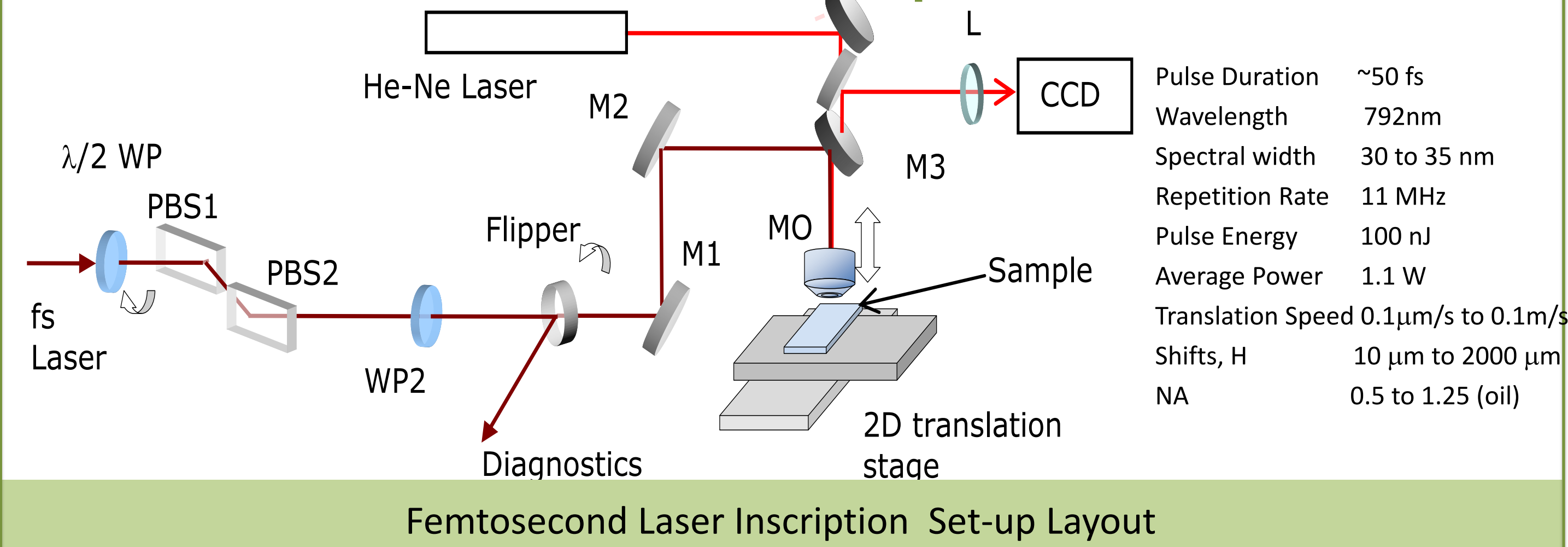
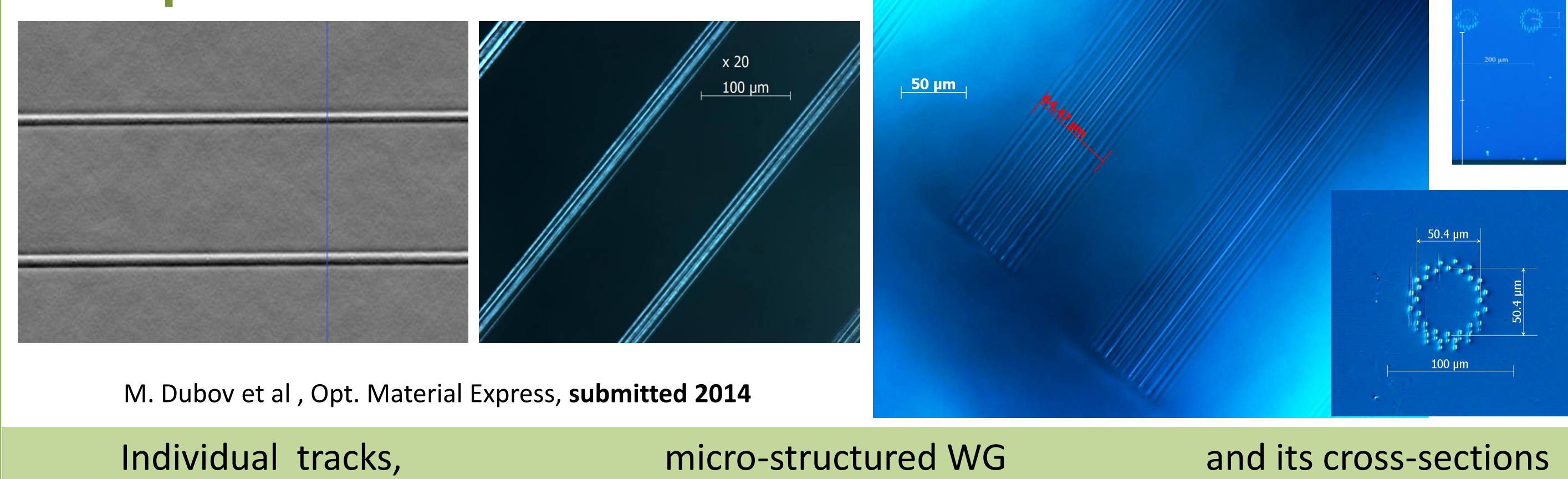


