Models for Simulation Based Selection of 3D Multilayered Graphene Biosensors

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Abstract: At the forefront of a new generation of sensors graphene and graphene composite materials are intensively studied for medical and biosensing applications. The outstanding electrical, mechanical and quantum properties of graphene make them a promising material solution to overlap the existing gap between biological and non-biological systems into a continuum like-viscoelastic integrated model. Through COMSOL Multiphysics® modeling and simulation were identified the best fitted solutions for a multilayered biosensing device structure from the presently known graphene (G), graphene- oxide (GO) and composite materials including different forms of graphene (graphene nanoribbons –GNRs, reactive graphene oxide –RGO, and TWEEN paper –TwGP).

Keywords: graphene, biosensor, Fröhlich quantum coherence, phonon, non-linear thermodynamics

1. Introduction

Intensely studied in the last decade, graphene (G), graphene oxides (GO), reactive graphene oxides (RGO), graphene nanoribbons (GNRs) and many other graphene based composite materials are continuously approach to the medical and biosensing area with the aim of defining new material solutions for properly personalized medical applications and therapeutic solutions.

With large similarities to the surface of graphite (Figure 1), graphene (G) can adsorb and desorb different type of atoms and molecules, remaining highly conductive [1]. This property can be used for sensor applications. It is largely known that single- layer graphene (1G) is much more reactive than 2G, 3G (<10 layers) graphene multilayer structures [2,3]. However, the edge of the graphene is more reactive than the surface, graphene being a fairly inert material, and thus an ideal candidate for bio-sensors.
The aim of the modeling and simulation of the multilayered graphene structures is mainly focused on the device response at different types of energy stimulus reaching the active surfaces of the 3D bio-sensing structures under the main restrictions of biocompatibility and non-toxicity (Figure 2, Figure 3).

2. Models Definition

The most accessible and nonintrusive interface of a sensor with humans is on the skin surface. Not only because skin is the organ that has the widest area of the human body, but because it has differentiated responses to internal and external stimuli, thus being an accessible environment for physical and chemical data gathering. Based on FET (Field Effect Transistor) properties [15,17] that can relate human skin to the presently known characteristics of G/GO/TwGP [1,4,5,13,16,18] two biosensing devices were designed (Figure 4 c, d).

For these studies were considered the main interfaces between: human skin – hydrogel polymer structure (PVA Hydrogel); PVA Hydrogel – graphene based module (G/GO/TwGP); graphene module – electrodes (Ag); graphene/electrodes – substrate (Silica glass SiO$_2$) (Figure 4 c, d). For each of these interfaces were identified models able to describe the evolution of the process microvariables as well as the environmental stimuli influences (macrovariables) as follows:

- Two electrodes biosensing module (Figure 4c) including skin, PVA Hydrogel, graphene (G) and graphene-oxide (GO) functionalized with different proteins (Alpha Helix, Loricin and Lysozyme)
  - Four electrodes module (Figure 4 d) that considers the same main interfaces with both graphene composite structure and without it, for the same environmental stimuli, in order to objectively differentiate the graphene responses (Figure 5,...15)

All these models are having the same continuum-like background of a biosensor device structure based on weak van der Waals interaction forces that describe the nonlinear behavior of graphene into a surrounding viscoelastic environment through classical Kirchhoff plate theory [14]

In the Equation 1, used for modeling single layer graphene vibration response based on Kirchhoff plate theory [14] $\alpha_1$ and $\alpha_3$ represents the linear and nonlinear interaction forces:

$$D \nabla^4 w + \alpha_1 w + \alpha_3 w^3 + \rho h_2 \frac{\partial^2 w}{\partial t^2} + N_x \frac{\partial^2 w}{\partial x^2} + N_y \frac{\partial^2 w}{\partial y^2} = 0$$  \hspace{1cm} (1)$$

where: $N_x$, $N_y$ are biaxial in-plane loads; $a$, $b$ - length, width of the single layer graphene; $h$ - thickness of the single layer graphene; $p$ – distributed transverse load per unit area (due to surrounding medium effect) ; $D$ is the bending stiffness of the plate:

$$D = \frac{E h^3}{12(1-\nu^2)}$$  \hspace{1cm} (2)$$

$E$ is the Young’s modulus; $
u$ – Poisson’s ratio; $\rho$ – mass density; $\nabla^2$ - Laplace operator:

$$\nabla^2 = \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2}$$  \hspace{1cm} (3)$$

The density of charge, characterizing all interfaces, is properly described through nonlinear thermodynamics with electron – phonon ($\bar{\varepsilon} - ph$), phonon – phonon ($ph - ph$) and ion –phonon interactions. Thus for all models were studied the charge density distributions of electric, thermal and acoustic field stimuli responsible for ($\bar{\varepsilon} - ph$), ($ph - ph$) and (ion –ph) interactions (Figures 5,..., 15).
For the envisaged multilayer structures of graphene biosensing devices a graphene model was firstly created in ChemBio 3D Ultra©. Its characteristics have been exported to MATLAB© and thus different process parameters and material properties were consistently interlinked for further analyses and simulations (Figure 2,3). MATLAB© model and the associated properties were exported through the LiveLink™ for MATLAB© add-on in COMSOL Multiphysics © and thus the variability of the structure properties (Figure 3) could be properly analyzed in at the device scale (Figure 5,...15). The models designed to include environmental stimuli acting upon human body were focused either on the thermal slight modifications or electric conductance variations due to emotional rise or on area exposure to acoustic waves (Figure 6,7). Acoustic Module of COMSOL Multiphysics © and Equation Based Models were used to define interface response to variations of environment acoustic pressure (frequency vary from 1000 Hz to 8000 Hz)

4. Results

A large number of device module types have been tested in order to define the best response of the hydrogel- polymer layer (PVA Hydrogel) on the graphene sheets and of the protein functionalized graphene biosensors.

