

Quasielectrostatic Induction on Stationary Vehicles under High Voltage Power Lines

Jon Leman, P.E.
Rob Schaerer, P.E.





The National Electrical Safety Code [®] states:

*“For voltages exceeding 98 kV ac to ground, either the clearances shall be increased or the electric field, or the effects thereof, shall be reduced by other means as required to **limit the steady-state current due to electrostatic effects to 5 mA** if the largest anticipated truck, vehicle, or equipment under the line were short-circuited to ground.”*

| Current (60 Hz) | Physiological Effect |
|-----------------|--------------------------------|
| 0.5-1 mA | Threshold of perception |
| 10-20 mA | Sustained muscular contraction |
| >100 mA | Ventricular fibrillation |

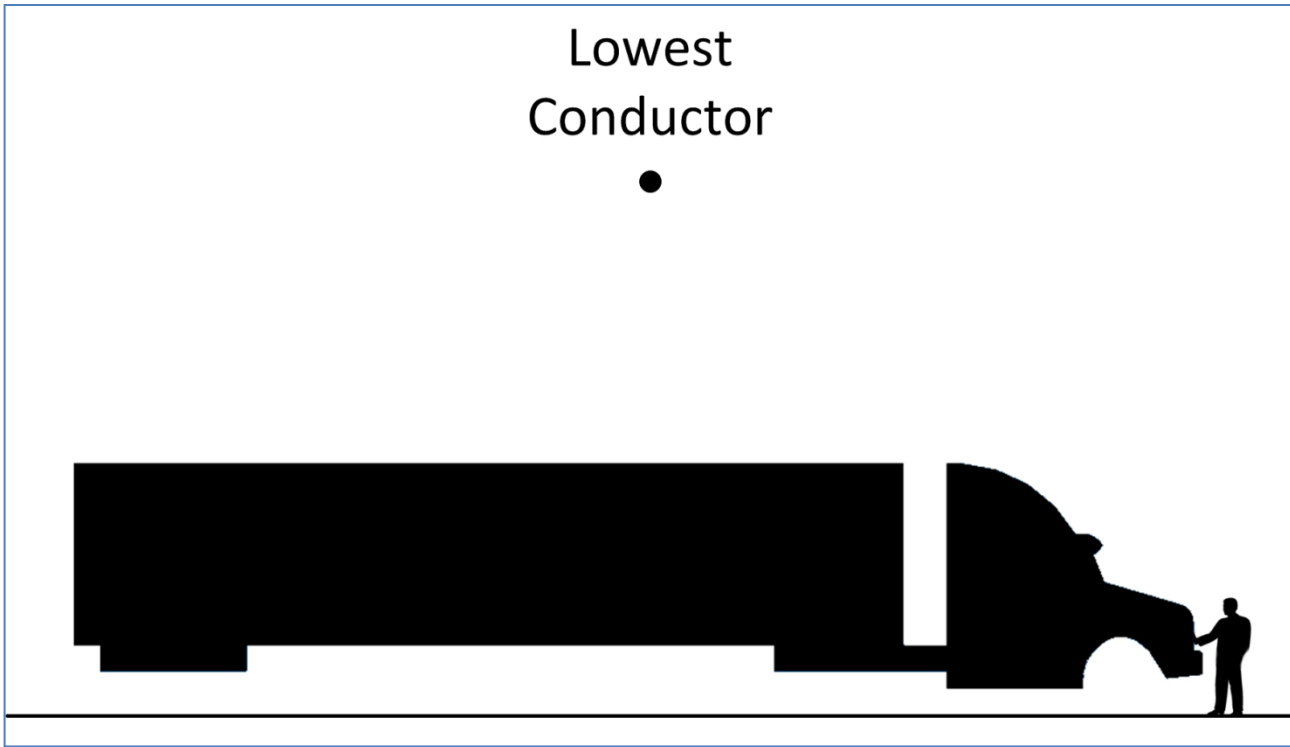
Lowest
Conductor



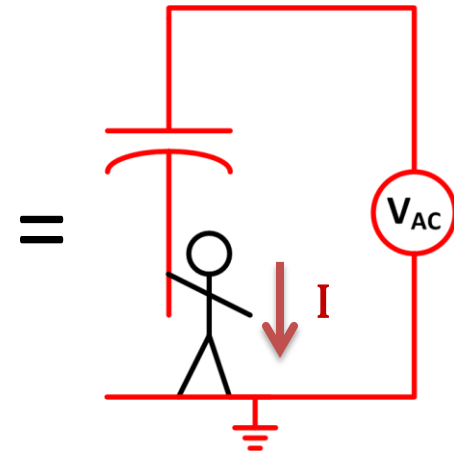
Lowest
Conductor



Lowest
Conductor

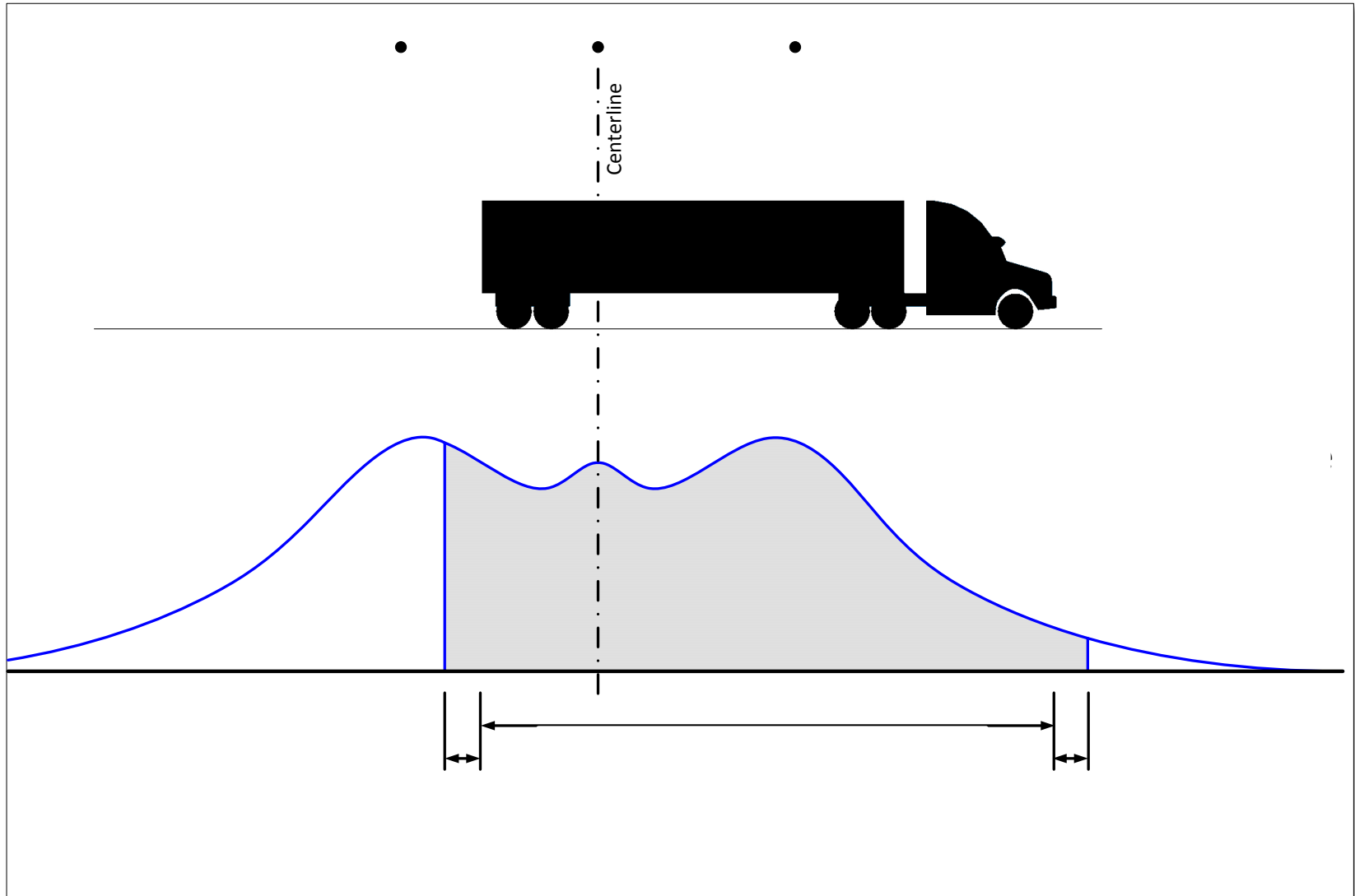


Lowest
Conductor



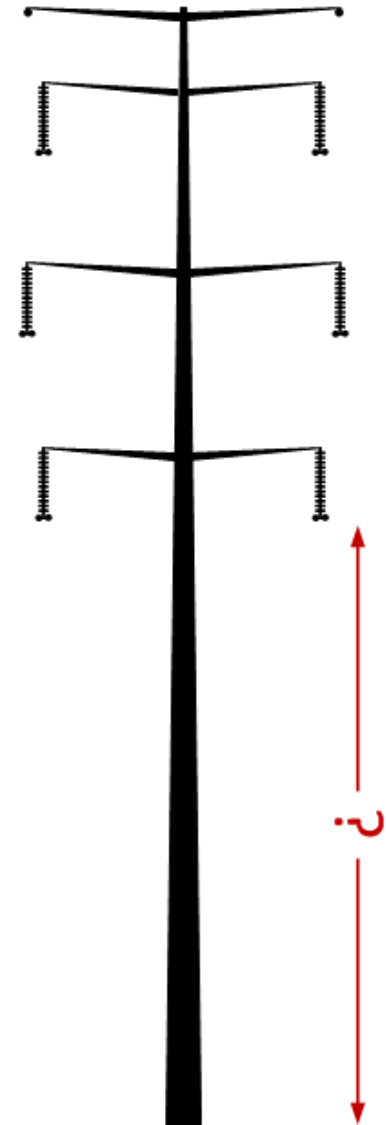
$$I < 5 \text{ mA}$$

SEMI-EMPIRICAL APPROACH



Cost vs. Electrical Clearances

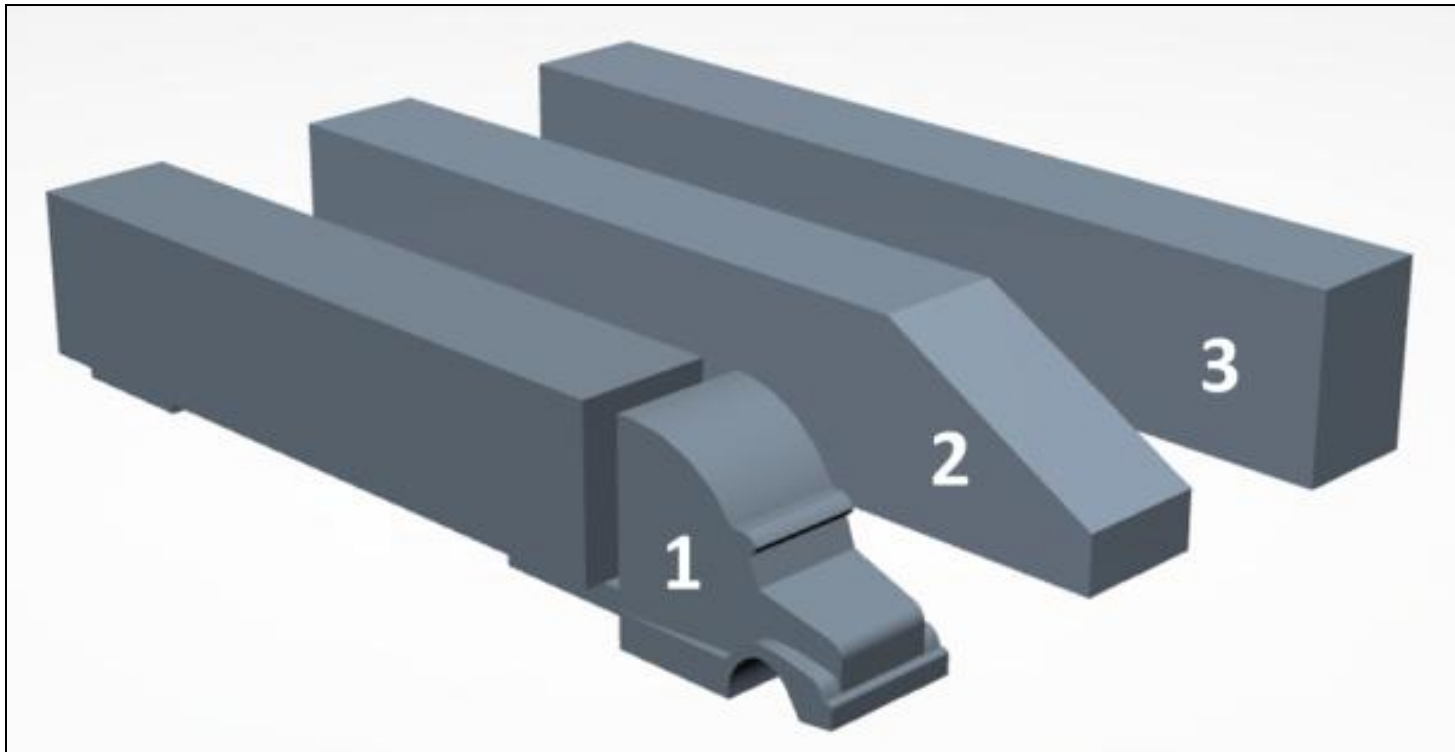
Need to understand
assumptions in order to
optimize the design!



Key Characteristics:

1. Transmission line allows 2D analysis, but **vehicle requires 3D**
2. ELF AC voltages and currents => **Electric Currents Interface**
3. Steady state 60 Hz => **Frequency domain**
4. Ground and vehicle body are assumed to be very good conductors with charge relaxation times much smaller than a 60 Hz period (hence classification as quasistatic).

| Equation | Summary |
|---|---|
| $E = -\nabla V$ | Relationship between electric potential and electric fields |
| $\nabla \cdot \mathbf{E} = \frac{\rho}{\epsilon_0}$ | Gauss' Law: Electric flux through a surface is proportional to the enclosed charge |
| $\mathbf{n} \cdot (\epsilon_0 \mathbf{E}^a - \epsilon_0 \mathbf{E}^b) = \sigma_s$ | Relationship between surface charge density and electric field at the surface boundaries |
| $\nabla \cdot \mathbf{J} = -\frac{\partial \rho}{\partial t}$ | Law of conservation of charge: Current in or out of a volume is equal to the rate of change of charge |
| $\mathbf{J} = \sigma \mathbf{E} + j\omega \mathbf{D} + \mathbf{J}_e$ | Equation for current density given a steady-state frequency domain problem |



