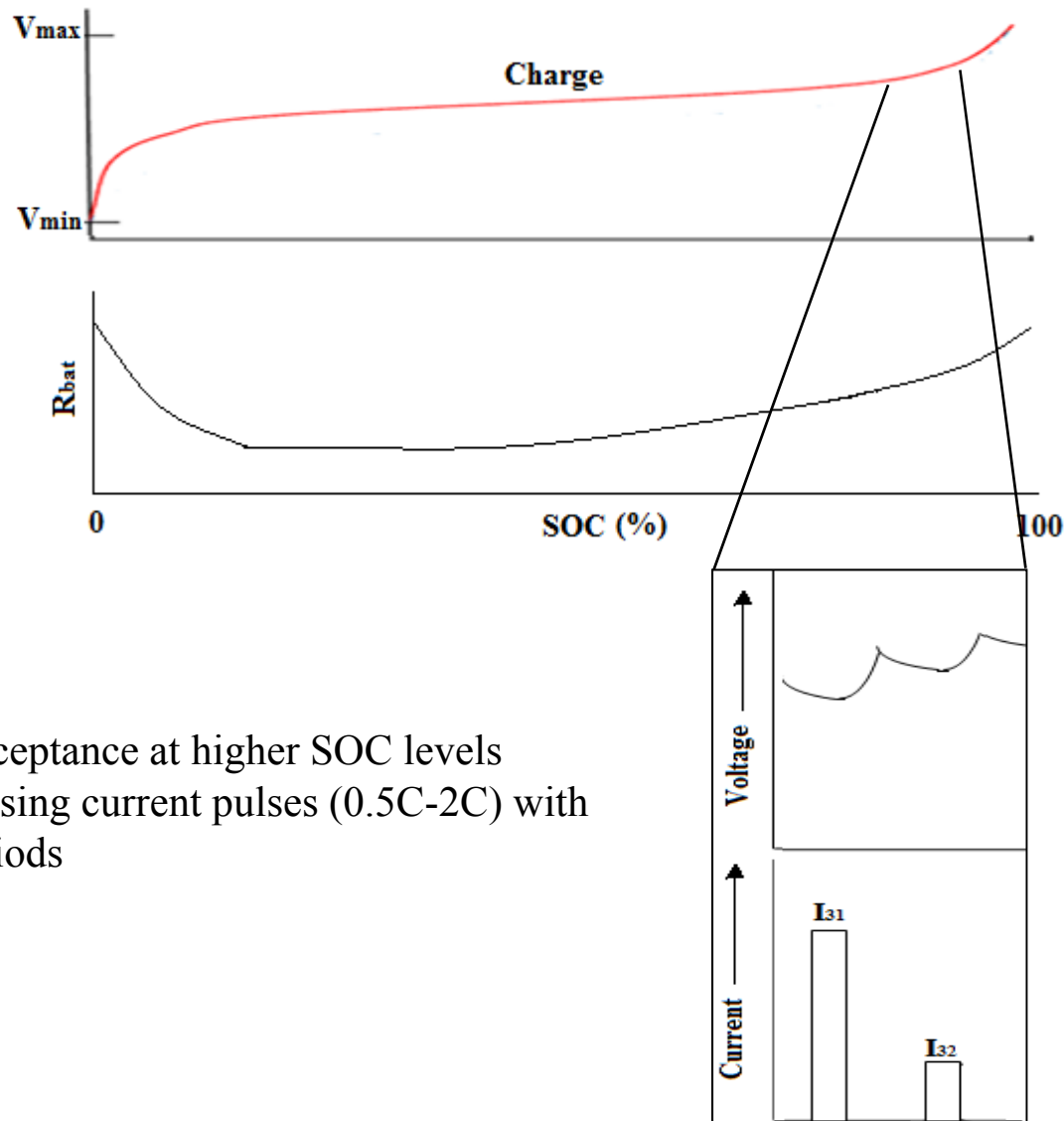
### Stage 2: Multiple CC-CV charging ( $50 \leq \text{SOC} \leq 80$ )



- Flat voltage plateau at intermediate SOC levels
- Charge pulse of high amplitude (2C-8C) with alternate CV steps



