## Balanced Patch Antenna for 6 GHz

## Introduction

Patch antennas are becoming more common in wireless equipment, like wireless LAN access points, cellular phones, and GPS handheld devices. The antennas are small in size and can be manufactured with simple and cost-effective techniques. Due to the complicated relationship between the geometry of the antenna and the electromagnetic fields, it is difficult to estimate the properties of a certain antenna shape. At the early stages of antenna design the engineer can benefit a lot from using computer simulations. The changes in the shape of the patch are directly related to the changes in radiation pattern, antenna efficiency, and antenna impedance.

Balanced antennas are fed using two inputs, resulting in less disturbances on the total system through the ground. Balanced systems also provide a degree of freedom to alter antenna properties, by adjusting the phase and magnitude of the two input signals. Figure 1 shows the antenna that this example simulates.


Figure 1: A photo of the real antenna that the model extracts the properties for.

## Model Definition

The patch antenna is fabricated on a printed circuit board (PCB) with a relative dielectric constant of 5.23 (Ref. 1). The entire backside is covered with copper, and the front side
has a pattern as shown in Figure 2 below.


Figure 2: The patch antenna. The $P C B$ is has a side length of 50 mm and a thickness of 0.7 mm . The centered printed square is 10 mm by 10 mm , the smaller rectangles are 5.2 mm by 3.8 mm , the thicker lines are 0.6 mm wide, and the thinner lines are 0.2 mm by 5.2 mm .

The coaxial cables have an outer conductor with an inner diameter of 4 mm and a center conductor with a diameter of 1 mm . The gap between the conductors is filled with a material with a dielectric constant of 2.07 , giving a characteristic impedance close to $58 \Omega$. There are two coaxial cables feeding the patch antenna from two sides. In this example, the signals in the cables have the same magnitude but are shifted 180 degrees in phase. This results in a balanced feed.

The entire antenna is modeled in 3D. The time-harmonic nature of the signals makes it possible to solve the vector-Helmholtz equation for the electric field everywhere in the geometry,

$$
\nabla \times\left(\mu^{-1} \nabla \times \mathbf{E}\right)-k_{0}^{2} \varepsilon_{\mathrm{r}} \mathbf{E}=0
$$

where $k_{0}$ is the wave number for free space and is defined as

$$
k_{0}=\omega \sqrt{\varepsilon_{0} \mu_{0}}
$$

All metallic objects are defined as perfect electric conductors. The antenna is placed in a spherical air domain surrounded by a Perfectly Matched Layer (PML) serving to absorb
the radiation from the antenna with a minimum of reflection. In addition, a scattering boundary condition is added outside the PML to further reduce the reflection.

The model is run through a range of frequencies surrounding the operational frequency of 6.28 GHz .

Results and Discussion


Figure 3: The patch antenna with the electric field plotted both on its surface and on a slice through the air domain. The surrounding PML is hidden from view.

Figure 3 shows the distribution of the electric field norm on the surface of the antenna and in the air, at 6.26 GHz . Most of the energy radiates out from the central patch.

The Lumped Port boundary condition, which is applied to the coaxial cables, is mimicking a connection to a transmission line feed with a characteristic impedance, $Z_{\text {ref }}$. The incident voltage wave from the transmission line has an amplitude equal to $V_{0}$, part of which is reflected directly at the port depending on how well $Z_{\text {ref }}$ matches the characteristic impedance of the coaxial cable.

Under these circumstances and from each coaxial cable, the theoretical maximum power that can be produced in the antenna is achieved when the antenna impedance matches that of the coaxial cable. This power evaluates to

$$
P_{\max }=\frac{V_{0}^{2}}{2 Z_{\mathrm{ref}}}
$$

where $V_{0}$ is the peak value of the time-harmonic applied voltage.
The antenna efficiency $\eta$ is defined as the fraction of the theoretical max power that actually radiates out of the antenna:

$$
\eta=\frac{P_{1}+P_{2}}{2 P_{\max }}
$$

where $P_{1}$ and $P_{2}$ are the net power flow through ports 1 and 2 respectively. In Figure 4 this efficiency is plotted against the frequency, showing that the optimum operating frequency is located at 6.26 GHz .