CAD Model of Vehicle Imported into COMSOL

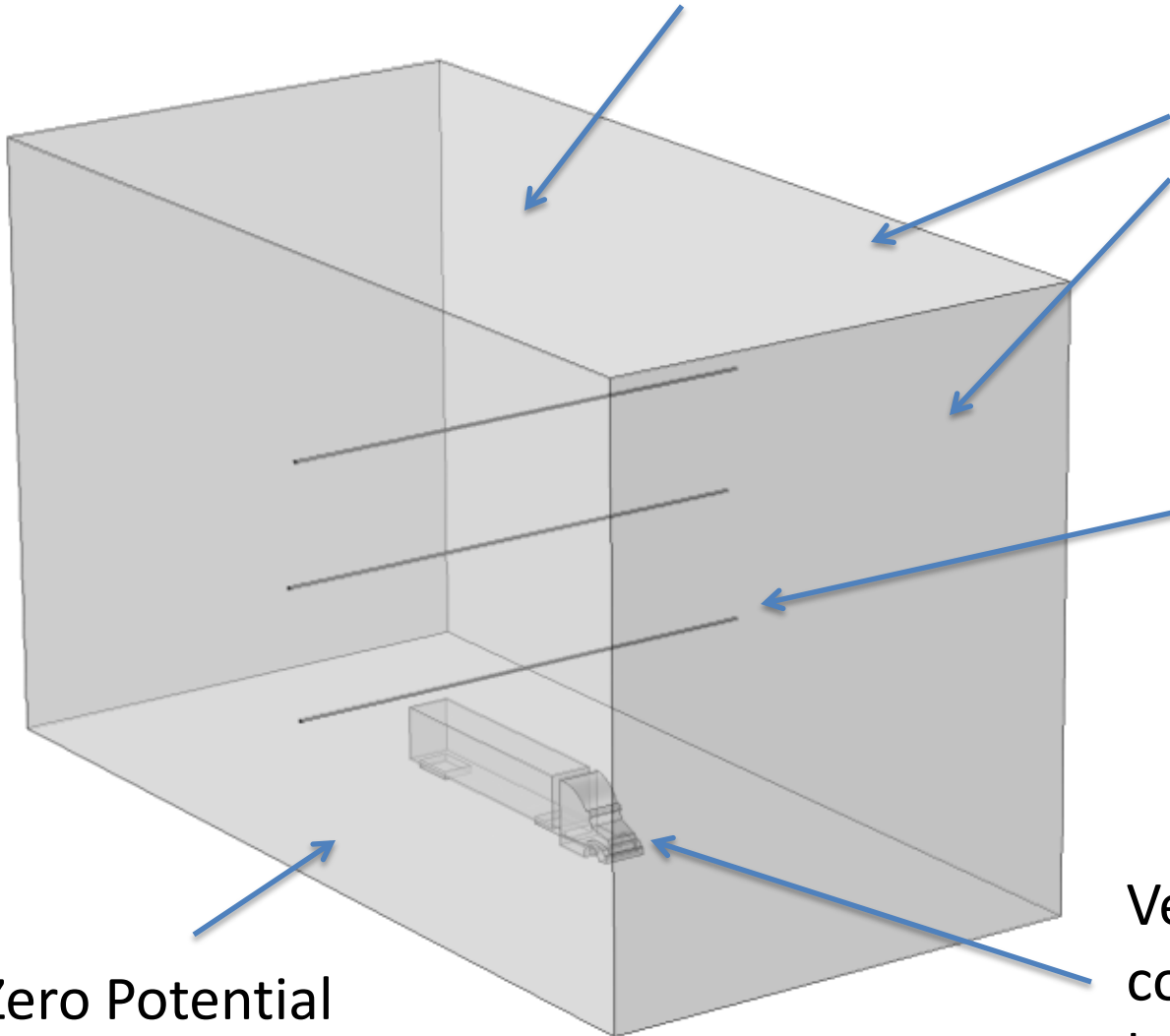
Air volume

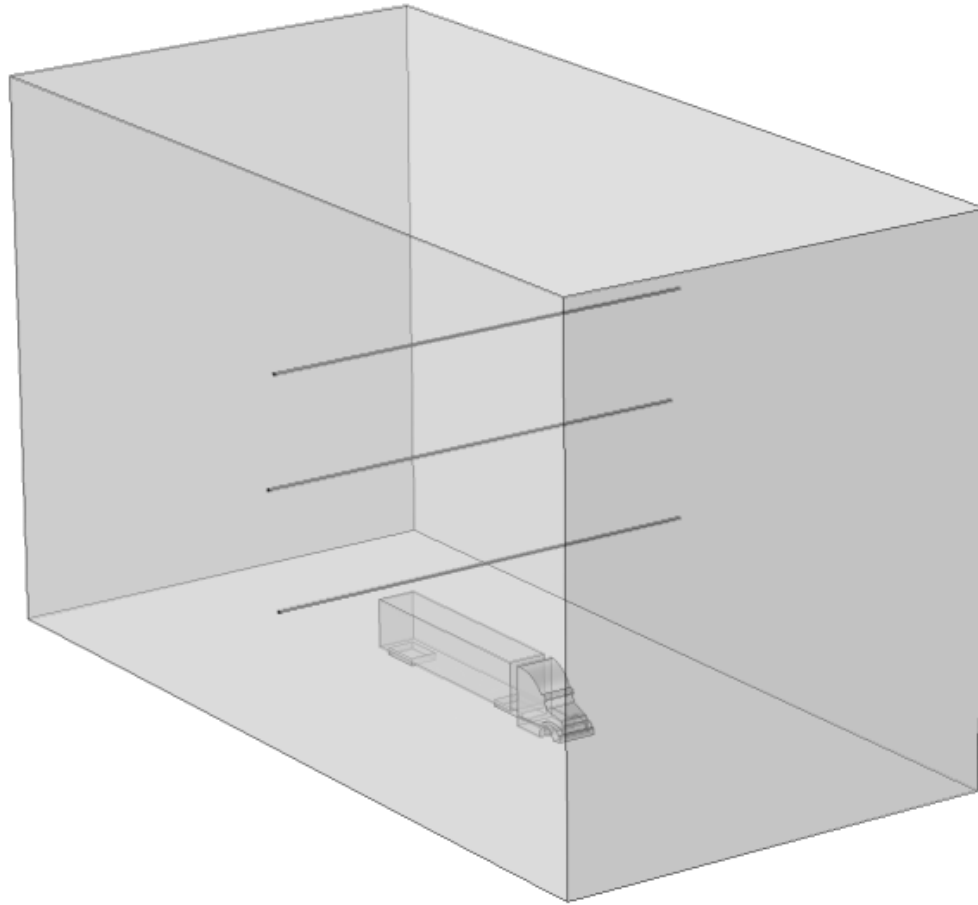
Electric insulation for
top and side
boundary surfaces

Electric Potential
Assigned to
Conductor Surface
(345 kV)

Zero Potential
Ground Plane

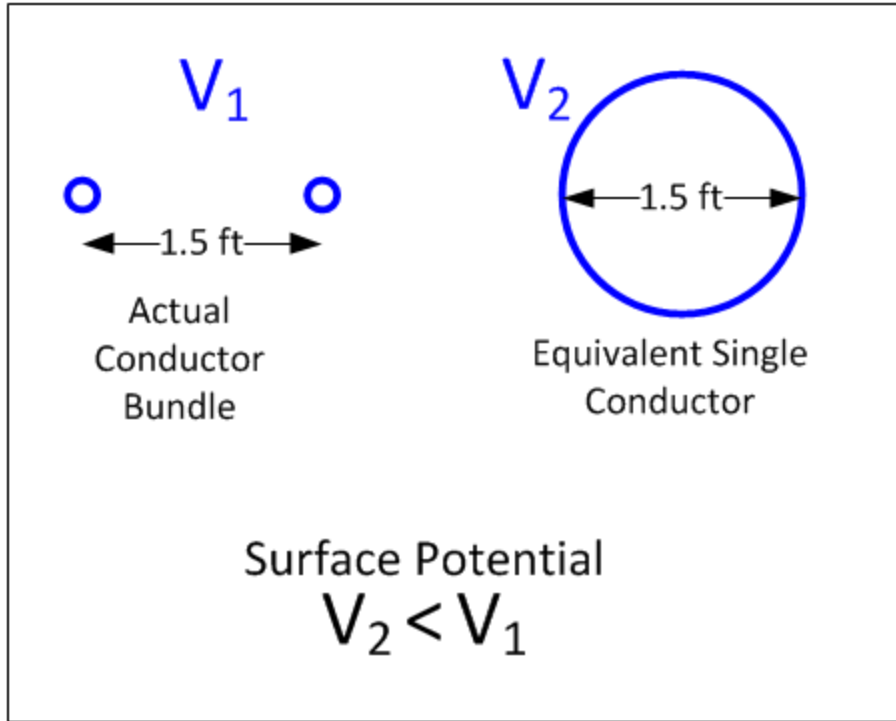
Vehicle is a
conducting body at a
height above ground