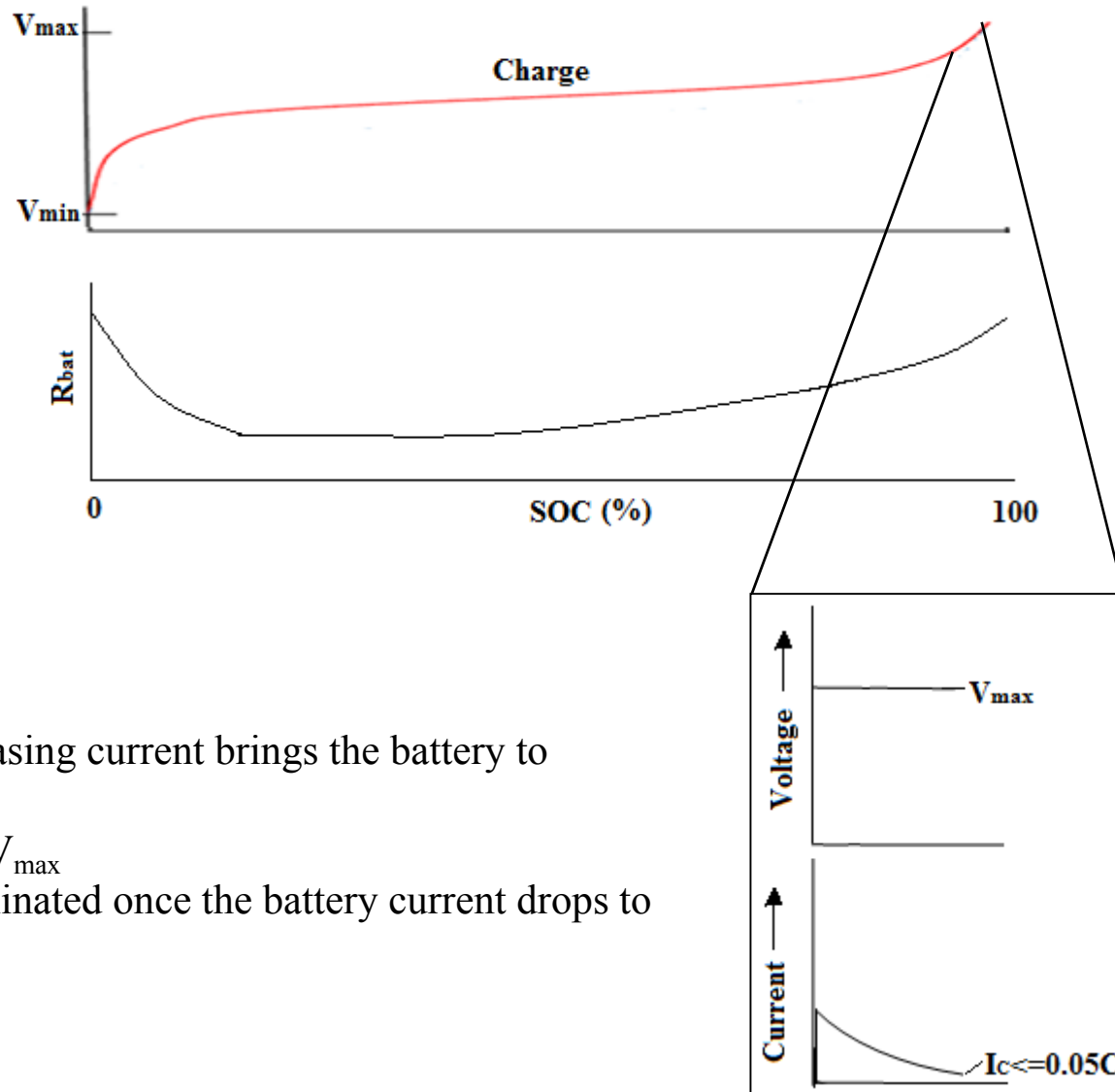
### Stage 3: Multiple CC charging ( $80 \leq \text{SOC} \leq 95$ )