Efficiency


Figure 4: The antenna efficiency as a function of the frequency.

```
Application Library path: RF_Module/Antennas/patch_antenna
```


## Notes About the COMSOL Implementation

This example uses a mesh resulting in almost 500,000 complex-valued degrees of freedom. It therefore needs a little bit more than 2 GB of memory and should be solved on a 64 -bit platform. You can make it solve on a 32 -bit computer with a coarser mesh, but the results are less accurate.

Possible model extensions include the addition of an external circuit or a far-field computation.

## Reference

1. E. Recht and S. Shiran, "A Simple Model for Characteristic Impedance of Wide Microstrip Lines for Flexible PCB," Proceedings of IEEE EMC Symposium 2000, pp. 1010-1014, 2000.

## Modeling Instructions

From the File menu, choose New.

## NEW

In the New window, click Model Wizard.

## MODEL WIZARD

I In the Model Wizard window, click 3D.
2 In the Select Physics tree, select Radio Frequency>Electromagnetic Waves, Frequency Domain (emw).

3 Click Add.
4 Click Study.
5 In the Select Study tree, select Preset Studies>Frequency Domain.
6 Click Done.

## GLOBAL DEFINITIONS

## Parameters

I On the Home toolbar, click Parameters.
2 In the Settings window for Parameters, locate the Parameters section.
3 In the table, enter the following settings:

| Name | Expression | Value | Description |
| :---: | :---: | :---: | :---: |
| Vo | 1 [V] | IV | Applied voltage |
| epsilonr_coax | 2.07 | 2.07 | Relative permittivity, coaxial cable |
| epsilonr_pcb | 5.23 | 5.23 | Relative permittivity, circuit board |
| a_coax | $0.5[\mathrm{~mm}$ ] | $5 \mathrm{E}-4 \mathrm{~m}$ | Inner coax conductor radius |
| b_coax | $2[\mathrm{~mm}]$ | 0.002 m | Inner radius of outer coax conductor |
| Z_coax | ```sqrt(mu0_const/ (epsilonr_coax* epsilon0_const)) /(2*pi)* log(b_coax/ a_coax)``` | 57.77 ת | Cable impedance |
| Pmax | V0^2/(2*Z_coax) | 0.008655 W | Theoretical max power |
| f_min | 6.2[GHz] | 6.2E9 Hz | Minimum frequency |
| f_max | 6.3[GHz] | 6.3E9 Hz | Maximum frequency |

GEOMETRY I

## Import I (impl)

I On the Home toolbar, click Import.
2 In the Settings window for Import, locate the Import section.
3 Click Browse.
4 Browse to the application's Application Libraries folder and double-click the file patch_antenna.mphbin.

## 5 Click Import.

The imported geometry consists of the patch antenna and its connectors. Add two concentric spheres, one for the air surrounding the antenna and one for the PML.

## Sphere I (sphl)

I On the Geometry toolbar, click Sphere.
2 In the Settings window for Sphere, locate the Size section.
3 In the Radius text field, type 0.06.
4 Click to expand the Layers section. In the table, enter the following settings:

| Layer name | Thickness (m) |
| :--- | :--- |
| Layer 1 | 0.02 |

## 5 Click Build All Objects.

6 Click the Wireframe Rendering button on the Graphics toolbar.
7 Click the Zoom Extents button on the Graphics toolbar.

## DEFINITIONS

Perfectly Matched Layer I (pmll)
I On the Definitions toolbar, click Perfectly Matched Layer.
Activate the PML in the volume covered by the outer but not the inner sphere:
2 Select Domains 1-4 and 13-16 only.
3 In the Settings window for Perfectly Matched Layer, locate the Geometry section.
4 From the Type list, choose Spherical.