ABSTRACT: We describe how the guiding properties of buried, micro-structured waveguides that can be formed in a lithium niobate crystal by direct femtosecond laser writing can be optimized for low-loss operation in the mid-infrared region beyond 3.5 μm .

1. Direct Femtosecond Laser Inscription

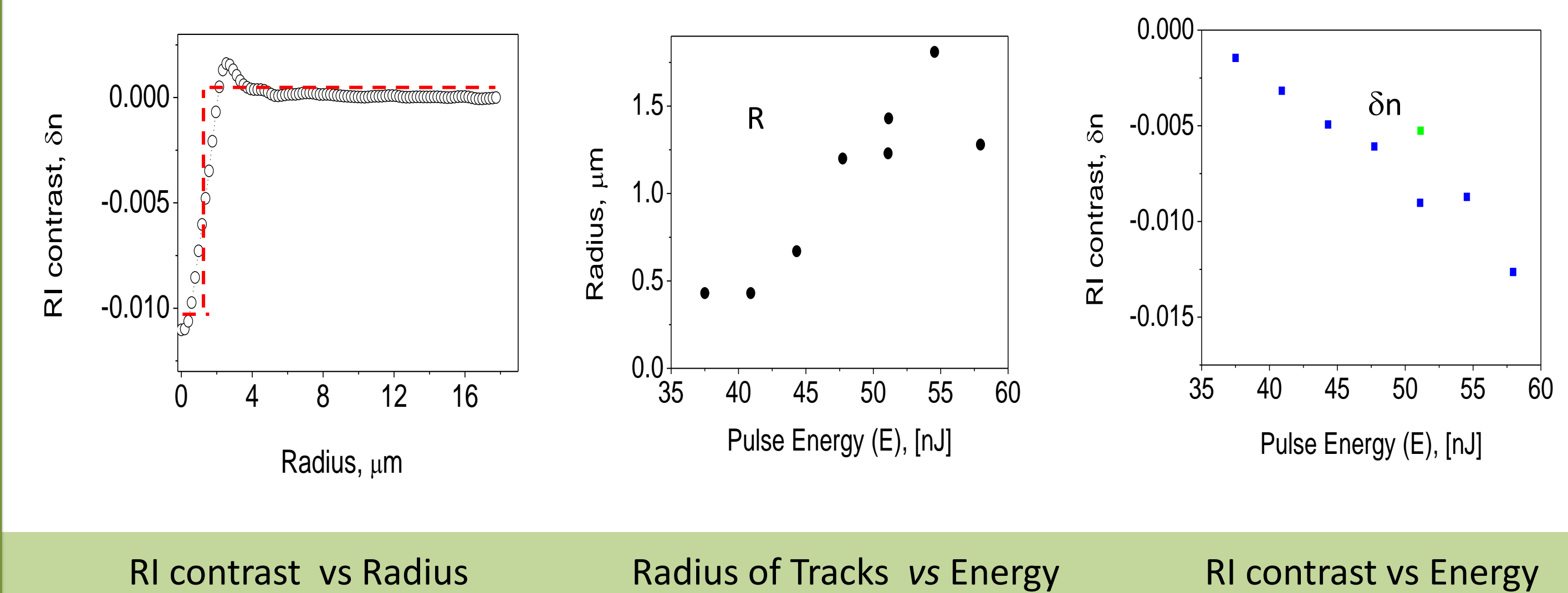


2. Experiment Results

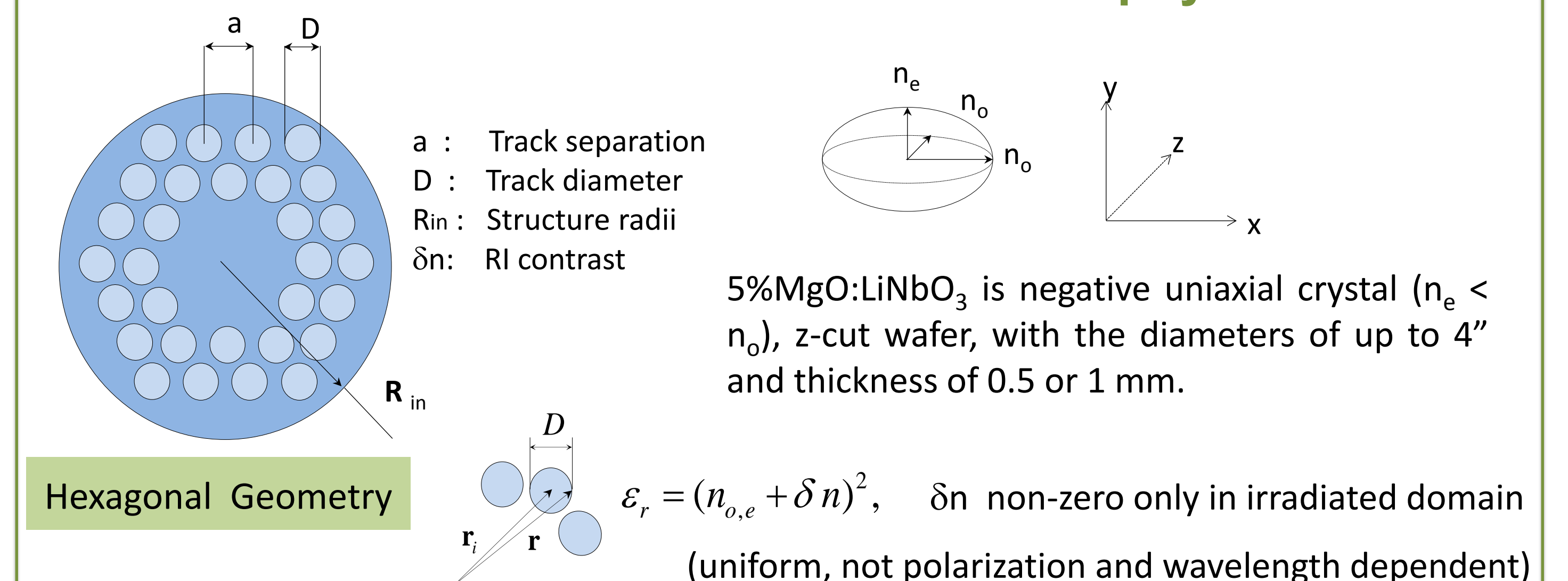


3. Parameters for Simulation

- The parameters measured were used in the simulations
- Step-index RI profile is assumed
- Both Radius and RI contrast of tracks are intra-dependent via Pulse Energy



4. Numerical Calculation with COMSOL Multiphysics®



- Wave Equation for Monochromatic Optical Wave in micro-structured WG:

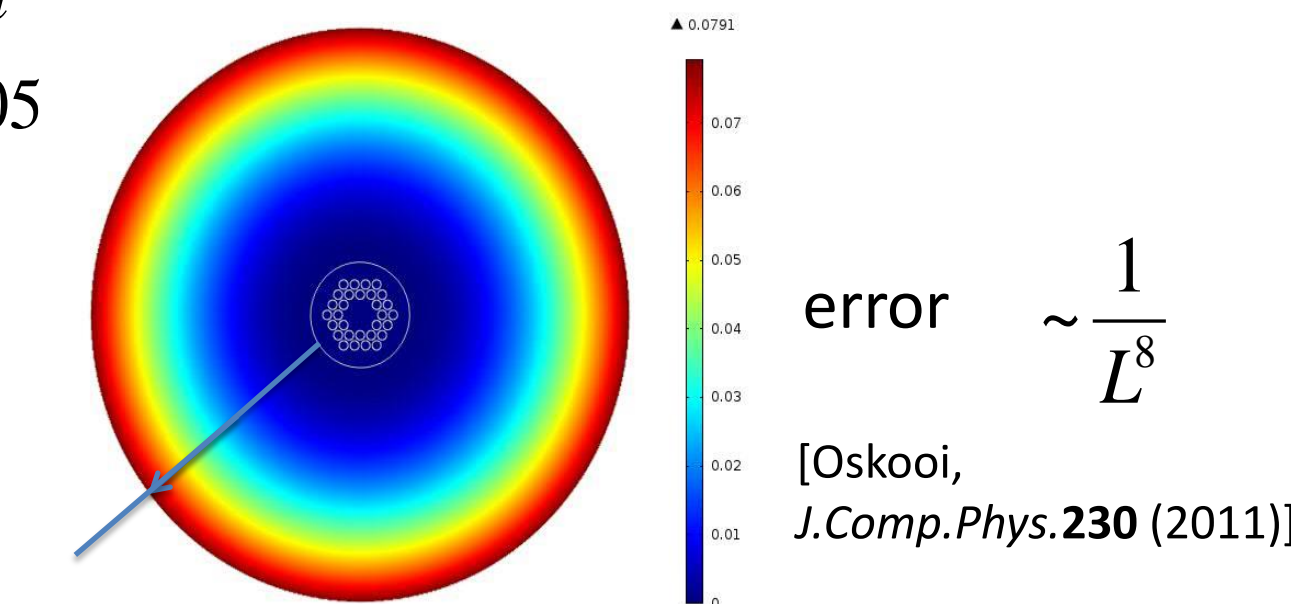
$$\nabla \times \nabla \times \mathbf{E} - \omega^2 \epsilon_0 \epsilon_r \mu_0 \mathbf{E} = 0, \quad \epsilon_r = \begin{pmatrix} \epsilon_o & 0 & 0 \\ 0 & \epsilon_e & 0 \\ 0 & 0 & \epsilon_o \end{pmatrix}$$

- Simulations are realized between 0.3 to 3 μm with 0.01 μm steps