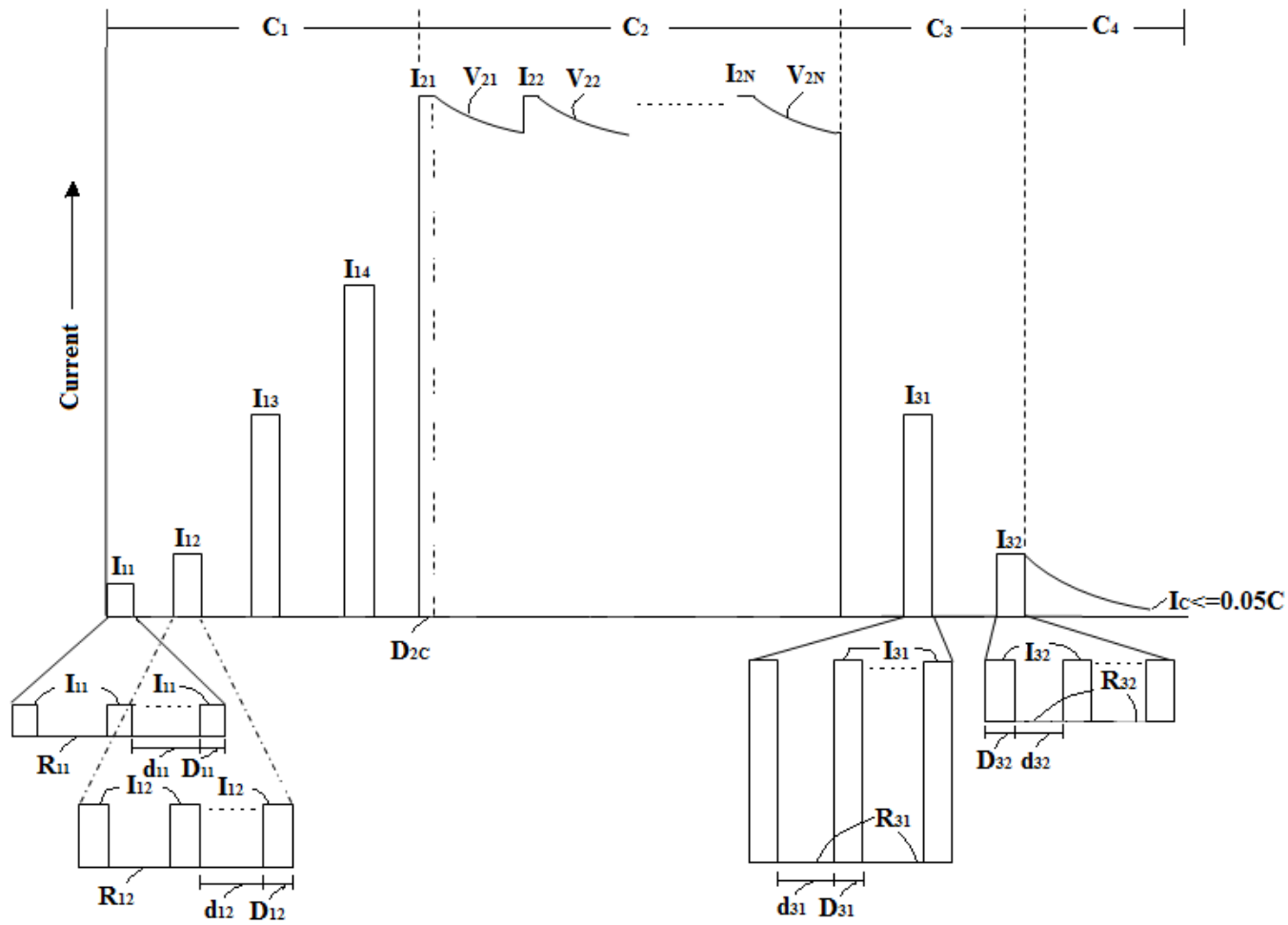
- Lower charge acceptance at higher SOC levels
- Gradually decreasing current pulses (0.5C-2C) with alternate rest periods



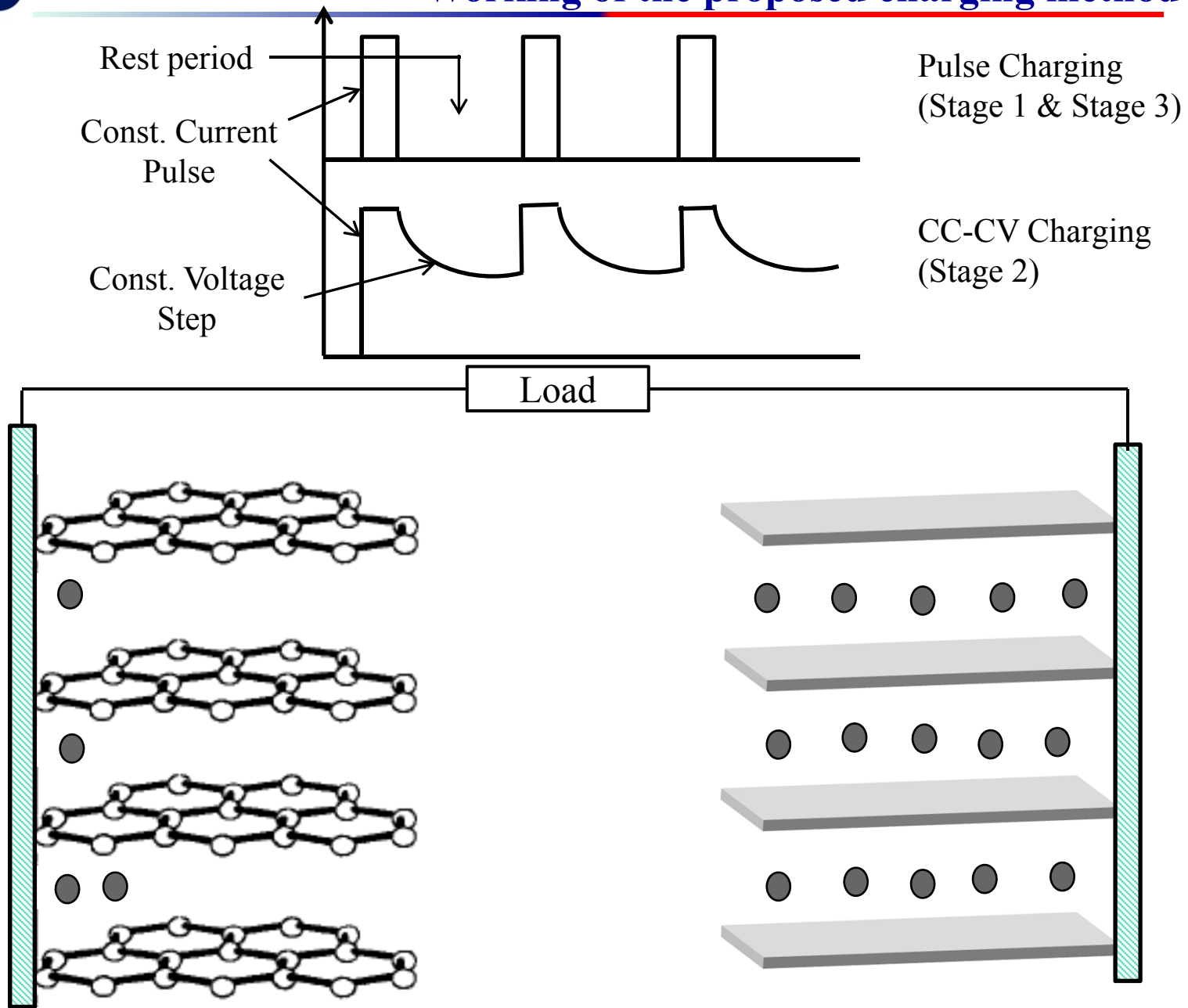
### Stage 4: CV charging ( $95 \leq \text{SOC} = 100$ )