## ADD MATERIAL

I On the Home toolbar, click Add Material to open the Add Material window.
2 Go to the Add Material window.
3 In the tree, select Built-In>Air.
4 Click Add to Component in the window toolbar.

## MATERIALS

On the Home toolbar, click Add Material to close the Add Material window.

## Material 2 (mat2)

I In the Model Builder window, under Component I (compl) right-click Materials and choose Blank Material.

2 In the Settings window for Material, type Coax Dielectric in the Label text field.
3 Locate the Geometric Entity Selection section. From the Selection list, choose Manual.

## 4 Click Clear Selection.

Select the cylinders between the inner and outer conductors of the coaxial cables:
5 Select Domains 7 and 11 only.
6 Locate the Material Contents section. In the table, enter the following settings:

| Property | Name | Value | Unit | Property <br> group |
| :--- | :--- | :--- | :--- | :--- |
| Relative permittivity | epsilonr | epsilonr_ <br> coax | I | Basic |
| Relative permeability | mur | 1 | I | Basic |
| Electrical conductivity | sigma | 0 | $\mathrm{~S} / \mathrm{m}$ | Basic |

## Material 3 (mat3)

I Right-click Materials and choose Blank Material.
2 In the Settings window for Material, type PCB in the Label text field.
Select the PCB board:
3 Select Domain 9 only.
4 Locate the Material Contents section. In the table, enter the following settings:

| Property | Name | Value | Unit | Property <br> group |
| :--- | :--- | :--- | :--- | :--- |
| Relative permittivity | epsilonr | epsilonr_ <br> pcb | I | Basic |
| Relative permeability | mur | 1 | I | Basic |
| Electrical conductivity | sigma | 0 | S/m | Basic |

## ELECTROMAGNETIC WAVES, FREQUENCY DOMAIN (EMW)

By default, the Electromagnetic Waves equation is active in all domains. However, because you represent the metal in this model as perfectly conductive boundaries, there is no need to model the interior of the contacts. Therefore, remove the metal domains from the domains selection.

I In the Model Builder window, under Component I (compl) click Electromagnetic Waves, Frequency Domain (emw).

2 In the Settings window for Electromagnetic Waves, Frequency Domain, locate the Domain Selection section.

## 3 Click Clear Selection.

## 4 Click Paste Selection.

5 In the Paste Selection dialog box, type 1-5, 7, 9, 11, 13-16 in the Selection text field.
6 Click OK.
7 In the Settings window for Electromagnetic Waves, Frequency Domain, locate the Physics-Controlled Mesh section.

8 Select the Enable check box.
Control the meshing by the maximum frequency. This will set the maximum mesh size to 0.2 wavelengths or smaller.

9 From the Maximum mesh element size control parameter list, choose Frequency.
10 In the Maximum frequency text field, type f_max.
II Locate the Analysis Methodology section. From the Methodology options list, choose Fast.

## Lumped Port I

I On the Physics toolbar, click Boundaries and choose Lumped Port.
To define the first port, select the outer air/dielectric boundary on the cable facing the $x$ direction:

2 Select Boundary 16 only.
3 In the Settings window for Lumped Port, locate the Lumped Port Properties section.
4 From the Type of lumped port list, choose Coaxial.
5 From the Wave excitation at this port list, choose On.
6 In the $V_{0}$ text field, type $V 0$.
7 Locate the Settings section. In the $Z_{\text {ref }}$ text field, type $Z_{-}$coax.

## Lumped Port 2

I On the Physics toolbar, click Boundaries and choose Lumped Port.
The second port is the outer air/dielectric boundary on the contact facing the $y$ direction:

2 Select Boundary 96 only.
3 In the Settings window for Lumped Port, locate the Lumped Port Properties section.
4 From the Type of lumped port list, choose Coaxial.
5 From the Wave excitation at this port list, choose On.
6 In the $V_{0}$ text field, type Vo.
7 In the $\theta_{\text {in }}$ text field, type pi.