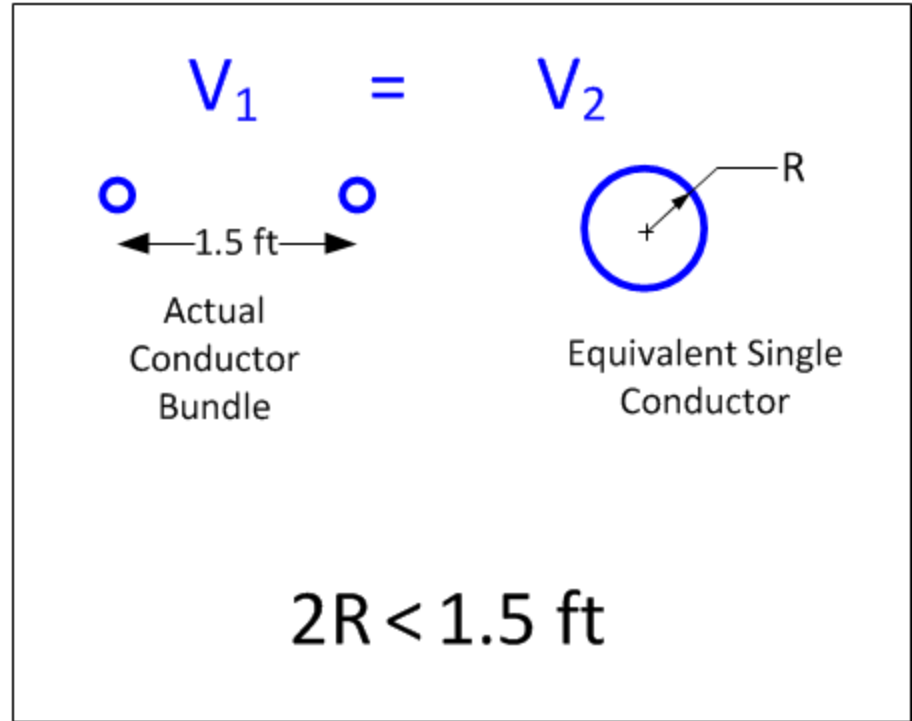
Largest dimension in space = 200 ft
Conductor diameter = 1 inch

