

# MODELING OF MAGNETOELECTRIC EFFECTS IN MAGNETOSTRICTIVE / PIEZOELECTRIC MULTILAYERS USING A MULTIPHYSICS SIMULATOR.

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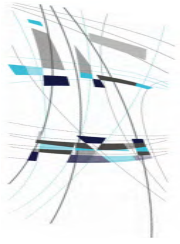
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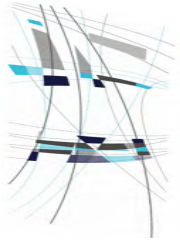
F. Rasoanoavy





# Outline

- Context
- Magnetolectric effect
- Theoretical aspects
- Static modeling of magnetolectric structures
- RF simulations of magnetolectric structures
- Conclusion and prospects



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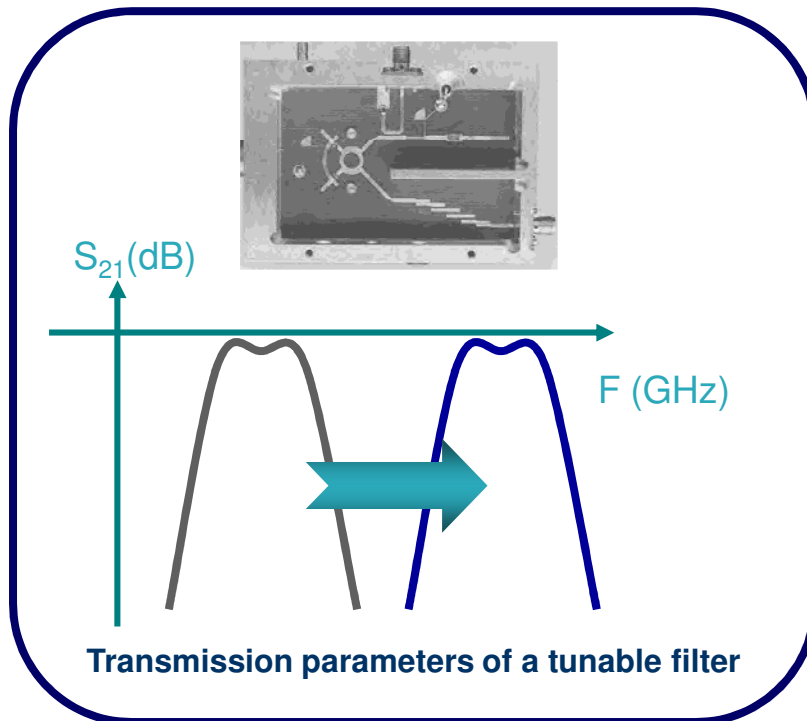
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# Context

## Wireless technology development / emerging services

↳ Compact and low cost tunable systems



Substrates with tunable  $\epsilon$  and/or  $\mu$ :

- ✓ Ferroelectrics
- ✓ Ferromagnetics
- ✓ Liquid Crystals
- ✓ .....

$$fr = \frac{c}{2l_{eff} \sqrt{\epsilon_{eff} \times \mu_{eff}}}$$





# Context

➤ Use of ferroelectric layers :

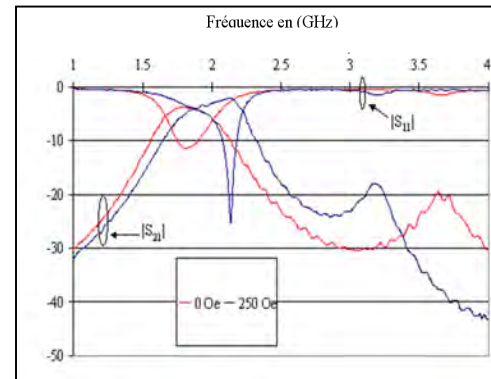
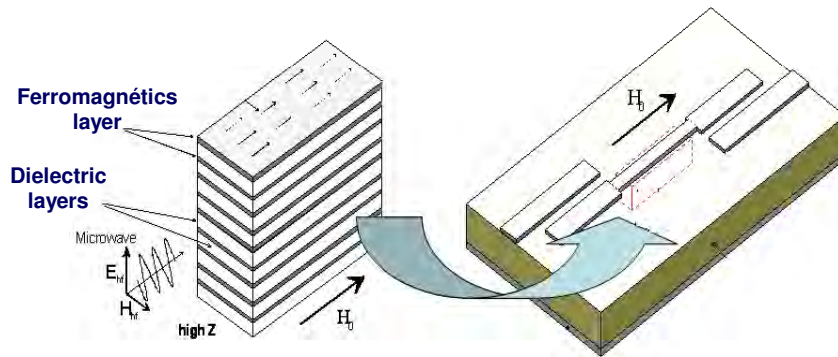
☺ Electrical biasing

☹ Impedance mismatch (high  $\epsilon$ ) & Loss  $\text{Tan}\delta > 10^{-2}$

➤ Use of ferromagnetic layers :

☺ Significant variations of  $\mu$  under a weak bias field (max 250 Oe)

☹ Application of an external DC magnetic field (coils integration)