- Gradually decreasing current brings the battery to equilibrium
- CV charging at  $V_{\max}$
- Charging is terminated once the battery current drops to 0.1-0.05C



- $C_1$ : m-CC<sub>i</sub>;       $0 = \text{SOC} < 0.5$
- $C_2$ : m-(CC-CV);     $0.5 \leq \text{SOC} < 0.80$
- $C_3$ : m-CC<sub>r</sub>;         $0.80 \leq \text{SOC} < 0.95$
- $C_4$ : CV;             $0.95 \leq \text{SOC} = 1$





➤ Cell characteristics

Cell chemistry	LiC <sub>6</sub> /LiMn <sub>2</sub> O <sub>4</sub>
Cell capacity, C	10Ah
Charge cut-off voltage, V <sub>max</sub>	4.2V
Discharge cut-off voltage, V <sub>min</sub>	3.0V
Charge cut-off current, I <sub>min</sub>	0.05C (5A)

➤ Dependent variables

Solid phase potential,  $\phi_s$

Electrolyte potential,  $\phi_l$

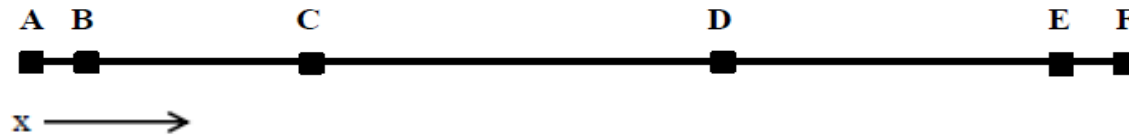
Electrolyte salt concentration,  $c_1$

➤ Material properties of the domain materials have been derived from that **Material Library**



## 1D lithium-ion battery model using “Batteries and Fuel cells module”

- Consists of 5 domains:
  - ve current collector (Copper) of length  $L_{neg\_cc}$
  - ve electrode ( $Li_xC_6$ ) of length  $L_{neg}$
  - Separator with electrolyte (1:1 EC:DEC in  $LiPF_6$  salt) of length  $L_{sep}$
  - +ve electrode ( $Li_{1-x}Mn_2O_4$ ) of length  $L_{pos}$
  - +ve current collector (Aluminum) of length  $L_{pos\_cc}$