=> 2400:1



Perform parametric
sweep of V_2

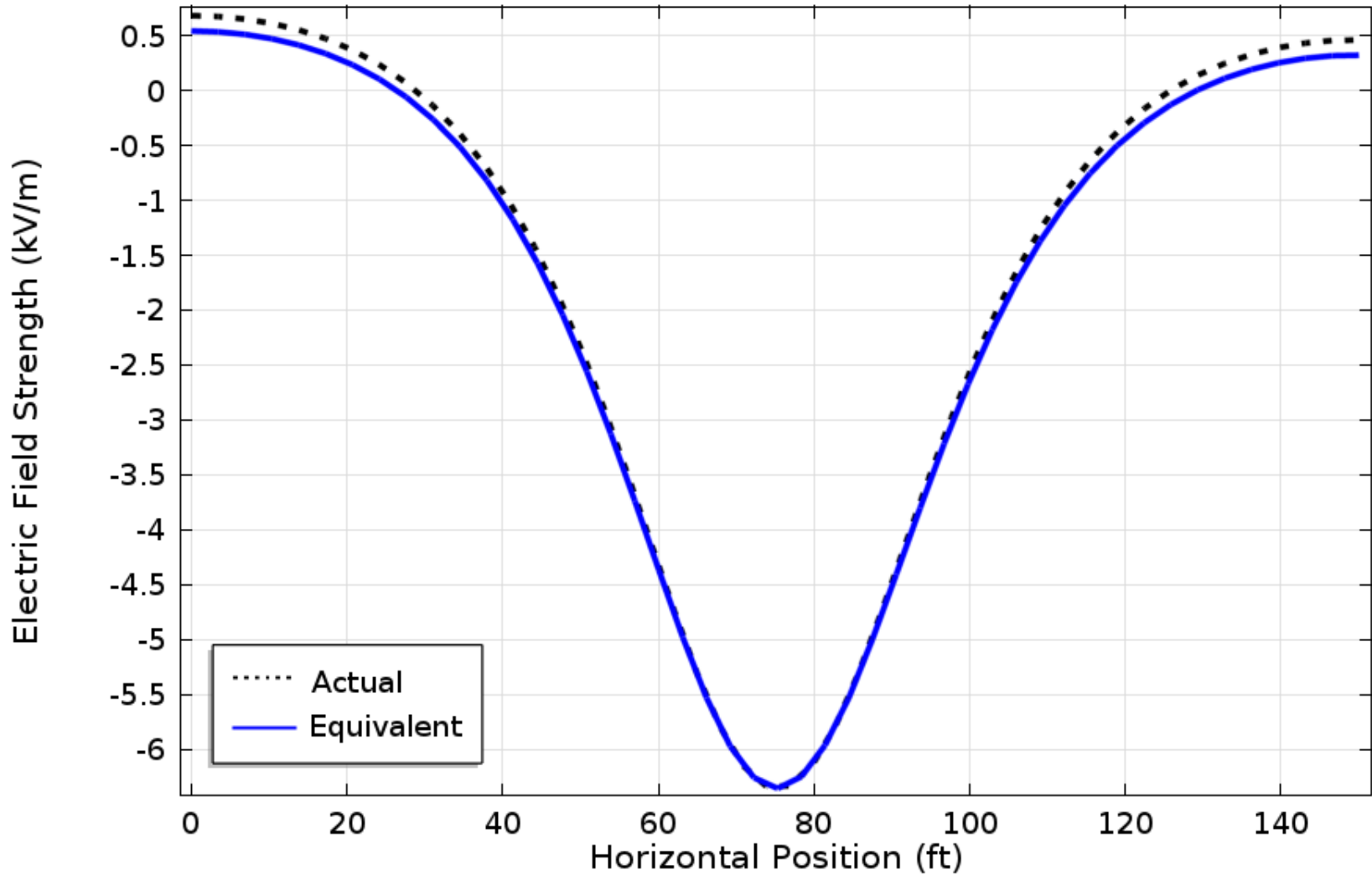
133:1



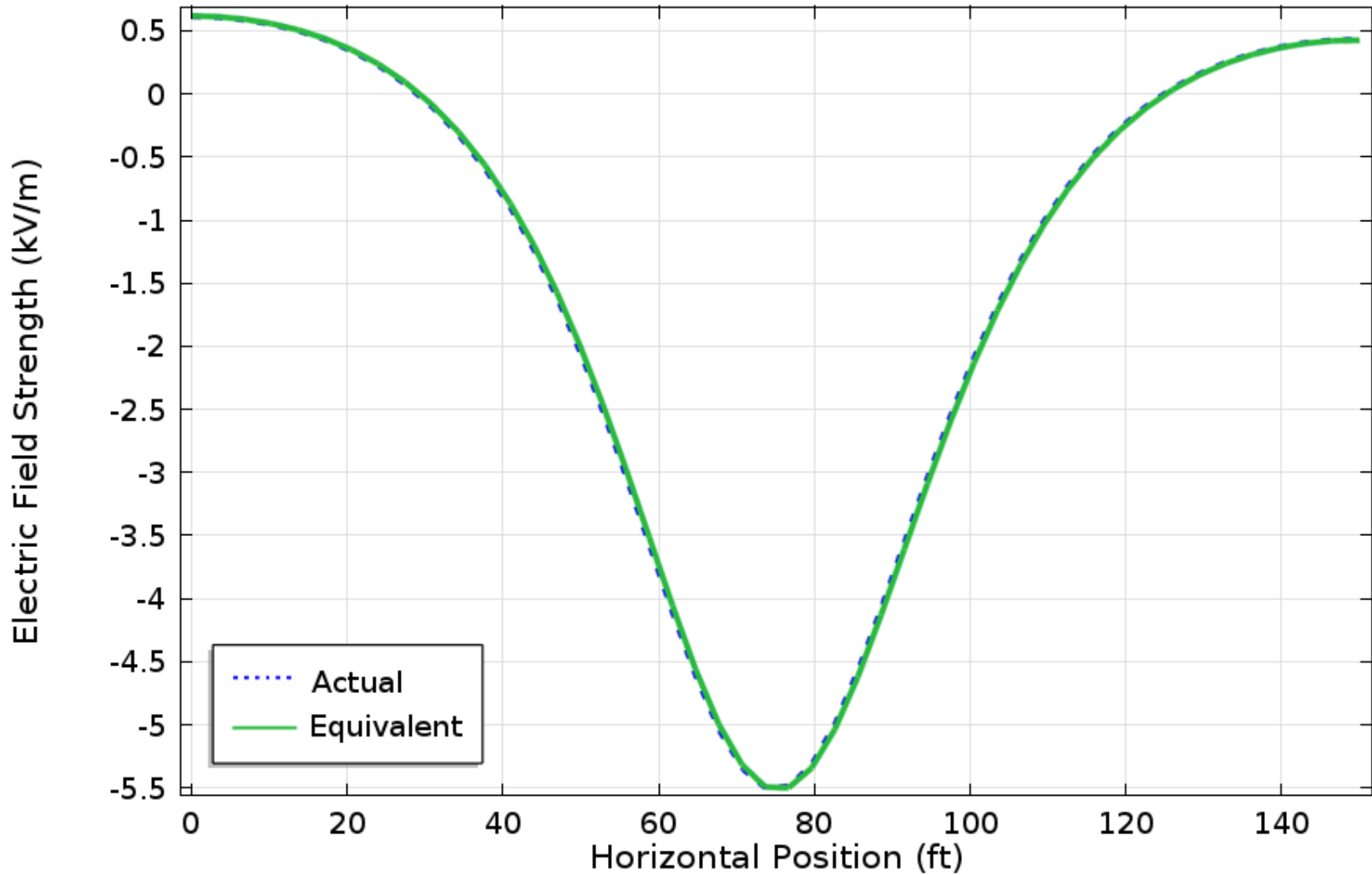
Perform parametric
sweep of R

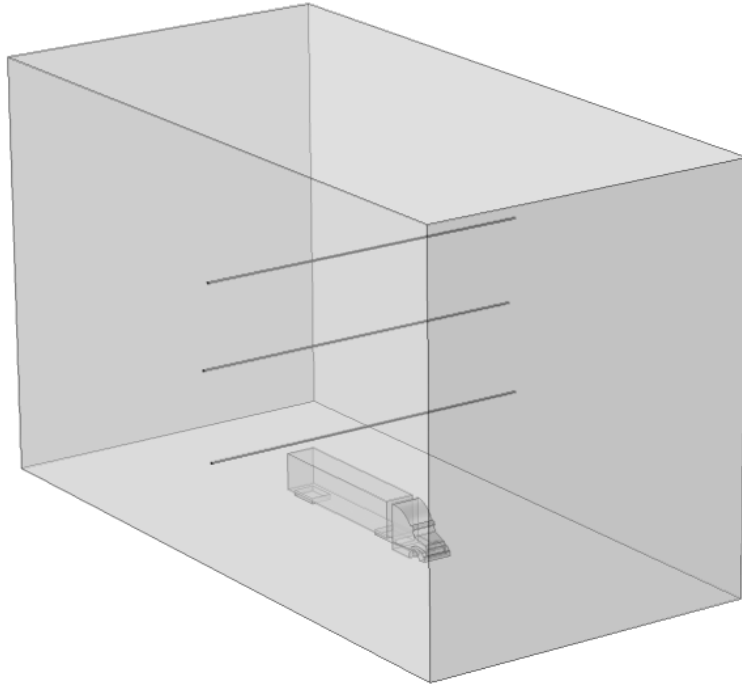
400:1

Performance of a 1.5 foot Diameter Equivalent Conductor



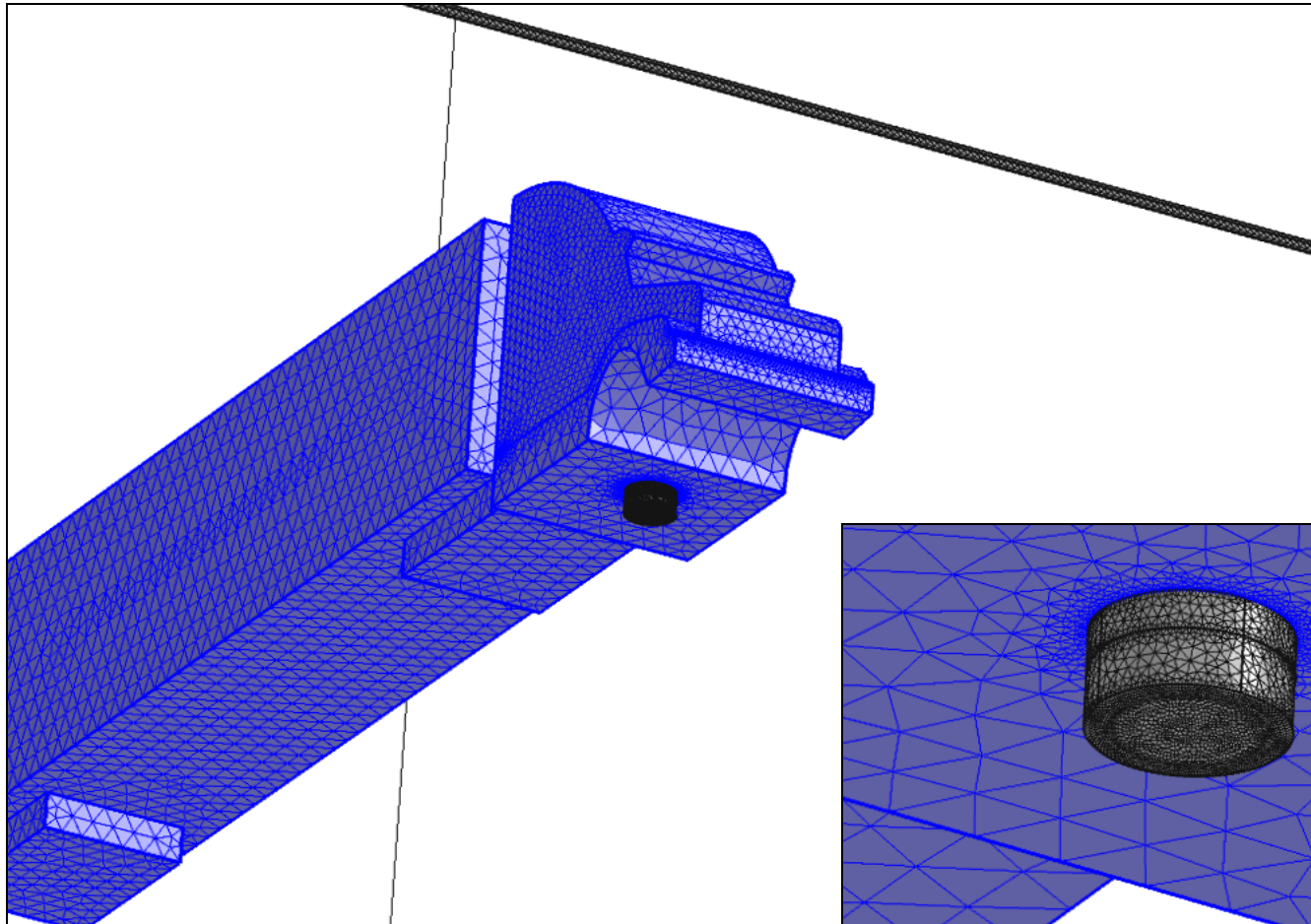
Performance of a 6 inch Diameter Equivalent Conductor