8 Locate the Settings section. In the $Z_{\text {ref }}$ text field, type $Z_{-} c o a x$.
Although you have not yet specified any conducting boundaries, there is already a Perfect Electric Conductor condition in the model. By default, it applies to all boundaries that are exterior to the active domains. It then gets over-ridden by any other conditions that you are applying. If you click its node in the Model Builder, you can see that it still applies to the conductors.

## Perfect Electric Conductor I

The patch and the PCB ground plane are interior to the model domain (meaning they neighbor only to domains where the equation is active) and hence need to be explicitly assigned this same condition.

## Perfect Electric Conductor 2

I On the Physics toolbar, click Boundaries and choose Perfect Electric Conductor.
Select the patch and the ground plane (bottom surface) of the PCB:
2 Select Boundaries 59 and 69 only.
The settings that you have made until now completely define the physics of your model. To enable postprocessing of the antenna efficiency, you need to add integral operators on the port boundaries.

## DEFINITIONS

## Variables I

I On the Home toolbar, click Variables and choose Local Variables.
2 In the Settings window for Variables, locate the Variables section.
3 In the table, enter the following settings:

| Name | Expression | Unit | Description |
| :--- | :--- | :--- | :--- |
| P1 | $0.5^{*}$ real(emw.Vport_1* <br> conj(emw.Iport_1)) | W | Power into Port 1 |
| P2 | 0.5*real(emw.Vport_2* <br> conj(emw.Iport_2)) | W | Power into Port 2 |
| eff | $($ P1+P2)/(2*Pmax) |  | Antenna efficiency |

The power that goes through each of the ports is computed from port voltage and current. The last variable defines the efficiency as the ratio of the input power and the theoretical maximum for each port.

## MESH I

I In the Model Builder window, under Component I (compl) click Mesh I.
2 In the Settings window for Mesh, click Build All.

## STUDY I

Step I: Frequency Domain
I In the Settings window for Frequency Domain, locate the Study Settings section.
2 In the Frequencies text field, type range (f_min, (f_max-f_min)/5, f_max).
This gives you 6 linearly spaced frequencies between 6.2 and 6.3 GHz . If you want to reproduce the plot in Figure 4 and are prepared to let the model run for a while, try range(6.0e9,0.01e9,6.5e9) instead.

3 On the Home toolbar, click Compute.

## RESULTS

## Electric Field (emw)

The default plot shows a slice plot of the electric field norm at 6.3 GHz . It is dominated by the result near the antenna. Most of the remaining part of these model instructions will guide you towards an informative and nice-looking plot of the local electric field on and around the antenna. But first, take the following steps in order to plot the antenna efficiency versus the frequency.

ID Plot Group 2
I On the Home toolbar, click Add Plot Group and choose ID Plot Group.
2 In the Settings window for 1D Plot Group, click to expand the Title section.
3 From the Title type list, choose Manual.
4 In the Title text area, type Efficiency.
5 Locate the Plot Settings section. Select the $\mathbf{x}$-axis label check box.
6 In the associated text field, type Frequency ( Hz ).

## Global I

I On the ID Plot Group 2 toolbar, click Global.
2 In the Settings window for Global, click Replace Expression in the upper-right corner of the $\boldsymbol{y}$-axis data section. From the menu, choose Component I>Definitions>Variables>eff - Antenna efficiency.

3 Click to expand the Legends section. Clear the Show legends check box.

4 On the ID Plot Group 2 toolbar, click Plot.


The plot has sharp edges because you solved only for 6 frequencies. See Figure 4 for a smoother version over a wider frequency range.

## Data Sets

In order to prepare for the 3D plot, define selections of the domains, boundaries, and edges that you want the plot to include. As everything is included per default, you will make these selections with the purpose of hiding what you do not select.

## Study I/Solution I (soll)

In the Model Builder window, expand the Data Sets node, then click Study I/Solution I (soll).

## Selection

I On the Results toolbar, click Selection.
2 In the Settings window for Selection, type Physical Domain in the Label text field.
3 Locate the Geometric Entity Selection section. From the Geometric entity level list, choose Domain.