$\Delta H_0 = 250\text{Oe}$  Fr:1,8→2,1GHz

→  $\Delta F/F = 19\%$

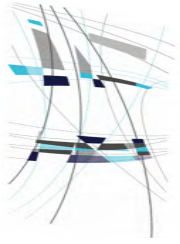


## Association of piezoelectric and magnetostrictive materials

☺ high tunability of ferromagnetic materials

☺ enable an electrical biasing

☺ low losses compared with ferroelectrics

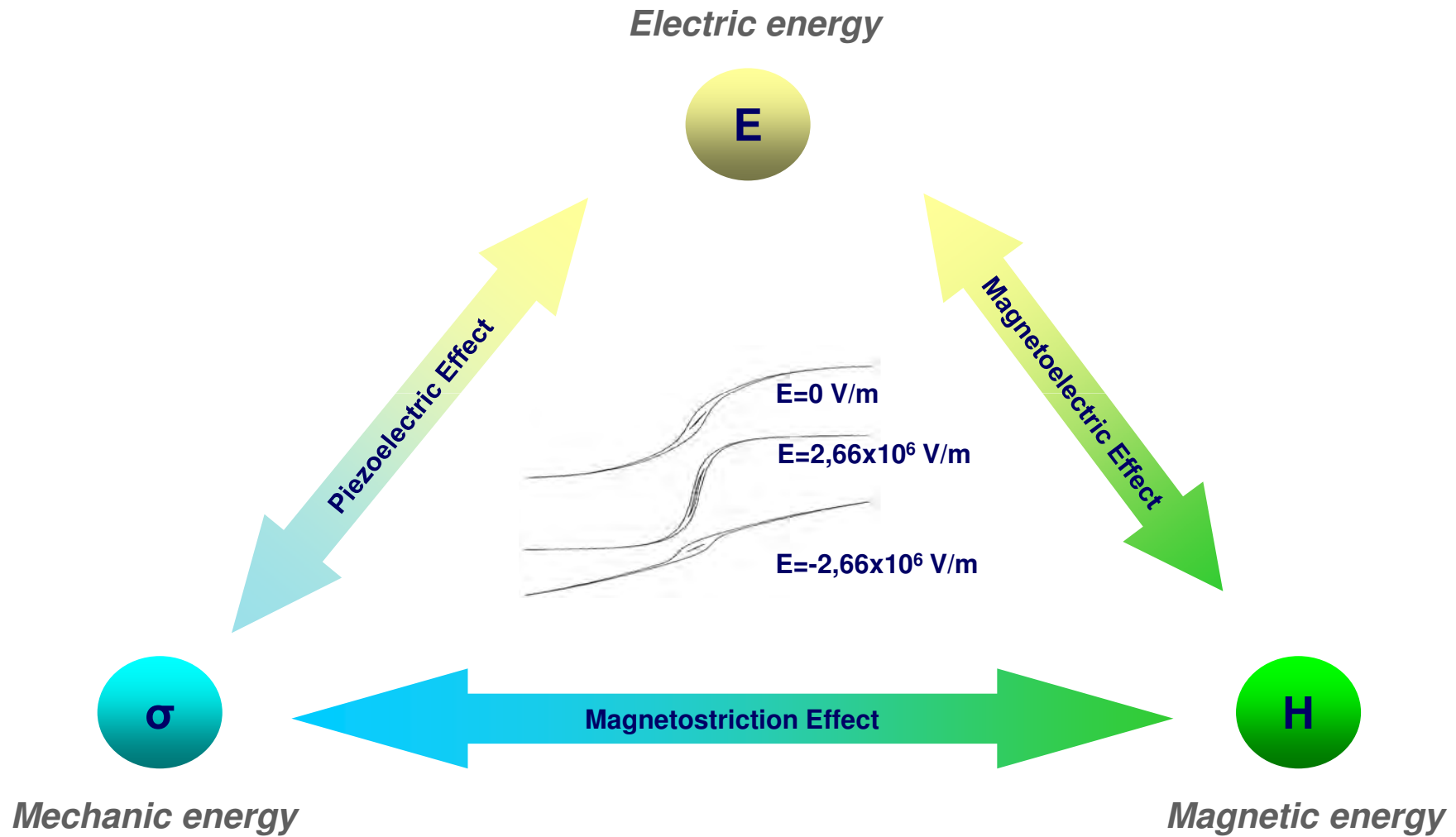


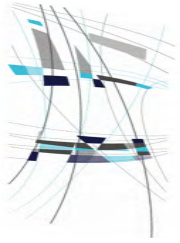
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# Magnetolectric effects





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# Theoretical aspects

Maxwell and Callen's relationships for an « electro-magneto-mechanics » system give us:

$$\frac{\partial \sigma_{ij}}{\partial S_{kl}} = C_{ijkl}, \quad \frac{\partial \sigma_{ij}}{\partial E_n} = -d_{ijn}, \quad \frac{\partial \sigma_{ij}}{\partial \delta T} = -\tau_{ij}$$

$$\frac{\partial D_n}{\partial S_{kl}} = d_{nkl}, \quad \frac{\partial D_m}{\partial E_n} = \epsilon_{mn}, \quad \frac{\partial D_m}{\partial \delta T} = \zeta_m$$

$$\frac{\partial \Theta}{\partial S_{kl}} = \tau_{kl}, \quad \frac{\partial \Theta}{\partial E_n} = \zeta_n, \quad \frac{\partial \Theta}{\partial \delta T} = C_v$$

Isocaloric process:

Integration of  $\sigma$  and  $D$   
as a function of  $S$  and  $E$

Piezoelectric equations:

$$\sigma_{ij}(E, S) = C_{ijkl}^E S_{kl} - d_{kij} E_k$$

$$D_i(E, S) = d_{ikt} S_{kl} + \epsilon_{ij}^S E_j$$

$$\frac{\partial \sigma_{ij}}{\partial S_{kl}} = C_{ijkl}, \quad \frac{\partial \sigma_{ij}}{\partial H_n} = -q_{ijn}, \quad \frac{\partial \sigma_{ij}}{\partial \delta T} = -\tau_{ij}$$

$$\frac{\partial B_n}{\partial S_{kl}} = q_{nkl}, \quad \frac{\partial B_m}{\partial H_n} = \mu_{mn}, \quad \frac{\partial B_m}{\partial \delta T} = \zeta_m$$

$$\frac{\partial \Theta}{\partial S_{kl}} = \tau_{kl}, \quad \frac{\partial \Theta}{\partial H_n} = \zeta_n, \quad \frac{\partial \Theta}{\partial \delta T} = C_v$$

Isocaloric process:

Integration of  $\sigma$  and  $B$   
as a function of  $S$  and  $H$

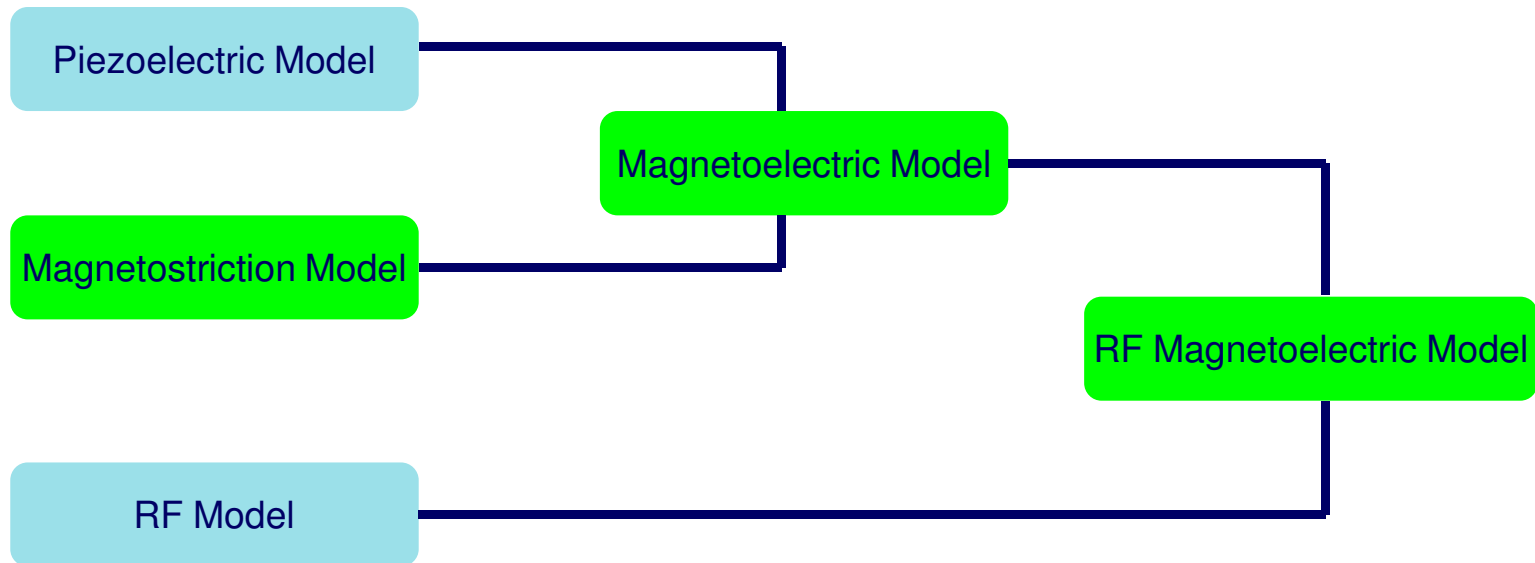
Magnetostriction equations:

$$\sigma_{ij}(H, S) = C_{ijkl}^H S_{kl} - q_{kij} H_k$$

$$B_i(H, S) = q_{ikt} S_{kl} + \mu_{ij}^S H_j$$

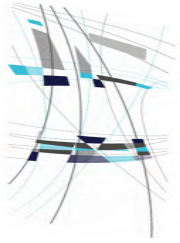


# Theoretical aspects



« X » Model Already integrated in Comsol Multiphysics

« X » Model Developed and Implemented in Comsol Multiphysics (at the Lab-STICC)



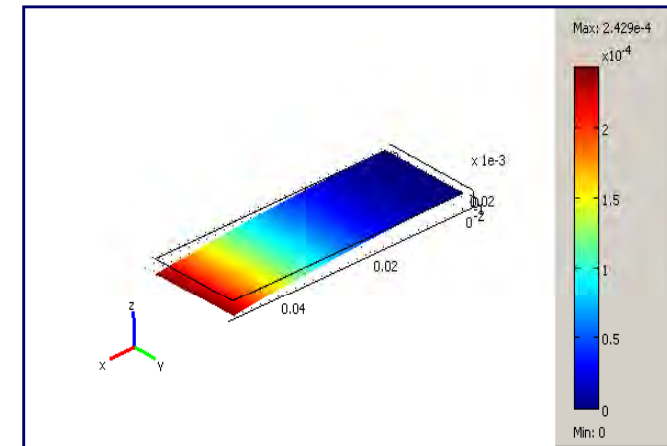
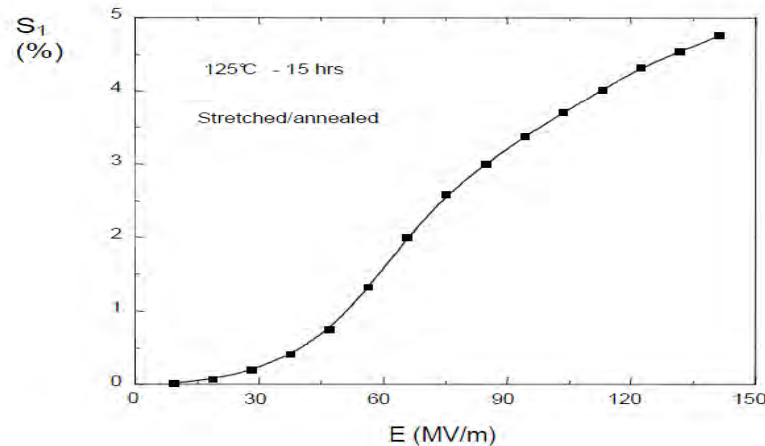
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# Modeling of magnetolectric structures

## Validation of piezoelectric model : Comparison between experimental and Comsol-based deflections of a PVDF cantilever



Comsol-based simulation of a PVDF cantilever

PVDF longitudinal strain as a function of strength electric field

\*Q. M. Zhang and col. « Recent advances in highly Electrostrictive P(VDF-TrFE-CFE) »