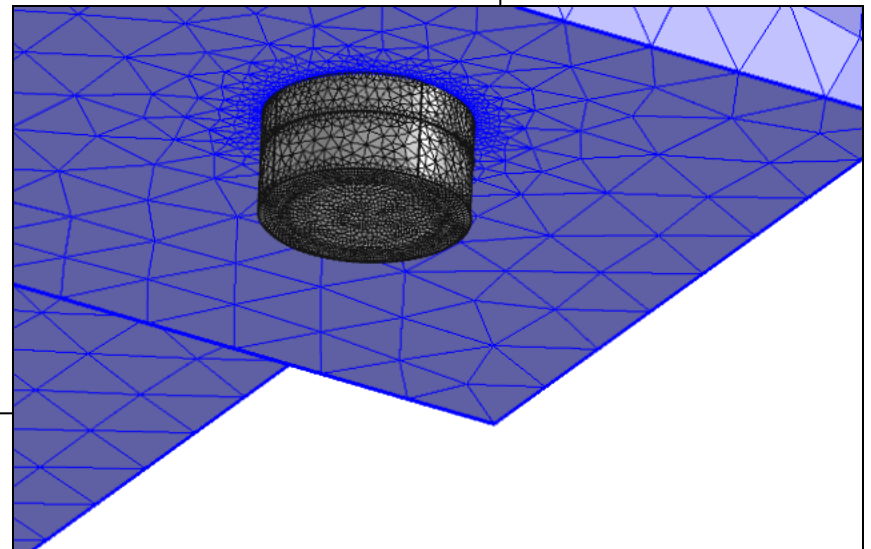


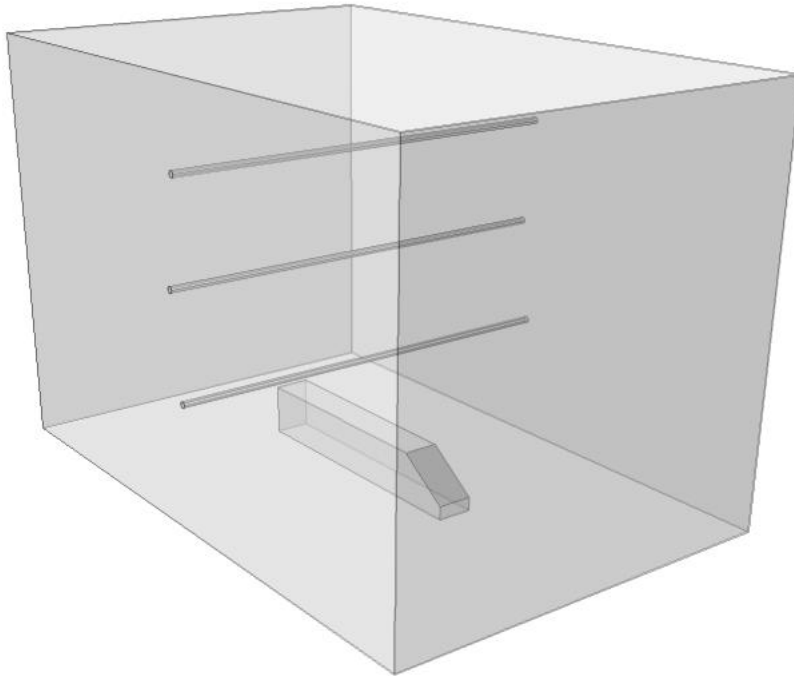
Approach 1:

- Electric Currents Interface with iterative solver => easily handled about 1.2M DoF
- Truck volume meshed and included in solution space
- Conducting cylinder connects vehicle to ground