Excerpt from the Proceedings of the 2015 COMSOL Conference in Grenoble
For each of these modules the biologic responses and the field excitations have to reach simultaneity under the COMSOL Multiphysics® model (Figure 4).

**Figure 11** Pressure distribution (skin-polymer)/sensor interface: (a) 2 electrodes device; (b) 4 electrodes device

**Figure 12** Spatial distribution of flux energy on graphene biosensor (4 electrodes device)

**Figure 13** Interfaces charge distributions (4 electrodes device)

**Figure 14** Membrane stress under environmental stimuli: 2 electrodes device

**Figure 15** Interface stress under environmental stimuli: (a) 2 electrodes device; (b) 4 electrodes device

5. Discussion

The analyzed biosensing device models, regardless their design solution (two or four electrodes; single- or multilayer graphene; graphene composite material) revealed through simulations output data the “sensing” ability of the graphene–based concept model.

For each module type the graphene/graphene composite materials generate clearly differentiate responses to the environmental stimuli, or process microvariables evolution, thus confirming the biosensing ability of this class of materials.

Operating with a continuum model for all interfaces (\(\tilde{e} - \text{ph}, \text{ph} - \text{ph}\) and \(\text{ion} - \text{ph}\)) and harvesting biological charge density variations to relate them to environment stimuli, the 3D multilayered graphene biosensors models and simulations offered valuable design solutions

6. Conclusions

Making the best use of the flexible modules of COMSOL Multiphysics® the most relevant device properties of the multilayered graphene biocompatible structures could be determined and, mostly important, could be related to the complex interface phenomena at human skin level.
7. References


8. Appendix

MODEL LIBRARY: Device SLGS (G/GO)
E.g.: Material 1 -Silica Glass

<table>
<thead>
<tr>
<th>Model Parameters</th>
<th>Details</th>
</tr>
</thead>
<tbody>
<tr>
<td>Definitions</td>
<td>Input voltage, Layer thickness, Electric conductivity of silver, Electric conductivity of Nichrome, Air temperature Heat transfer film coefficient, Air Fluid temperature, Heat transfer film coefficient, fluid</td>
</tr>
<tr>
<td>Material 1</td>
<td>Silica Glass</td>
</tr>
<tr>
<td>Coefficient of thermal expansion Heat capacity /constant pressure Density, Thermal conductivity Young’s modulus, Poisson’s ratio</td>
<td></td>
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</tbody>
</table>
| Equations Material 1 |  \begin{align*}
0 &= \nabla \cdot \mathbf{s} + \mathbf{F}_v \\
\mathbf{s} &= \mathbf{s}_0 + \mathbf{C} \cdot (\mathbf{\epsilon} - \epsilon_0 - \epsilon_{\text{inel}}) \\
\mathbf{\epsilon} &= \frac{1}{2} (\mathbf{u} + \{\mathbf{u}\}^T)
\end{align*} |

Excerpt from the Proceedings of the 2015 COMSOL Conference in Grenoble
Normal; Number of degrees of freedom solved for: 2761 (plus 210 internal DOFs).

COMSOL Multiphysics AC/DC Module CAD Import Module Heat Transfer Module Structural Mechanics Module

Stress (Solid), Isosurface: Total stored energy

For each material and interface layer of both devices were generated similar reports.

MODEL LIBRARY: Acoustic stimulation of devices MLGS (G/GO/TwGP)

<table>
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</tr>
<tr>
<td>Used modules</td>
<td>COMSOL Multiphysics AC/DC Module CAD Import Module Heat Transfer Module Structural Mechanics Module</td>
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<tr>
<td>Material 1</td>
<td>Substrate (Si)</td>
</tr>
<tr>
<td>Material 2</td>
<td>Silica Glass</td>
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<tr>
<td>Material 3</td>
<td>Electrodes</td>
</tr>
<tr>
<td>Material 4</td>
<td>TWEEN/RGO (TwGP)</td>
</tr>
<tr>
<td>Material 1 Parameters</td>
<td>Coefficient of thermal expansion; Heat capacity /constant pressure Density Thermal conductivity Young’s modulus Poisson’s ratio</td>
</tr>
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<tr>
<th>Equations Material 1</th>
<th>(-\nabla \cdot \sigma = F_V)</th>
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<tbody>
<tr>
<td>Equations Material 2</td>
<td>(0 = \nabla \cdot s + F_V) (s = S_0 + C : \left(\epsilon - \epsilon_0 - \epsilon_{inel}\right)) (\epsilon = \frac{1}{2} \left( \nabla u + (\nabla u)^T \right))</td>
</tr>
<tr>
<td>Equations Material 3</td>
<td>(-\nabla \cdot \sigma = F_V + \sigma (M_V \times n) \frac{Z}{\rho d^2}) (\sigma_z = 0, -\frac{d}{2} \leq z \leq \frac{d}{2})</td>
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For each material and interface layer of the biosensing devices were generated similar reports with and without acoustic stimulation.