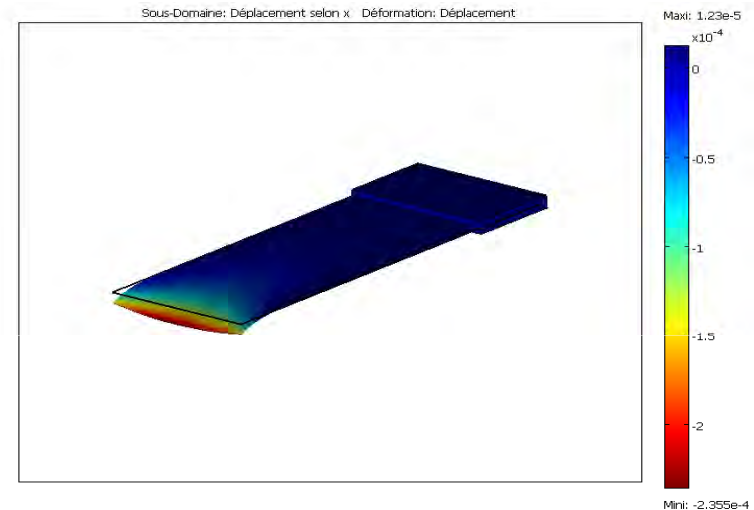
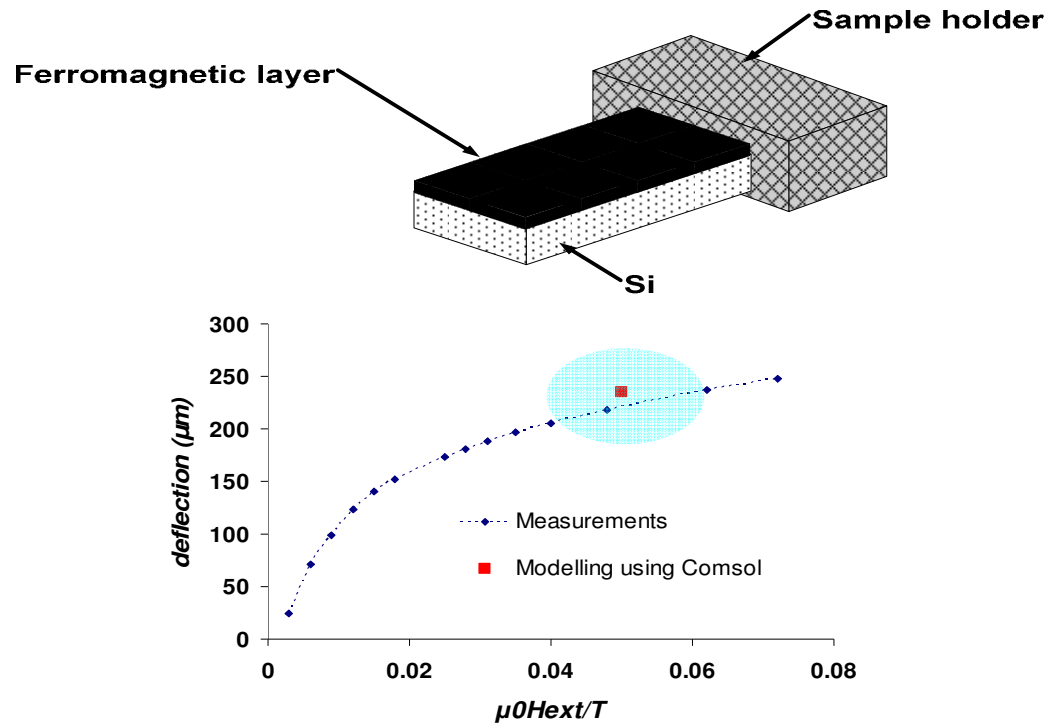


Good agreement between experimental and Comsol-based deflections



# Modeling of magnetoelectric structures

## Validation of the developed magnetostrictive model



Finite-element calculated deflection of a TbDyFe / Si cantilever under a DC magnetic field

Comparison between Comsol-based calculated deflection and experimental results for a TbDyFe / Si cantilever.



Good agreement between experimental and Comsol-based deflections



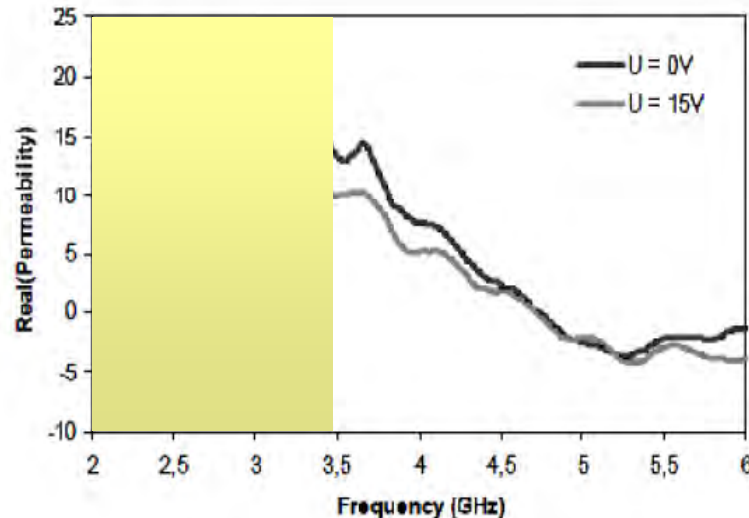
# Modeling of magnetoelectric structures