Approach 1

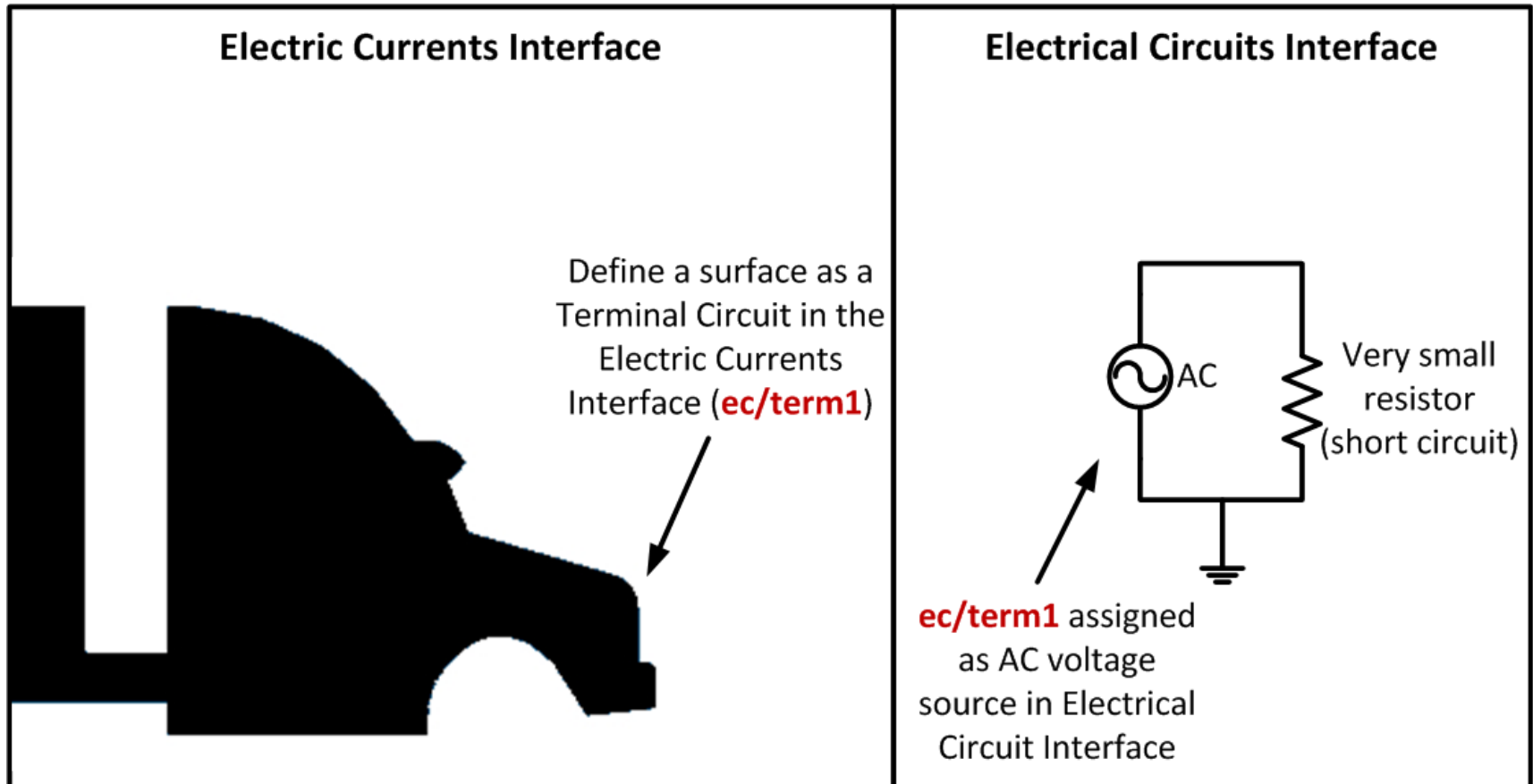


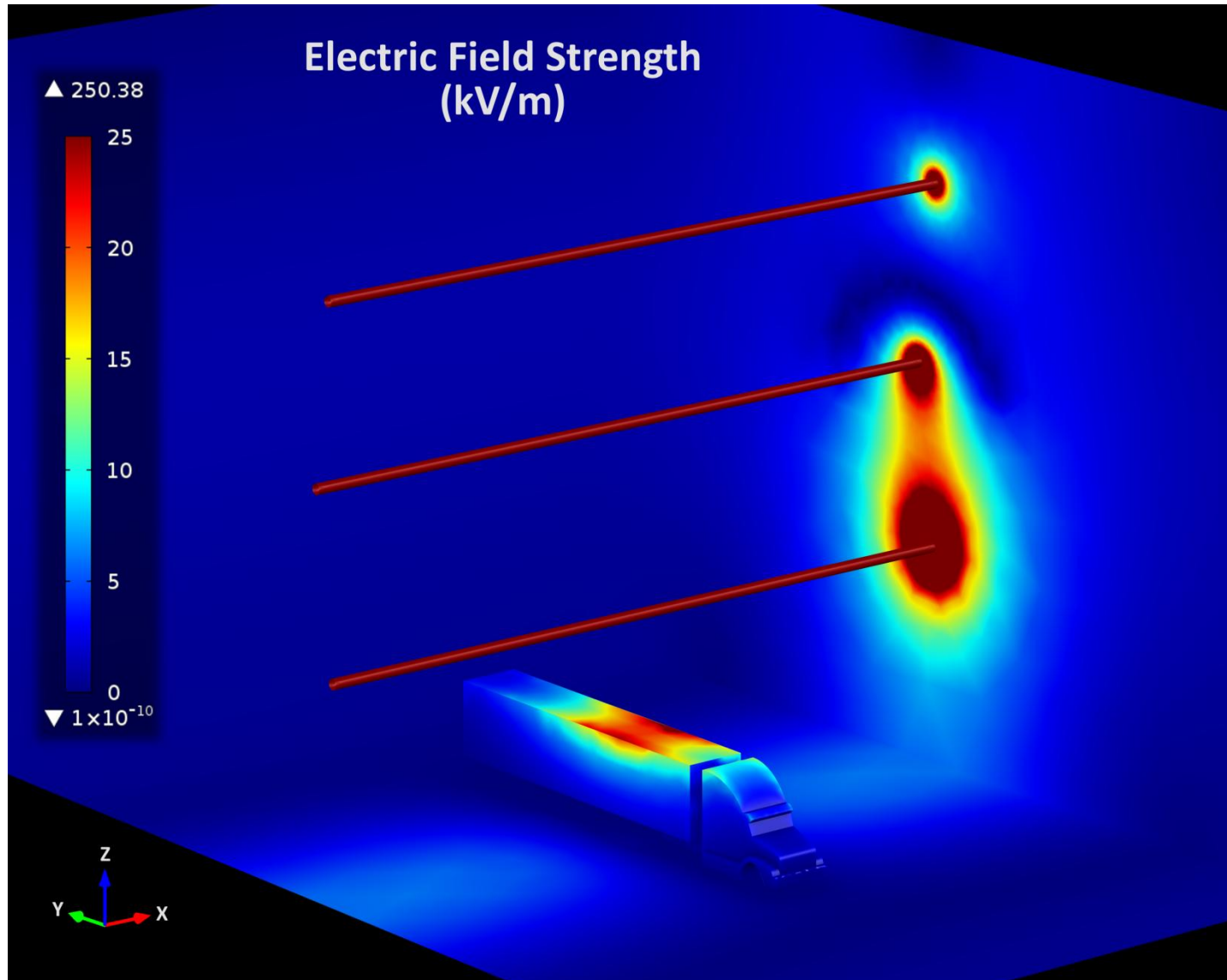


Approach 2:

- Electric Currents Interface and Electrical Circuits Interface with direct solver => **could only handle about 200K DoF**
- Truck volume not meshed and not included in solution space
- Electric Shielding element with conducting properties used on vehicle surfaces