Where,

A;  $x=0$

B;  $x=L_{neg\_cc}$

C;  $x=L_{neg\_cc}+L_{neg}$

D;  $x=L_{neg\_cc}+L_{neg}+L_{sep}$

E;  $x=L_{neg\_cc}+L_{neg}+L_{sep}+L_{pos}$

F;  $x=L_{neg\_cc}+L_{neg}+L_{sep}+L_{pos}+L_{pos\_cc}$





## Governing equations

Governing equation	Physics	Applied to	Expression
Butler-Volmer	Electrode kinetics	+ve & -ve electrodes	$J_n = \frac{i_0}{F} \left[ \exp\left(\frac{\alpha_a F \eta}{RT}\right) - \exp\left(\frac{-\alpha_c F \eta}{RT}\right) \right]$
Ohm's law (liquid phase)	Charge balance of Li <sup>+</sup> in electrolyte	Electrolyte region in separator, +ve & -ve electrodes	$i_l = -\sigma_{l,eff} \nabla \phi_l + \frac{2RT\sigma_{l,eff}}{F} \left( 1 + \frac{\partial \ln f}{\partial \ln c_l} \right) (1 - t_+^0) \nabla \ln c_l$
Ohm's law (solid phase)	Charge balance of Li <sup>+</sup> in the solid matrix	+ve & -ve electrodes	$i_s = -\sigma_{s,eff} \nabla \phi_s$
Fick's second law (liquid phase)	Diffusion in electrolyte	Electrolyte region in separator, +ve & -ve region	$\epsilon_l \frac{\partial c_l}{\partial t} = \frac{\partial}{\partial x} \left( D_{l,eff} \frac{\partial c_l}{\partial x} \right) + (1 - t_+^0) a_s J_n$
Fick's second law (solid phase)	Intercalation / diffusion of Li <sup>+</sup> into the active materials	+ve & -ve electrodes	$\frac{\partial c_s}{\partial t} = D_s \left[ \frac{\partial^2 c_s}{\partial r^2} + \frac{2}{r} \left( \frac{\partial c_s}{\partial r} \right) \right]$
Double layer capacitance	Film formation on electrode surface	+ve & -ve electrodes	$i_{dl} = \left( \frac{\partial \phi_s}{\partial t} - \frac{\partial \phi_l}{\partial t} \right) a_{dl} C_{dl}$



## Boundary conditions

Physics	Applied at	Expression
No flux condition	-ve electrode   -ve current-collector interface	$\frac{\partial c_{s,n}}{\partial x} \Big _{x=L_{neg\_cc}} = 0$
No flux condition	+ve electrode   +ve current-collector interface	$\frac{\partial c_{s,n}}{\partial x} \Big _{x=L_{neg\_cc}+L_{neg}+L_{sep}+L_{pos}} = 0$
No flux condition	Center of active material particles in +ve & -ve electrodes	$\frac{\partial c_s}{\partial r} \Big _{r=0} = 0$
Flux is equal to the rate of generation / consumption of $Li^+$ at particle surface	Surface of active material particles in +ve & -ve electrodes	$\frac{\partial c_s}{\partial r} \Big _{r=r_p} = J_n$
Electric ground	-ve electrode	$\Phi_s \Big _{x=0} = 0$
Applied current density	+ve electrode	$\Phi_s \Big _{x=L_{neg\_cc}+L_{neg}+L_{sep}+L_{pos}+L_{pos\_cc}} = -i_{app}$



## Modeling charging methods using “Events interface”

- **Explicit Event:** Occurs at predetermined times  
Can be repeatedly invoked until the desired condition is fulfilled  
C<sub>1</sub> and C<sub>3</sub> stages modeled using explicit events
- **Implicit Event:** Occurs when a condition involving an indicator state is fulfilled  
C<sub>2</sub> and C<sub>4</sub> stages modeled using implicit events
- **Discrete states:** Describes the individual steps in a load profile  
Needs to be used for both implicit and explicit events  
e.g. OCV, C1\_CC\_CH1, C1\_CC\_CH2, C2\_CC\_CH1, C2\_CV\_CH1, etc.
- **Indicator states:** Indicates the conditions that needs to be fulfilled to switch from one step to another  
To be used only for implicit events

e.g.

Step change	Condition
c2_cc_ch1_to_c2_cv_ch1	$C2\_CC\_CH1*(t-(t+20))$
c2_cv_ch1_to_c2_cc_ch2	$C2\_CV\_CH1*(SOC-(SOC+0.5))$
c2_cc_ch2_to_c2_cv_ch2	$C2\_CC\_CH2*(t-(t+50))$



## Modeling charging methods using “Events interface” (contd.)

- Applied current is defined using a global ODEs and DAEs interface  
 e.g.  $i_{C1\_1} = C1\_CC\_CH1*(i_{ch11}-i_{C1\_1}) + !C1\_CC\_CH1*i_{C1\_1}$   
 $i_{C1\_2} = C1\_CC\_CH2*(i_{ch12}-i_{C1\_2}) + !C1\_CC\_CH2*i_{C1\_2}$   
 $i_{C2} = C2\_CC\_CH1*(i_{ch2}-i_{C2}) + C2\_CV\_CH1*(E_{cell}-E_{max1}) + \dots +$   
 $!C2\_CC\_CH1*!C2\_CV\_CH1*\dots*i_{C2}$