## Modeling of a trilayer magnetoelectric structure

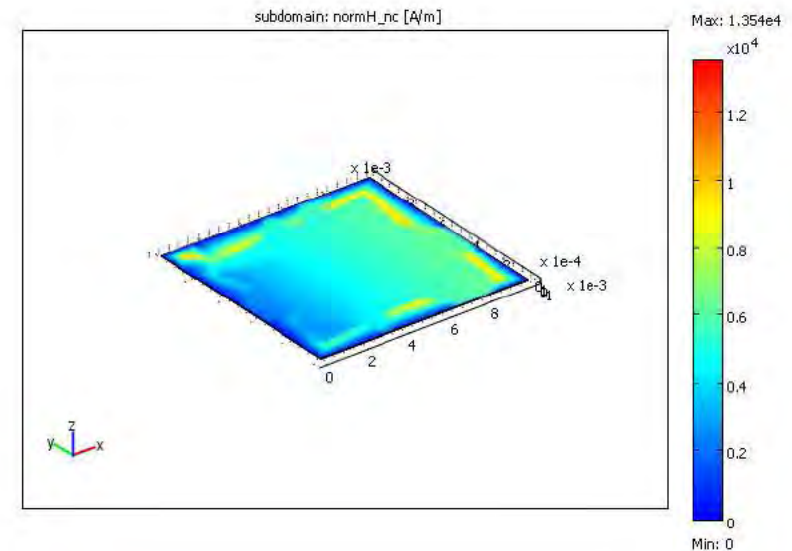
**PVDF**  
 $e = 10\mu\text{m}$ ,  $\epsilon = 11$ ,  $d_{33} = -33 \text{ pC/N}$ ,  $d_{31} = 23 \text{ pC/N}$



**FeCoB Magnetostrictive layers**  
 $e = 140 \text{ nm}$ ,  $H_K = 20 \text{ Oe}$ ,  $4\pi M_s = 19000 \text{ G}$ ,  $\lambda_s = 50.10^{-6}$



Permeability spectrum measured in a tri-layered (FeCoB / PVDF / FeCoB) structure under an electrical voltage  $U=15\text{V}$ .



Induced magnetic field about of 600e in the FeCoB layer under a static electric field.

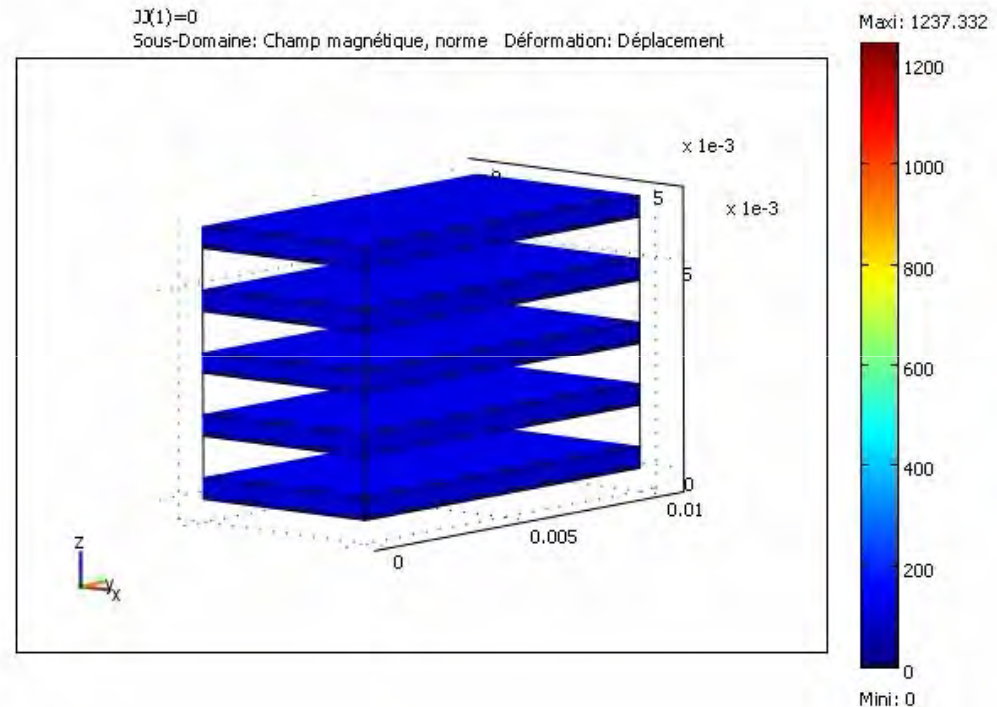
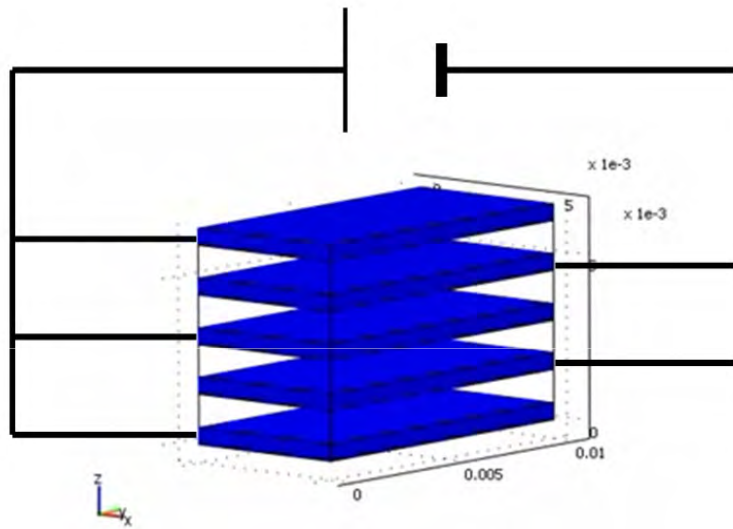


Decrease of the permeability ( $\sim 30\%$ ) under an electric field of 1,5MV/m, corresponding with the calculated of the magnitude field induced using static magnetoelectric model



# Modeling of magnetoelectric structures

## Modeling of a multilayer {piezoelectric/magnetostrictive}x5 structure



☺ Stronger interaction with RF field (coupling)