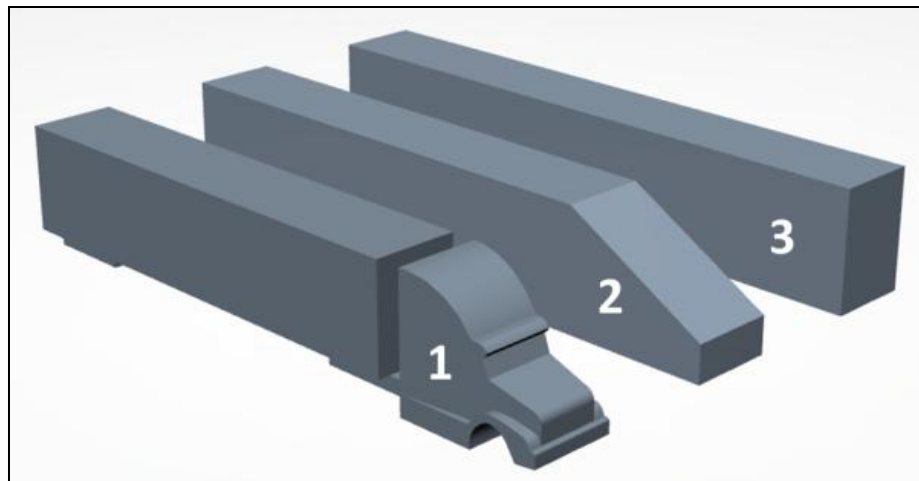
Approach 2



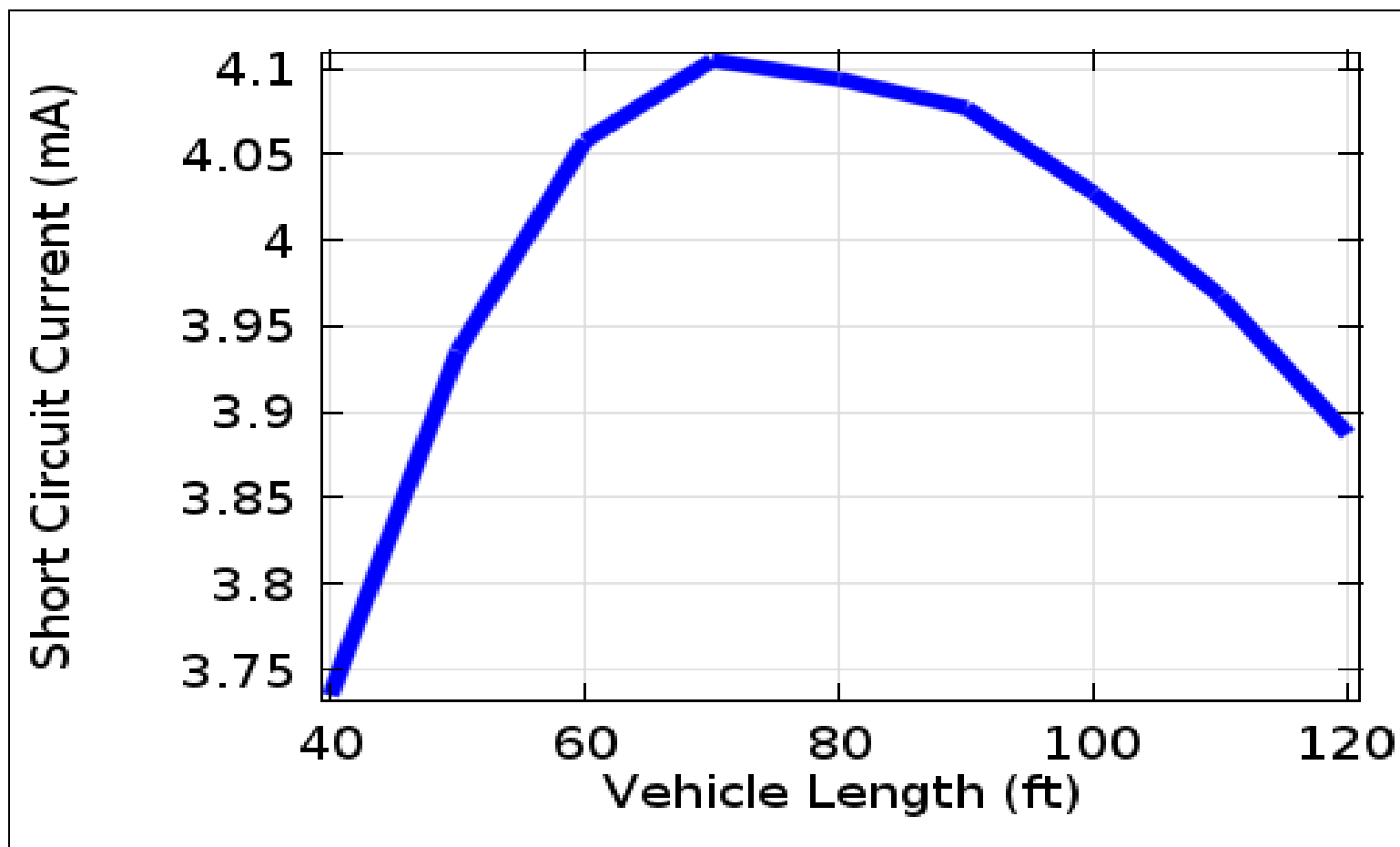


Short Circuit Current

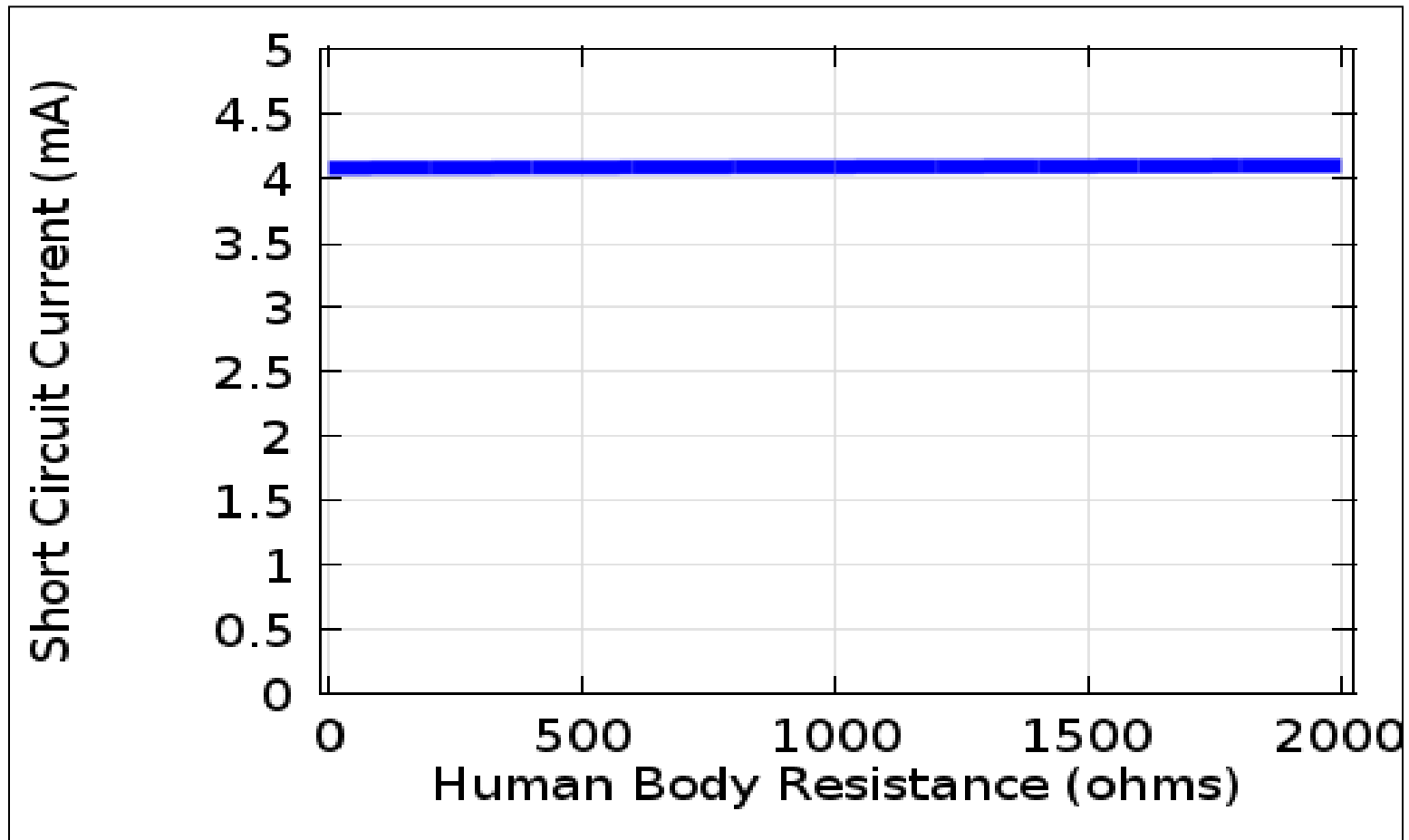
| Approach | Short Circuit Current | | |
|-------------------|-----------------------|---------|---------|
| | Truck 1 | Truck 2 | Truck 3 |
| Semi-empirical | n/a | n/a | 4.2 mA |
| COMSOL approach 1 | 3.8 mA | 4.1 mA | 4.2 mA |
| COMSOL approach 2 | 4.0 mA | 4.0 mA | 4.1 mA |
| CDEGS | n/a | 4.1 mA | 4.2 mA |



Parametric Sweep of Vehicle Length

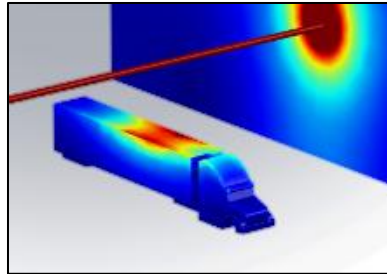


Parametric Sweep of Body Resistance



For The Case Studied:

1. The semi-empirical approach with geometric simplifications provides reasonably accurate results and is biased appropriately on the side of safety
2. The “largest anticipated vehicle” is not necessarily the controlling case for electrical clearances
3. Resistances in the range of that of the human body have negligible effect on the flow of current to/from the vehicle



QUESTIONS?