- RI for congruently grown LiNbO₃ taken from [Zelmon et al., JOSA B 14 1997]
- PML and Mesh optimization is required for correct results

PML (Perfectly Matching Layer):

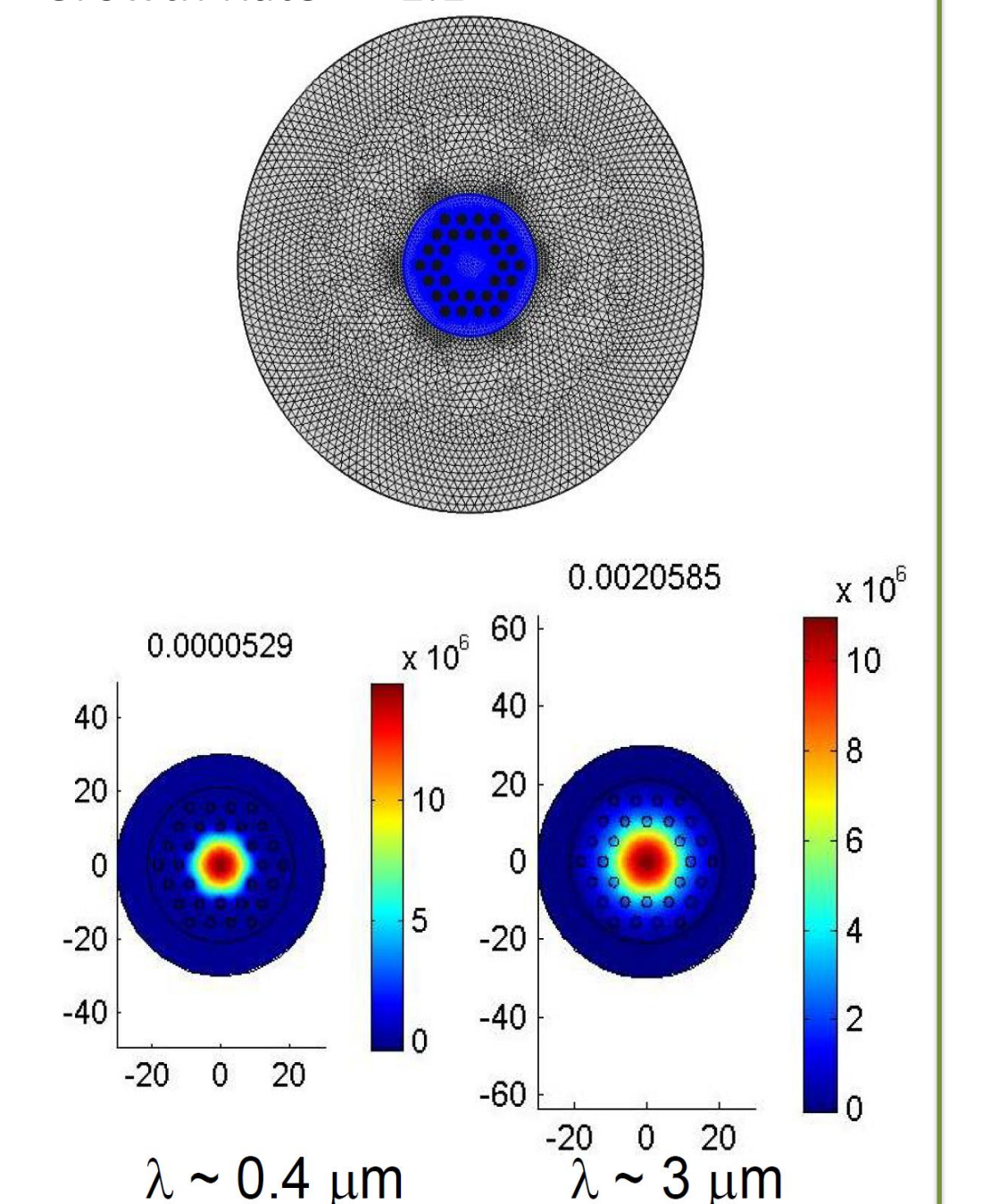
$$n_{PML}(r) = n_{o,e} - i k_{MAX} \left(\frac{r - r_{in}}{L} \right)^2, \quad r_{in} < r < r_{in} + L$$