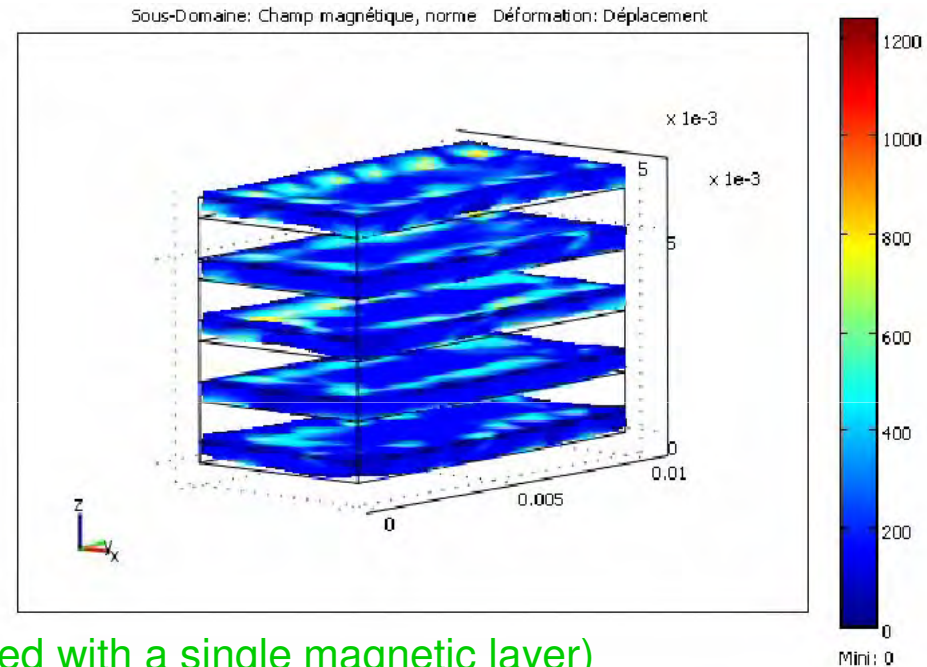
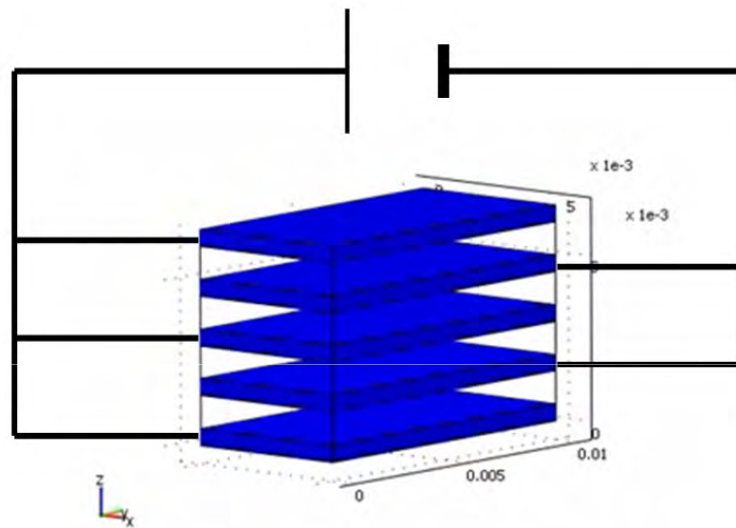
☹ Technologically complicated

➔ Multilayer composite driven by a piezoelectric actuator (electric field bias)



# Modeling of magnetoelectric structures

## Modeling of a multilayer {piezoelectric/magnetostrictive}x5 structure



☺ Stronger interaction with RF field (compared with a single magnetic layer)

☹ Technologically complicated

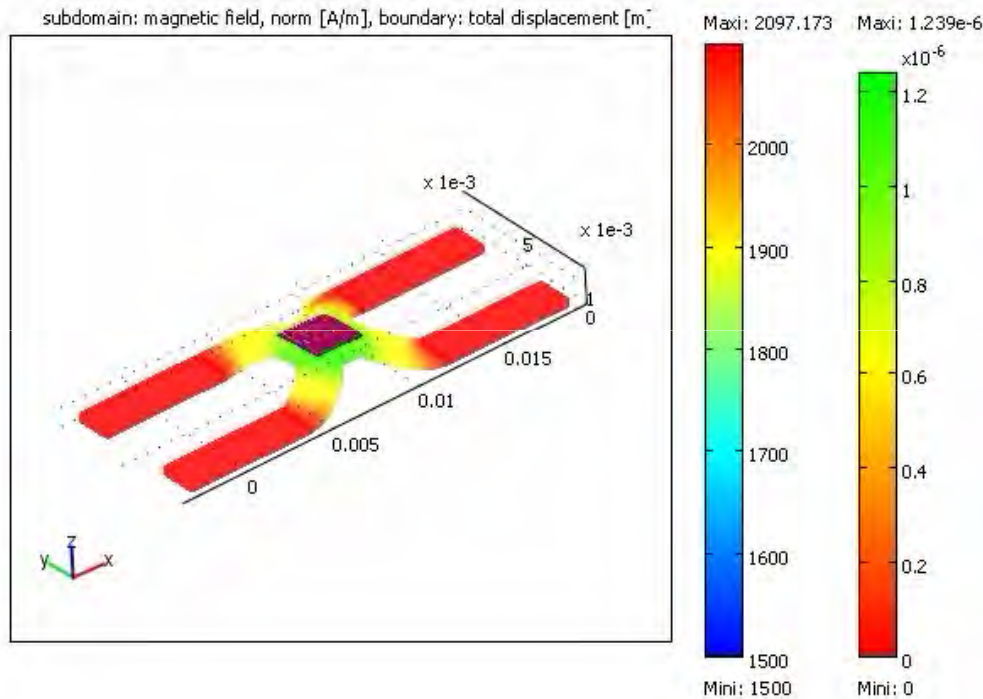
➡ Multilayer composite driven by a piezoelectric actuator (electric field bias)





# Modeling of magnetolectric structures

## Uniaxial piezoelectric actuators for microwave tunable applications



☺ The stress induced by the application of electric field leads to an induced magnetic field about of 250e in the multilayer