## 4 Click Paste Selection.

5 In the Paste Selection dialog box, type 5-12 in the Selection text field.
6 Click $\mathbf{0 K}$.

Study I/Solution I (2) (sol I)
On the Results toolbar, click More Data Sets and choose Solution.

## Selection

I On the Results toolbar, click Selection.
2 In the Settings window for Selection, type Physical Boundaries in the Label text field.
3 Locate the Geometric Entity Selection section. From the Geometric entity level list, choose Boundary.

4 Click Paste Selection.
5 In the Paste Selection dialog box, type 13-106, 114-121, 131-144 in the Selection text field.

6 Click OK.

Study I/Solution I (3) (sol I)
On the Results toolbar, click More Data Sets and choose Solution.

## Selection

I On the Results toolbar, click Selection.
2 In the Settings window for Selection, type Physical Edges in the Label text field.
3 Locate the Geometric Entity Selection section. From the Geometric entity level list, choose Edge.

## 4 Click Paste Selection.

5 In the Paste Selection dialog box, type 10-235, 243-264, 278-335 in the Selection text field.

6 Click OK.

## Electric Field (emw)

The plot group you just selected already contains a slice plot of the electric field norm. Note that because it uses the data set for which you defined the domain selection, the plot does not show up in the PML.

## Multislice

Delete the multislice plot and add a single slice.
I In the Model Builder window, expand the Electric Field (emw) node.
2 Right-click Multislice and choose Delete.
Electric Field (emw)
In the Model Builder window, under Results right-click Electric Field (emw) and choose Slice.

Slice I
I In the Settings window for Slice, locate the Plane Data section.
2 From the Plane list, choose $\mathbf{z x}$-planes.
3 In the Planes text field, type 1.
4 Click to expand the Range section. Select the Manual color range check box.
5 In the Minimum text field, type 0.
6 In the Maximum text field, type 500.
7 Locate the Coloring and Style section. From the Color table list, choose Thermal.
8 On the Electric Field (emw) toolbar, click Plot.
You are now looking at a nicely scaled plot of the electric field norm on a slice of your geometry, excluding the PML where it does not have any physical relevance.

## Electric Field (emw)

Right-click Electric Field (emw) and choose Surface.

## Surface I

I In the Settings window for Surface, locate the Data section.
2 From the Data set list, choose Study I/Solution I (2) (soll).
3 On the Electric Field (emw) toolbar, click Plot.
The electric field norm now also shows up on the surface of the antenna. All exterior surfaces are hidden from view, but the edges defining the contour of the PML are still visible.

## Electric Field (emw)

I In the Model Builder window, under Results click Electric Field (emw).
2 In the Settings window for 3D Plot Group, locate the Plot Settings section.
3 Clear the Plot data set edges check box.
4 On the Electric Field (emw) toolbar, click Plot.
Now all edges are gone. This makes the contours of the PCB and the contacts less prominent. To retain a sharper-looking geometry, draw your selected edges in black with the help of a line plot.

## Line I

I Right-click Results>Electric Field (emw) and choose Line.
2 In the Settings window for Line, locate the Data section.
3 From the Data set list, choose Study I/Solution I (3) (soll).

4 Locate the Expression section. In the Expression text field, type 1.
5 Locate the Coloring and Style section. From the Coloring list, choose Uniform.
6 From the Color list, choose Black.
7 On the Electric Field (emw) toolbar, click Plot.
Electric Field (emw)
I In the Model Builder window, under Results click Electric Field (emw).
2 In the Settings window for 3D Plot Group, click to expand the Title section.
3 From the Title type list, choose Manual.
4 In the Title text area, type Electric field norm (V/m).
5 On the Electric Field (emw) toolbar, click Plot.
6 Click the Go to Default 3D View button on the Graphics toolbar.
7 Click the Zoom In button on the Graphics toolbar.
Your plot should now look like that in Figure 3.