$L = 40 \mu\text{m}$
 $k_{MAX} = 0.05$



MESH:

'Triangular' MESH
Max Mesh Size (at periphery) $\sim 1 \mu\text{m}$
Min Mesh Size (at core) $\sim 0.003 \mu\text{m}$
Growth Rate = 1.1

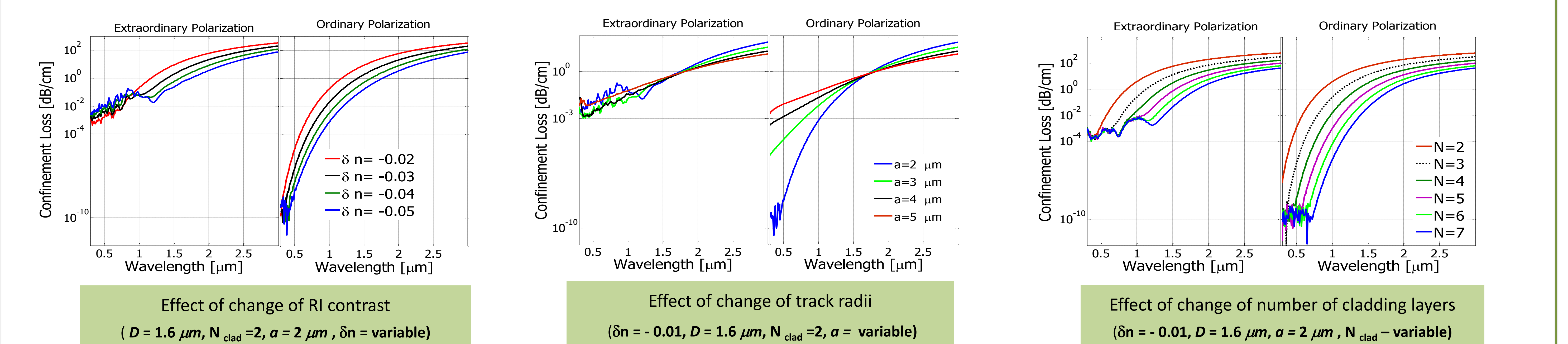


Parameters and Constrains for the numerical simulation

| | | |
|-----------------|------------|--|
| Period | a | >D/2 (2 μm to 5 μm) |
| Track Diameter | D | >0.5 μm (0.08 μm) |
| RI Contrast | Δn | -0.02 ... -0.0005 (-0.05.....-0.01) |
| Cladding Layers | N_{clad} | >1 (1 to 7) |