☺ Low DC bias Voltage

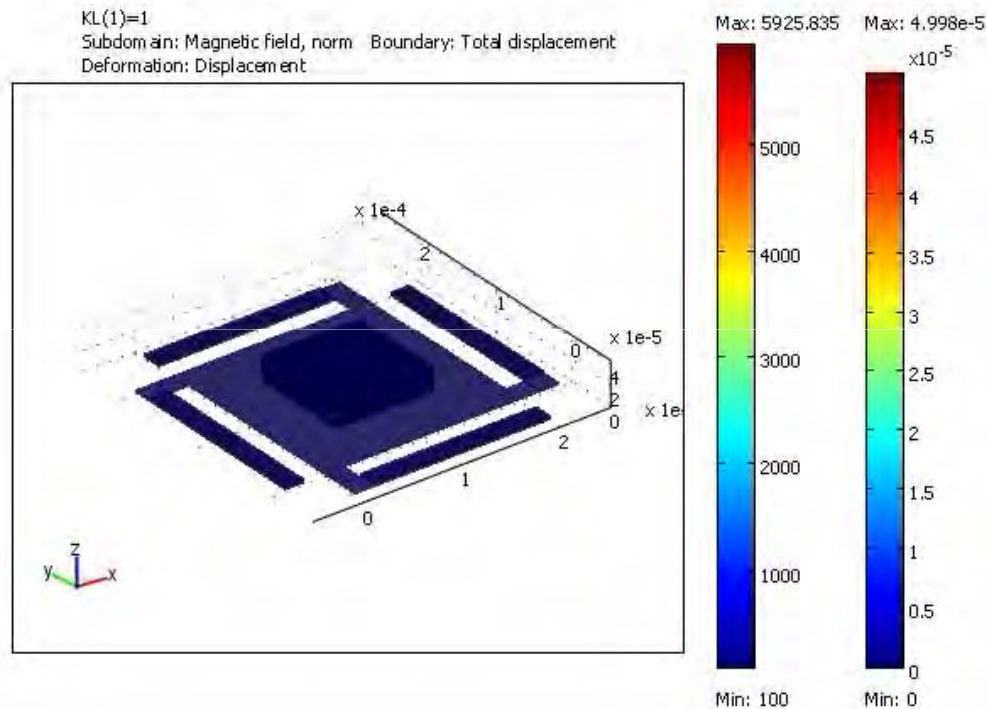
☺ Easy integration in RF circuit

☹ Weak strain induced at interface { Multilayer / piezoelectric actuator } (compared with biaxial structure)



# Modeling of magnetoelectric structures

## Biaxial piezoelectric actuators for microwave tunable applications



☺ Stronger strain induced in the Multilayer.

☺ Easy integration in RF circuit

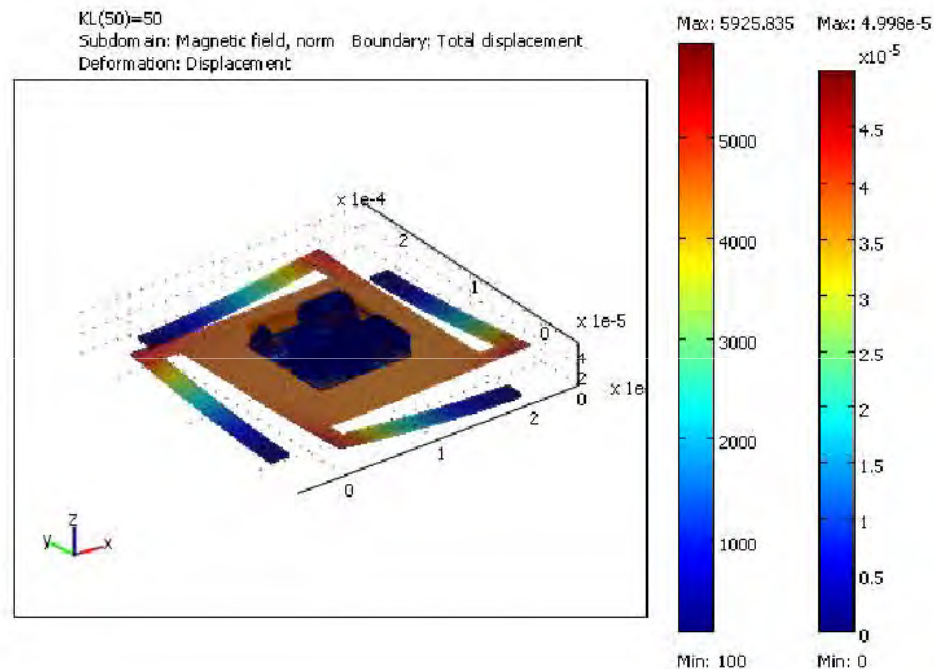
☺ Low DC bias Voltage

☹ Complicated fabrication



# Modeling of magnetoelectric structures

## Biaxial piezoelectric actuators for microwave tunable applications

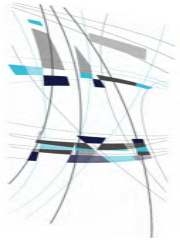


☺ Stronger strain induced in the Multilayer.

☺ Easy integration in RF circuit

☺ Low DC bias Voltage

☹ Complicated fabrication



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# RF simulations of magnetolectric structures