- Shift from one stage to another depends on the SOC of the cell, given by

$$SOC = \frac{\int c_s dS}{c_{s,max}L}$$

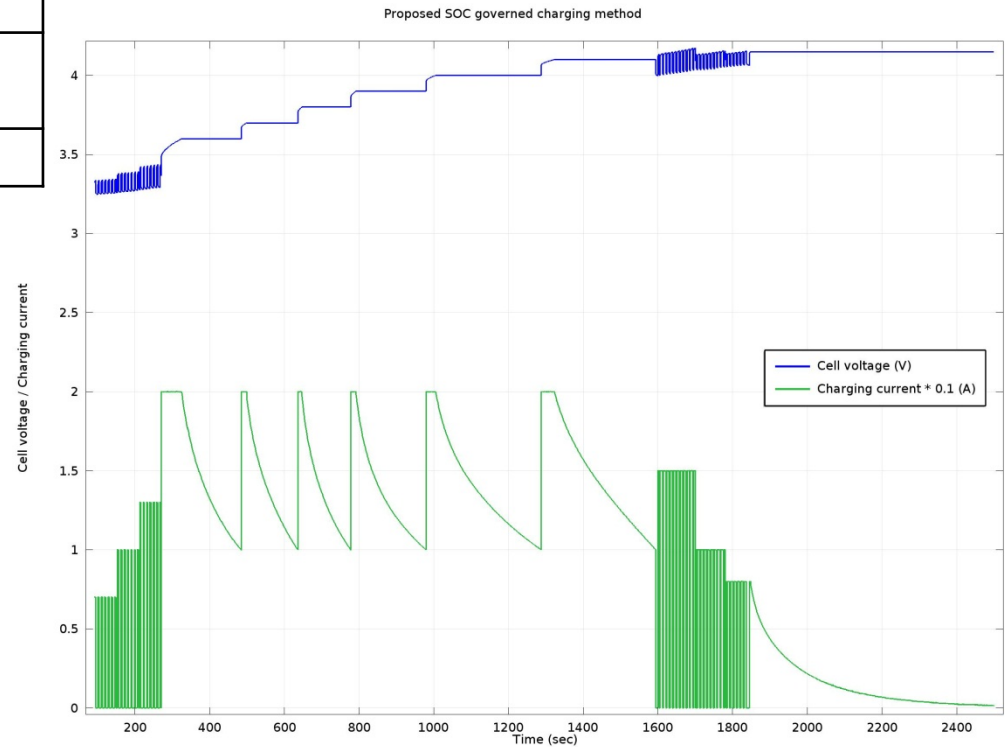
e.g.  $i_{C11} = i_{C1\_1}*(SOC < 0.3)$   
 $i_{C12} = i_{C1\_2}*(SOC > 0.3)*(SOC < 0.5)$   
 $i_{C20} = i_{C2}*(SOC > 0.5)*(SOC < 0.8)$

- Applied current is defined as  
 $i_{app} = i_{C11} + i_{C12} + \dots + i_{C20} + i_{C31} + i_{C32} + \dots + i_{C40}$



Charging stage ( $C_x$ )	Sub step ( $C_{xy}$ )	Charging current ( $i_{C_{xy}}$ )	SOC range	Charging time (s)
$C_1$	$C_{11}$	0.7C (7A)	0.2-0.3	280
	$C_{12}$	1C (10A)	0.3-0.4	
	$C_{13}$	1.3C (13A)	0.4-0.5	
$C_2$	$C_{20}$	2C (20A)	0.5-0.8	1300
$C_3$	$C_{31}$	1.5C (15A)	0.8-0.85	280
	$C_{32}$	1C (10A)	0.85-0.9	
	$C_{33}$	0.8C (8A)	0.9-0.95	
$C_4$	$C_{40}$	0.8C (8A) to 0.05C (0.5A)	0.95-1.0	640
Total charging time				2500