H. Karakuzu, et al., Opt. Express, 21 2013

6. Results

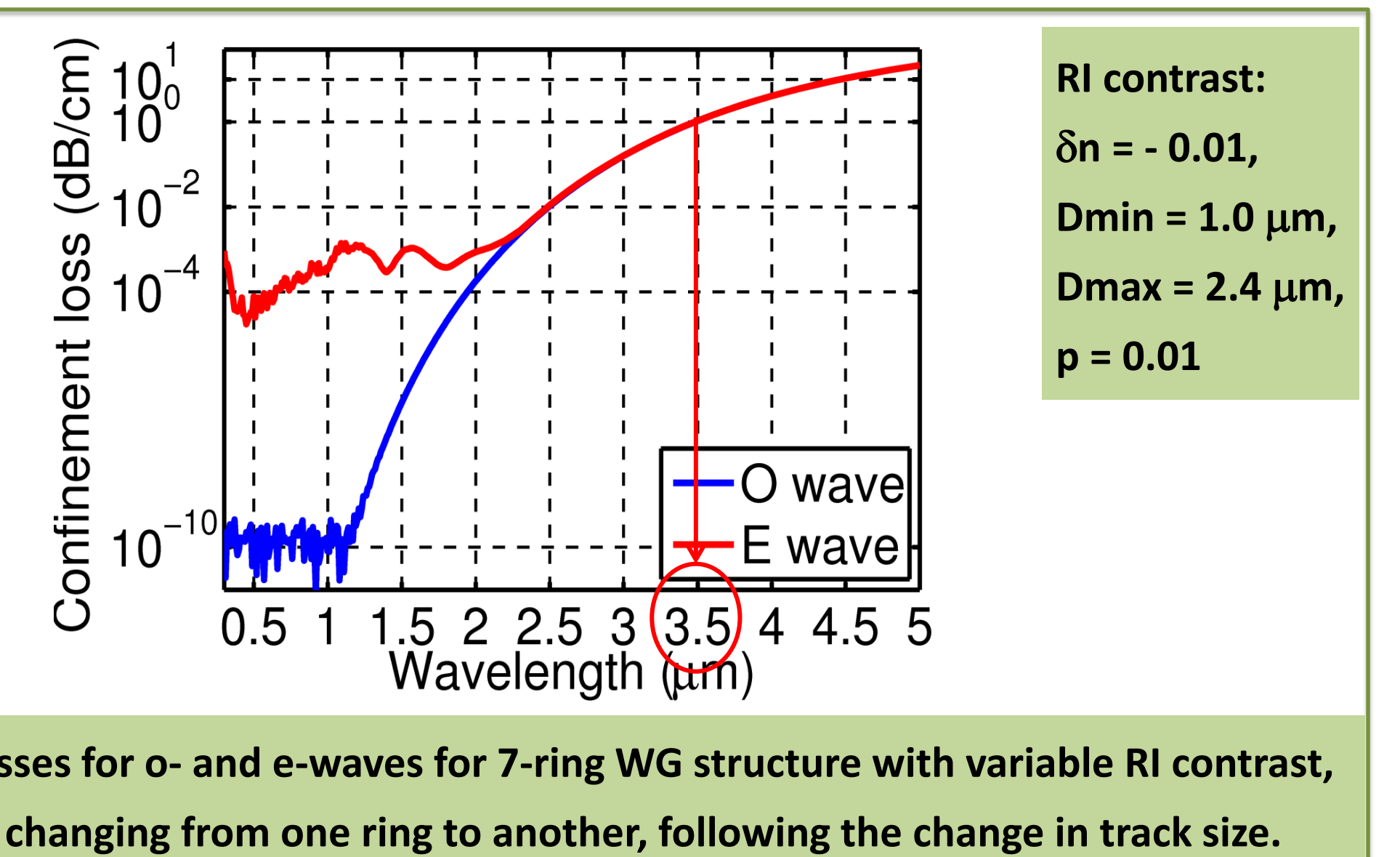
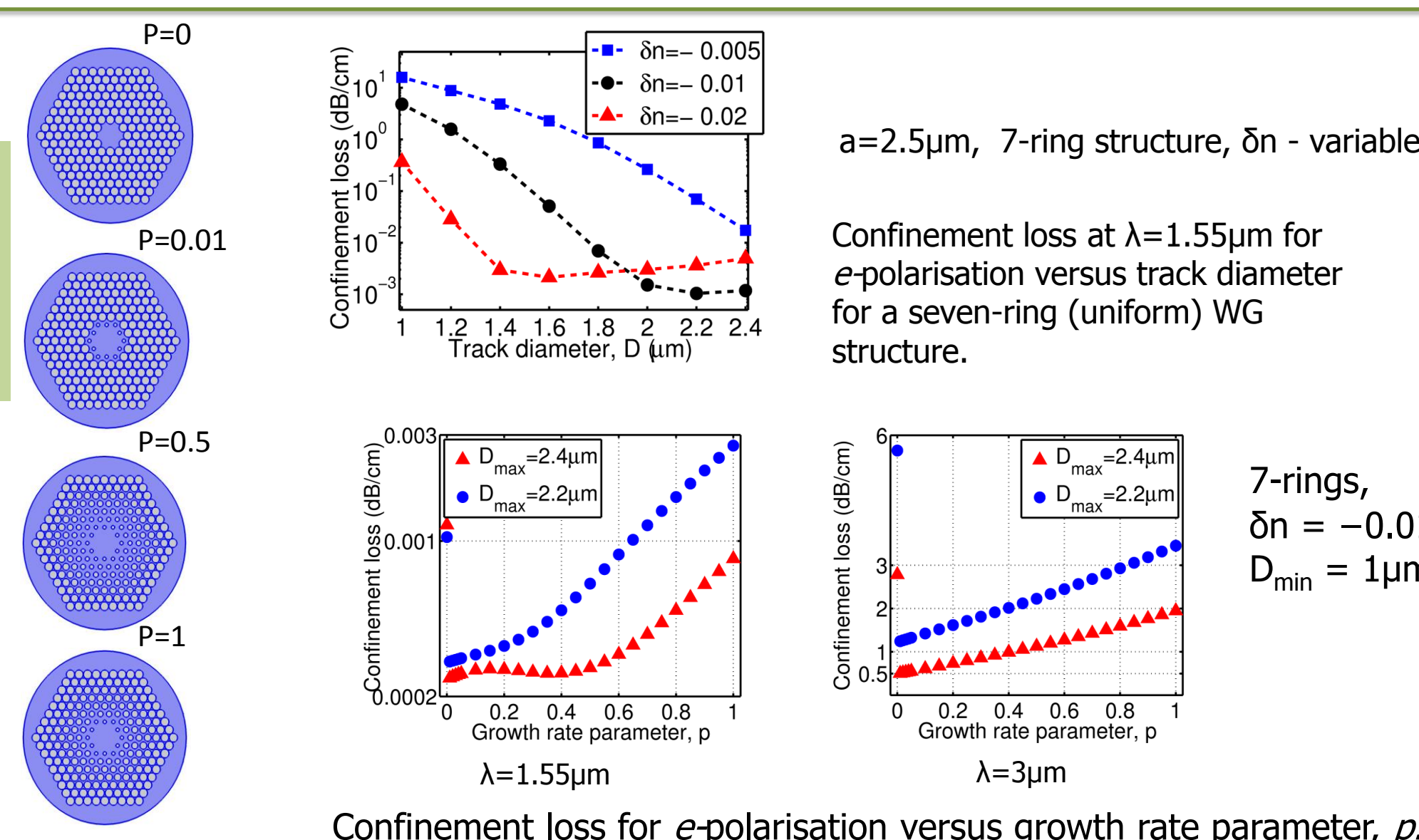


7. Optimisation

Minimum confinement loss is searched by changing the track diameters of each layer according to the formula:

$$D(N) = D_{min} + 2 \cdot \left(\frac{N-1}{N_{clad}-1} \right)^p \cdot (D_{max} - D_{min})$$

H. Karakuzu, et al., Opt. Mat. Express., 4 2014



CONCLUSIONS: We have numerically demonstrated that the guiding properties of depressed-cladding, buried WGs formed in a LiNbO₃ crystal by fs laser writing can be controlled by the WG structural characteristics, even for the relatively moderate induced RI contrasts typical of the direct fs inscription. In particular, the number of depressed-cladding layers has revealed to play a major role in the control of the WG properties. Importantly for practical applications, we have shown that for an induced RI contrast of -0.013, the propagation losses can in principle be reduced by four orders of magnitude at telecom wavelengths by increasing the number of cladding layers from 2 to 7. Minimisation of the confinement loss at mid-infrared wavelengths is realised by varying the growth rate of track diameters.