## Magnetolectric tunable microstrip line

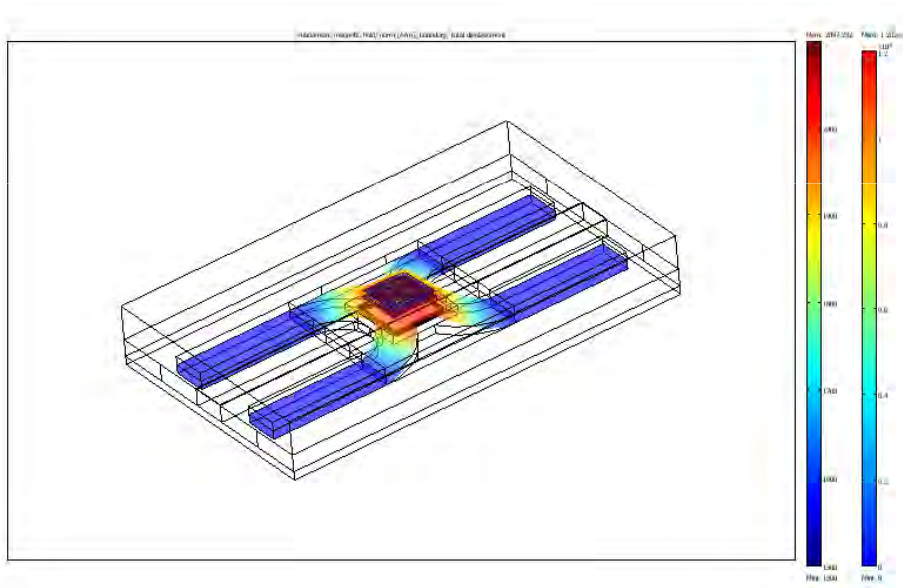
Stored Solutions: Ha(V),....

Kittel law

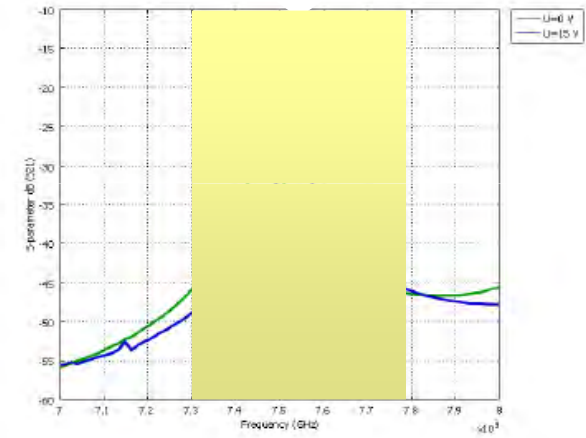
$$f, \alpha \propto \frac{1}{\mu(\Delta V)}$$

Step #1: Solved using static magnetolectric model

Step#2: Solved using RF model



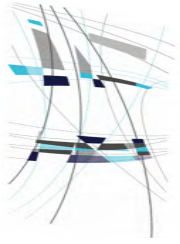
Induced magnetic field distribution , actuated by a piezoelectric actuator (uniaxial), under an electrical voltage U=15V



Magnitude of the transmission parameter of a microstrip line loaded by a magnetodielectric actuator for 0V and 15V.

☺ Tuning of the resonance peak about of 50MHz under an external electric field (U=15V)





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# Conclusion

➤ Development of a magnetostriction, and magnetoelectric specific models using Comsol Multiphysics

➤ Capacity to determine:

- the total displacement of the actuator
- the stress induced in the ferromagnetic layer
- the voltage induced magnetic field in the ferromagnetic layers

➤ Developement of a RF tunable magnetoelectric model:

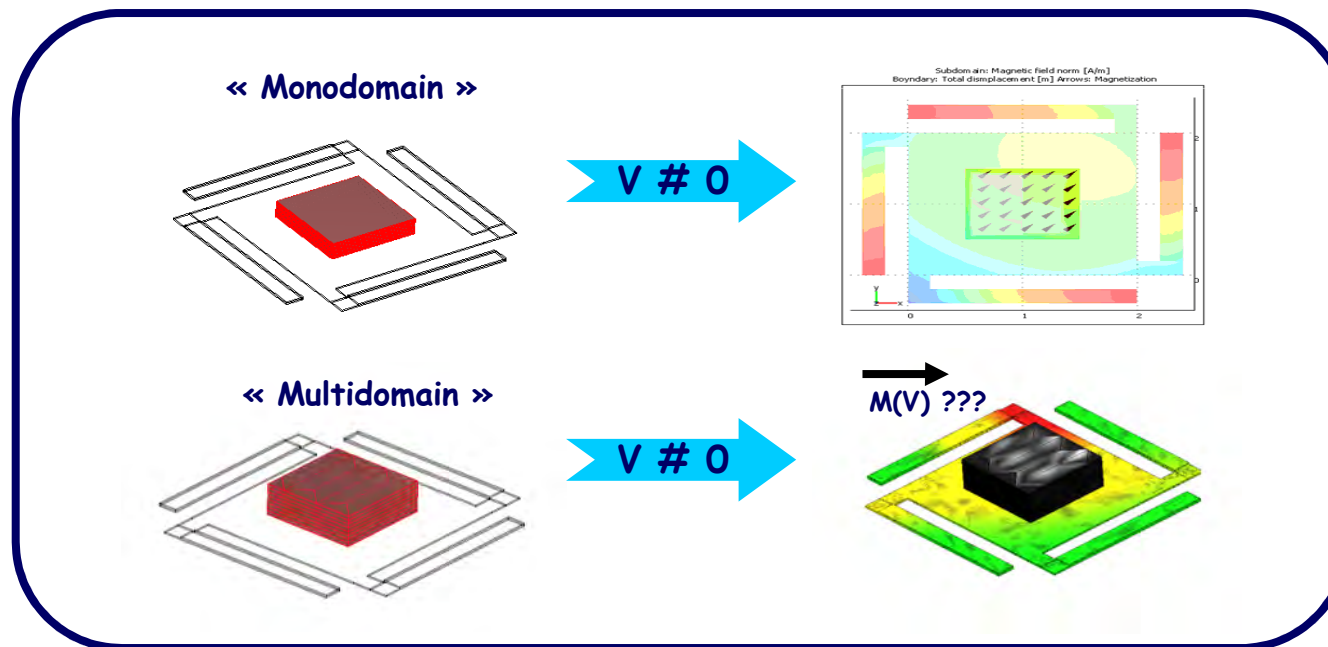
- simulation of a tunable microstrip line based on {ferromagnetic/PVDF} multilayers driven by an electric field



# Prospects

➤ Future use of Comsol:

- design of new magnetoelectric tunable RF functions
- implementation of the free energy model (rotation of the magnetization)
- implementation micromagnetic simulations (domains wall movements)







Thank You for Your Attention