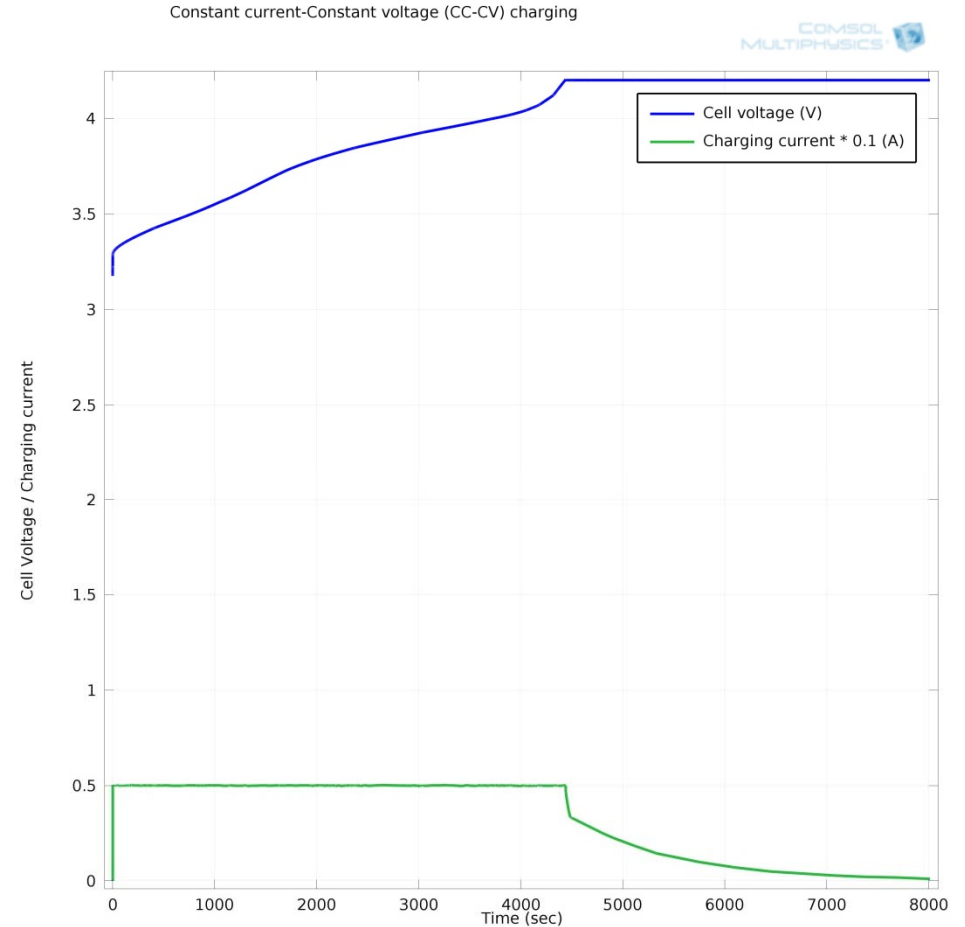
### Proposed charging method





## Constant-current constant-voltage (CC-CV) charging

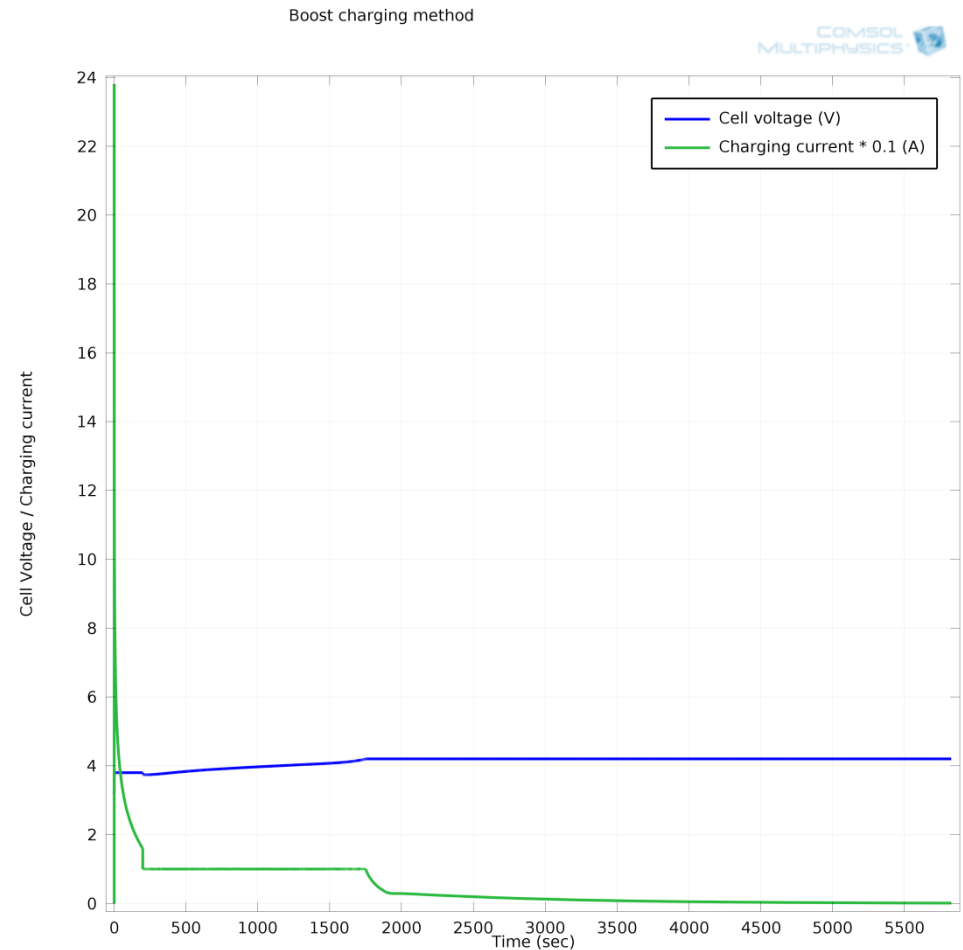
Charging stage	Charging current	Step limit	Charging time (s)
Constant current	0.5C (5A)	till the cell reaches $V_{\max}$	4460
Constant voltage	0.5C (5A) to 0.05C (0.5A)	@ $V_{\max}$ till the charging current drops to $I_{\min}$	3540
Total charging time			8000





## Boost charging

Charging stage	Charging current	Step limit	Charging time (s)
Boost charging	20C-50C (max.)	3.5 mins	210
Constant current	1C (10A)	till the cell reaches $V_{max}$	1540
Constant voltage	1C (10A) to 0.05C (0.5A)	@ $V_{max}$ till the charging current drops to $I_{min}$	3250
Total charging time			5000



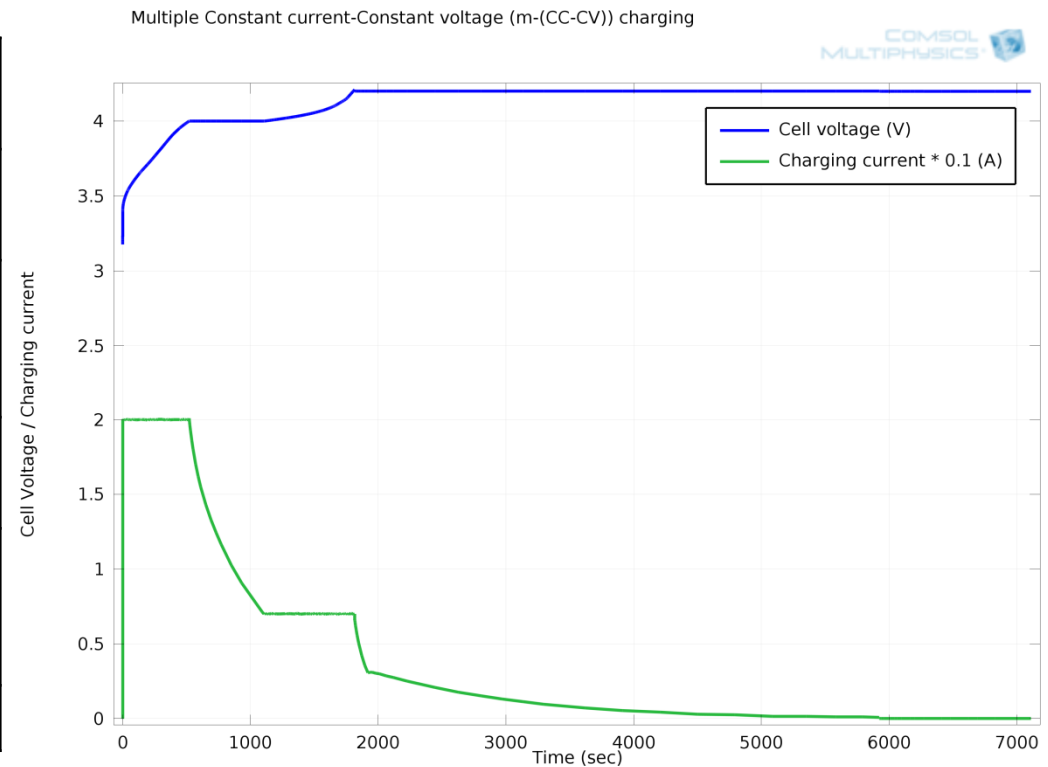
### References:

1. Notten et.al, Method and charger for boost charging a rechargeable battery on the basis of a physical model, US2010/0148731 A1, 2010
2. Notten P.H.L. et.al, Boost-charging Li-ion batteries: A challenging new charging concept, Journal of Power Sources, 145, 89-94 (2005)



## Multistage constant-current constant-voltage, m(CC-CV) charging

Charging stage	Charging current	Step limit	Charging time (s)
Constant current	2C (20A)	till the cell reaches $V_{0.8}$	550
Constant voltage	2C (10A) to 0.7C (7A)	@ $V_{0.8}$ till the charging current drops to 0.7C (7A)	550
Constant current	0.7C (7A)	till the cell reaches $V_{max}$	750
Constant voltage	0.7C (7A) to 0.05C (0.5A)	@ $V_{max}$ till the charging current drops to $I_{min}$	3600
Total charging time			5400



### References:

1. Paryani et.al, Fast charging of battery using adjustable voltage control, US2011/0012563 A1, 2011
2. Tomohisa Hagino, Pulse charging method for rechargeable batteries, US5808447, 1998





## Comparison of charging methods

- ✓ Simulation has been carried for 500 cycles
- ✓ Capacity fade as a result of cycling
- ✓ Initial capacity: 10Ah

Charging method	Charging time (s)	Cell capacity after 500 cycles (Ah)	Capacity fade (%)
CC-CV	8000	9.06	9.4%
m(CC-CV)	5400	8.63	13.7%
Boost	5000	8.42	15.8%
Proposed SOC based	2500	8.96	10.4%



## Advantages of the present method

- ✓ Faster charging
- ✓ Lower capacity fade
- ✓ Lower safety risks due to controlled charging

## Future work

- ✓ Inclusion of side reaction (e.g. SEI formation)
- ✓ Temperature performance
- ✓ 3D modeling to visualize current density distribution on electrode surface



## Queries

